# Data Calculator

#### Stratos Idreos & Data Systems Lab



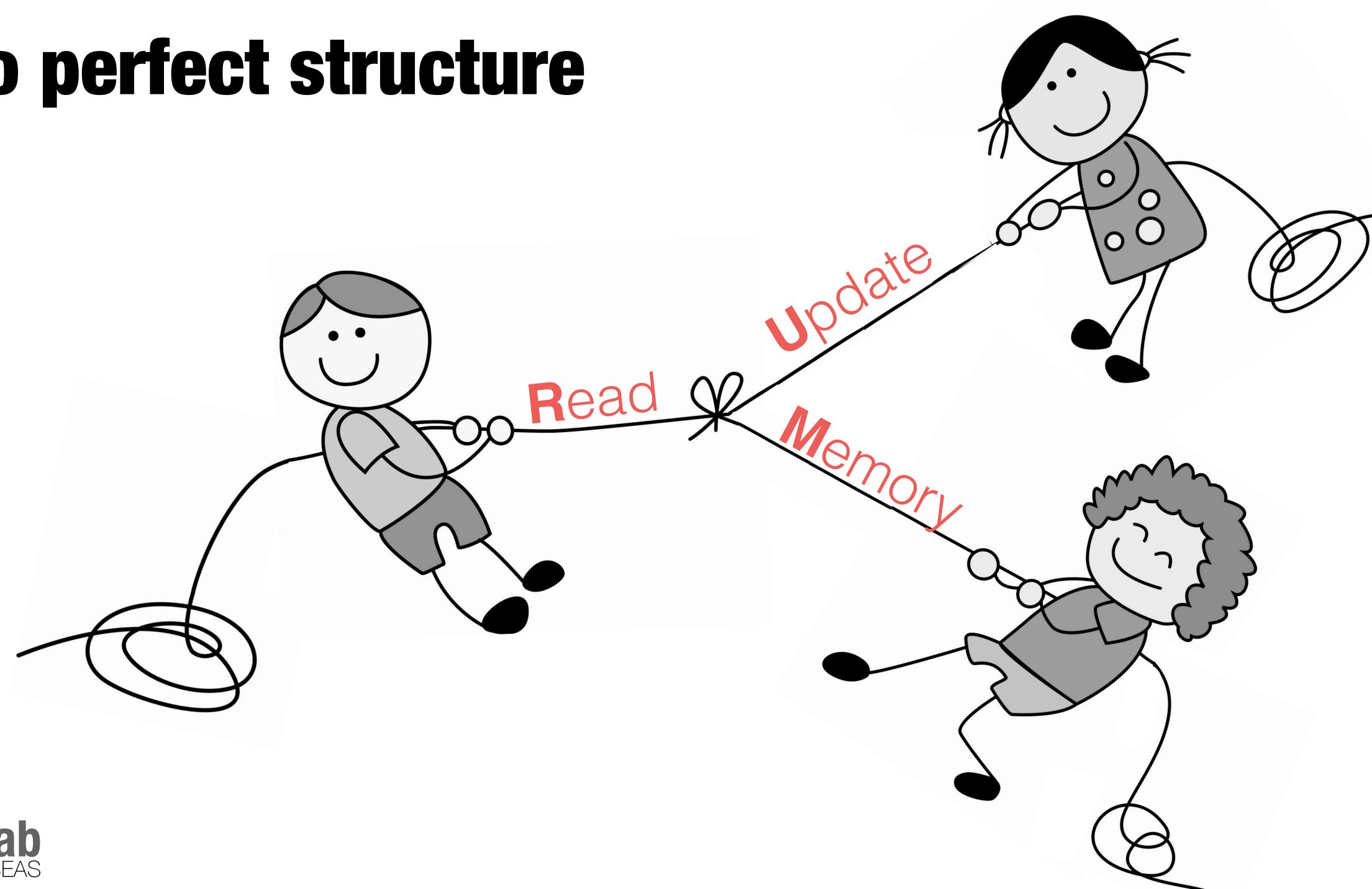
# Data Calculator

# WHAT IF WE COULD **REASON** ABOUT THE **DESIGN SPACE** OF DATA STRUCTURES?

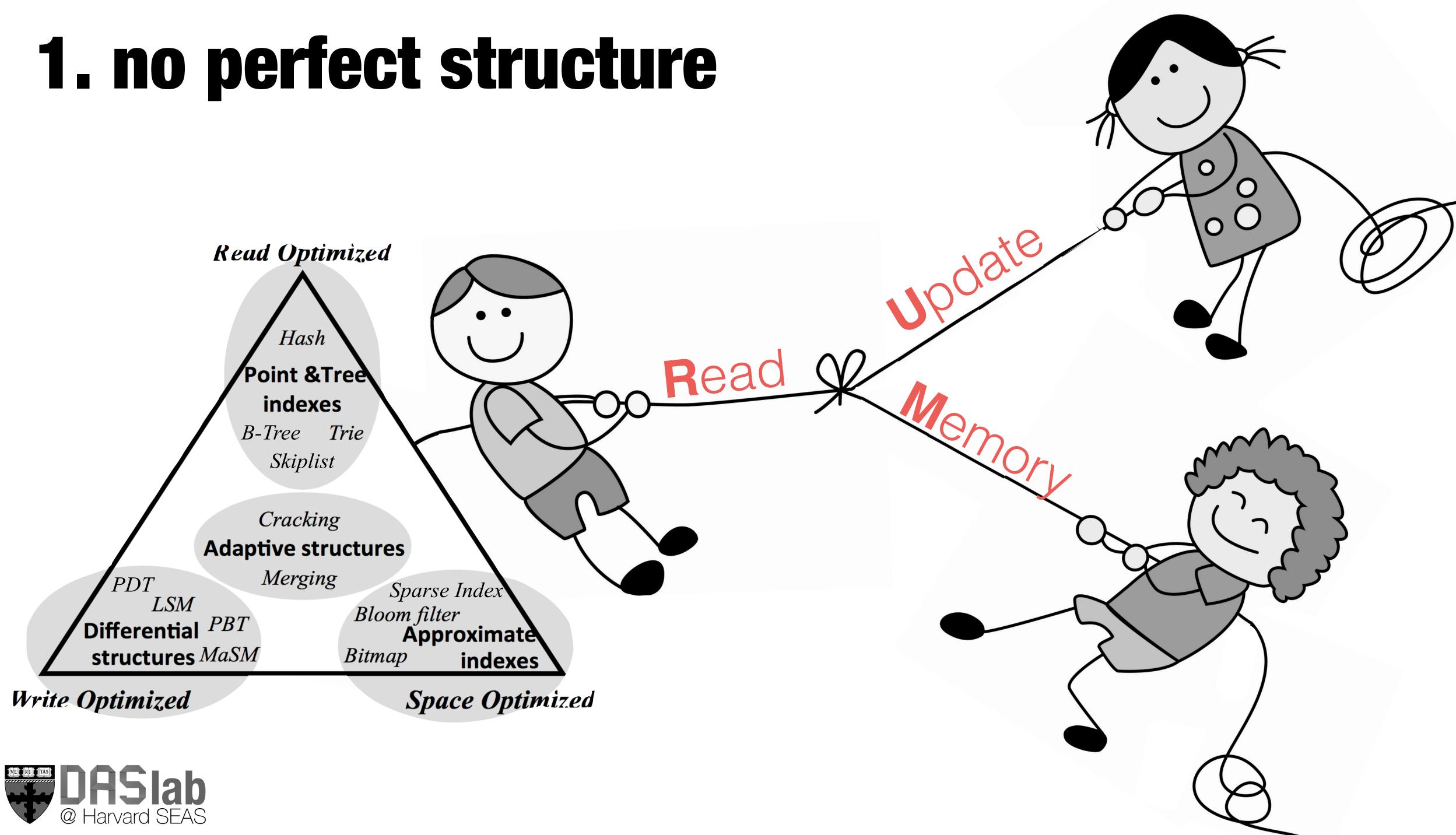
### Stratos Idreos & Data Systems Lab



# 1. no perfect structure

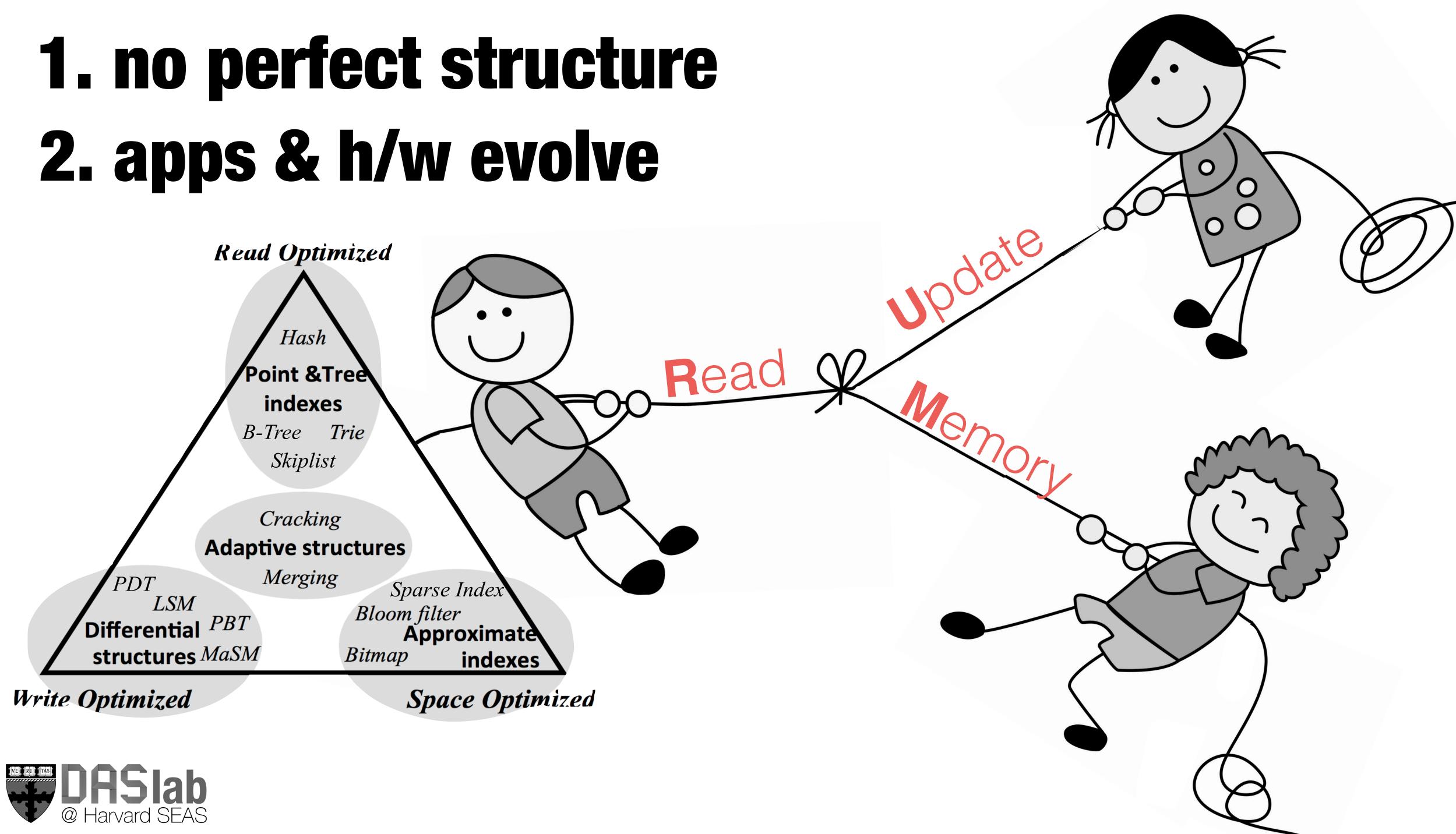




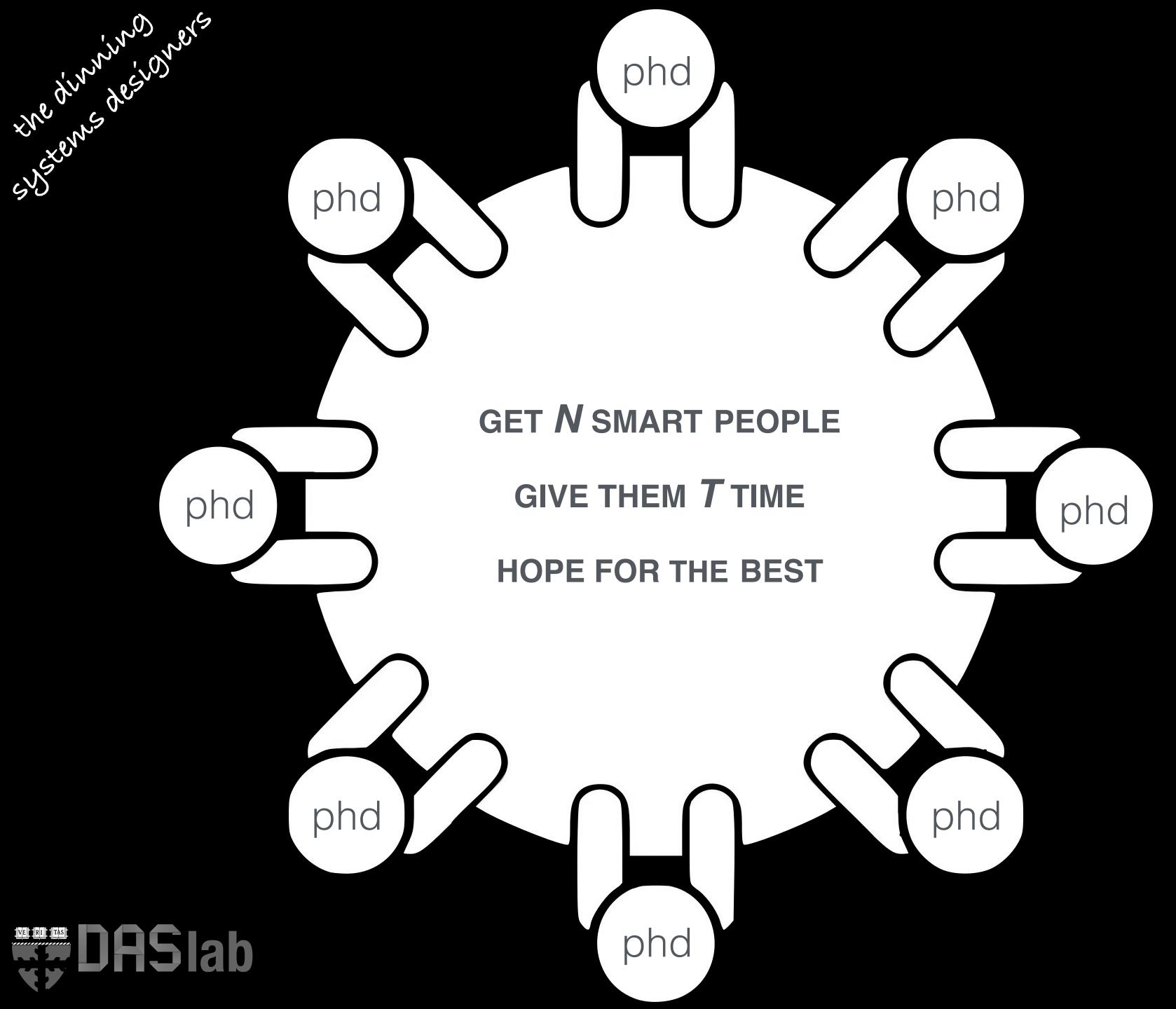


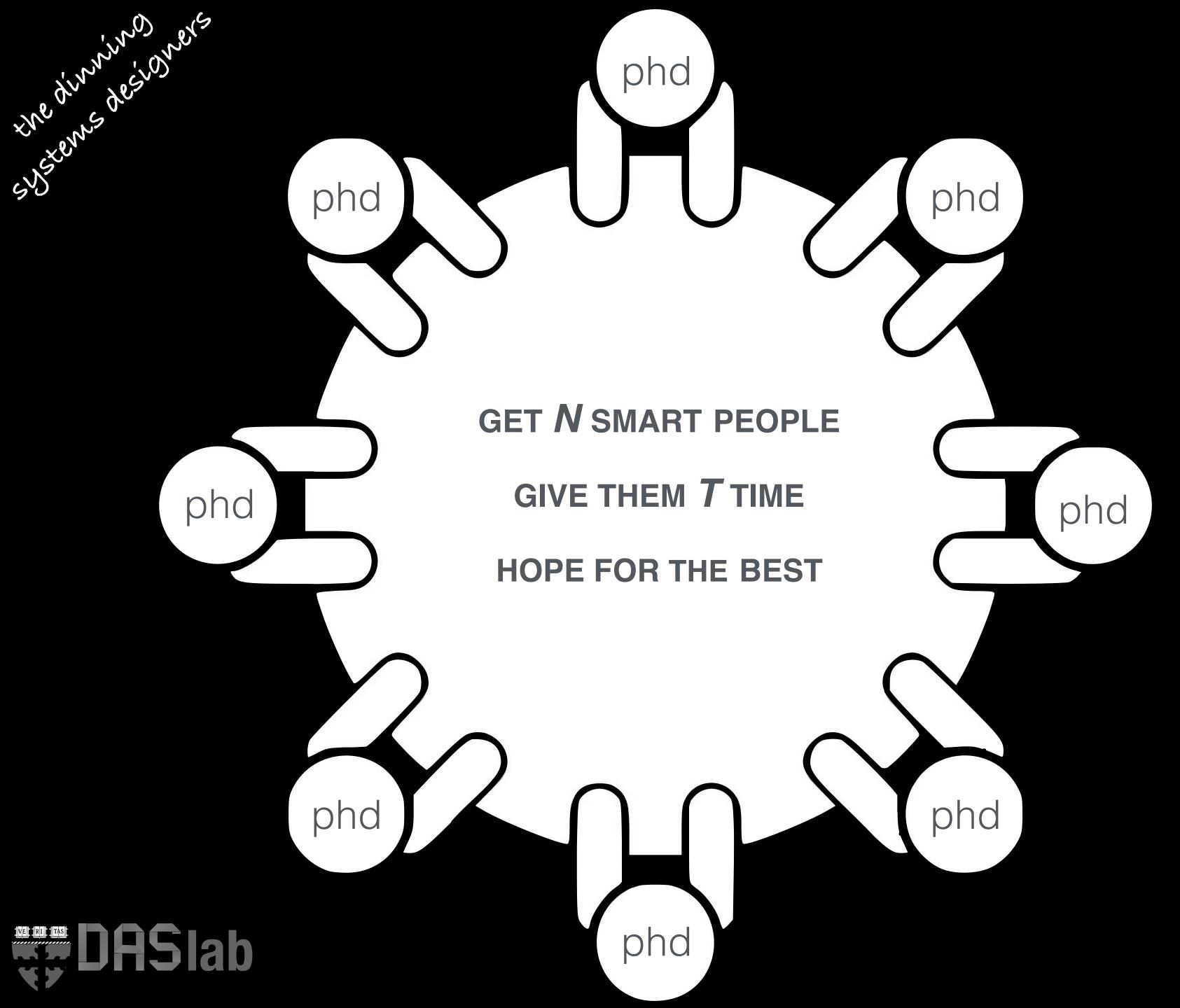


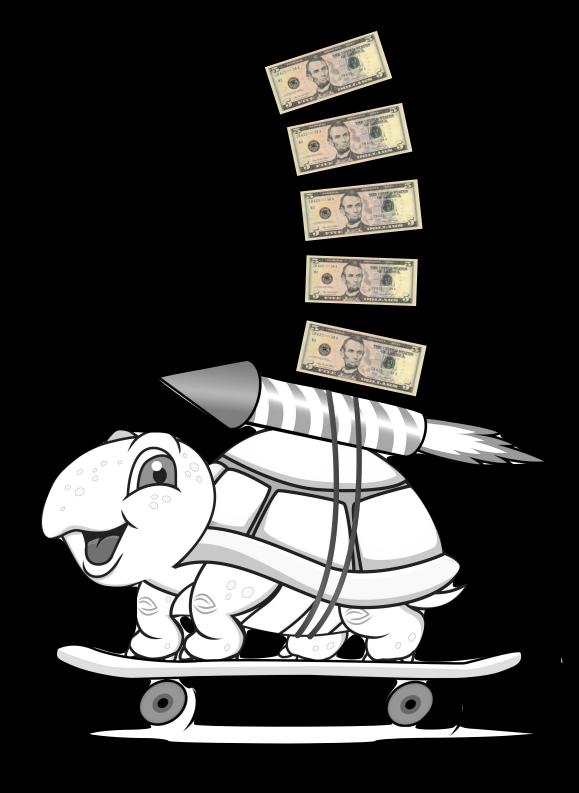
# 2. apps & h/w evolve

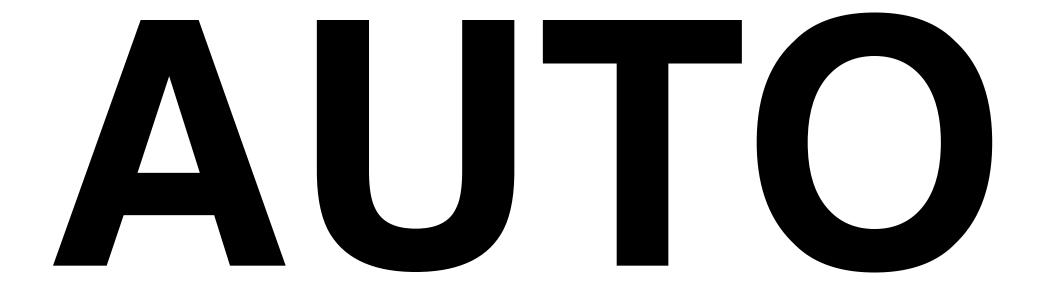




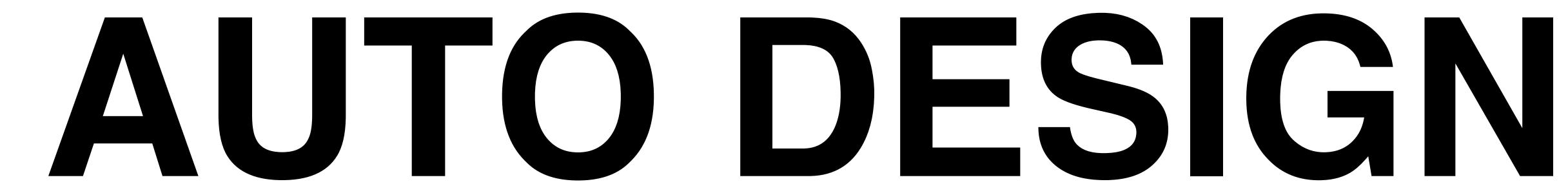














#### **ROBERT TARJAN**



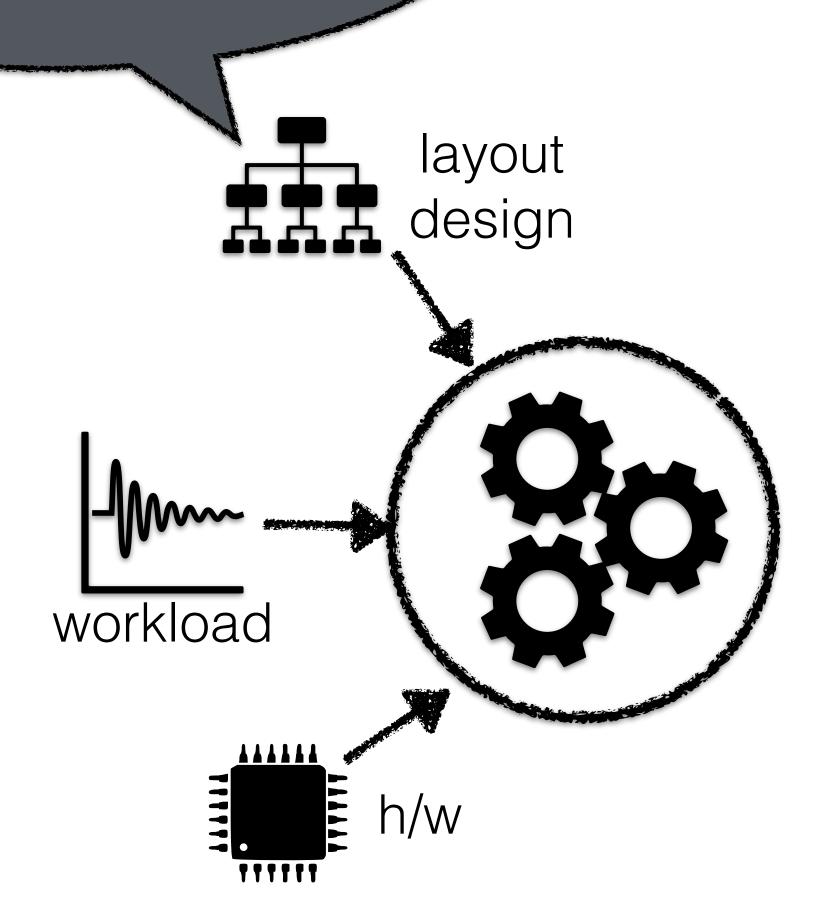
**"IS THERE A CALCULUS OF DATA STRUCTURES** by which one can choose the appropriate representation and techniques for a given problem?" (SIAM, 1978)



# HOW MANY AND WHICH? COMPUTE PERFORMANCE?

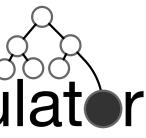


## **DESIGN SPACE OF POSSIBLE STORAGE LAYOUTS**

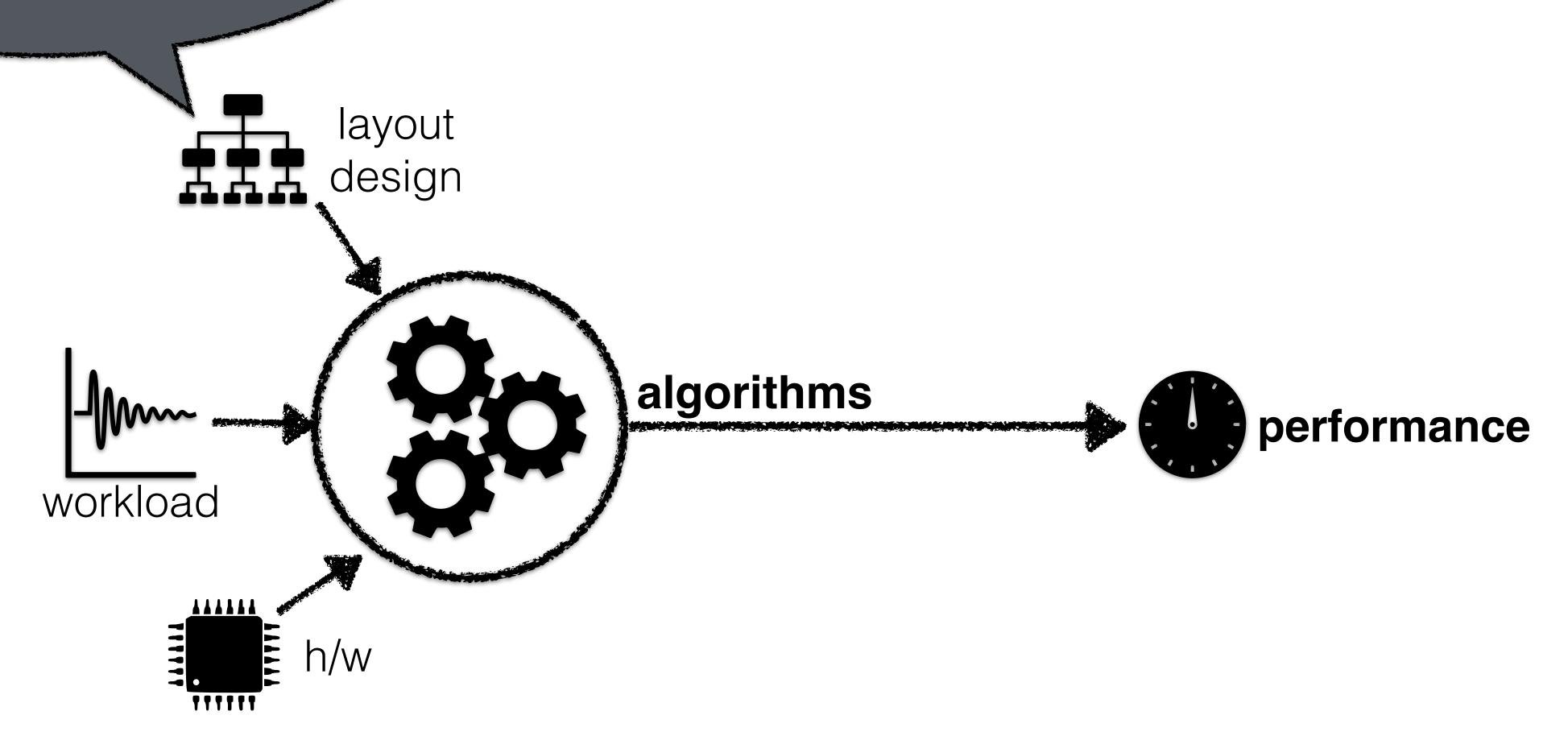




#### Data Calculater

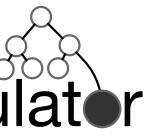


### **DESIGN SPACE OF POSSIBLE STORAGE LAYOUTS**

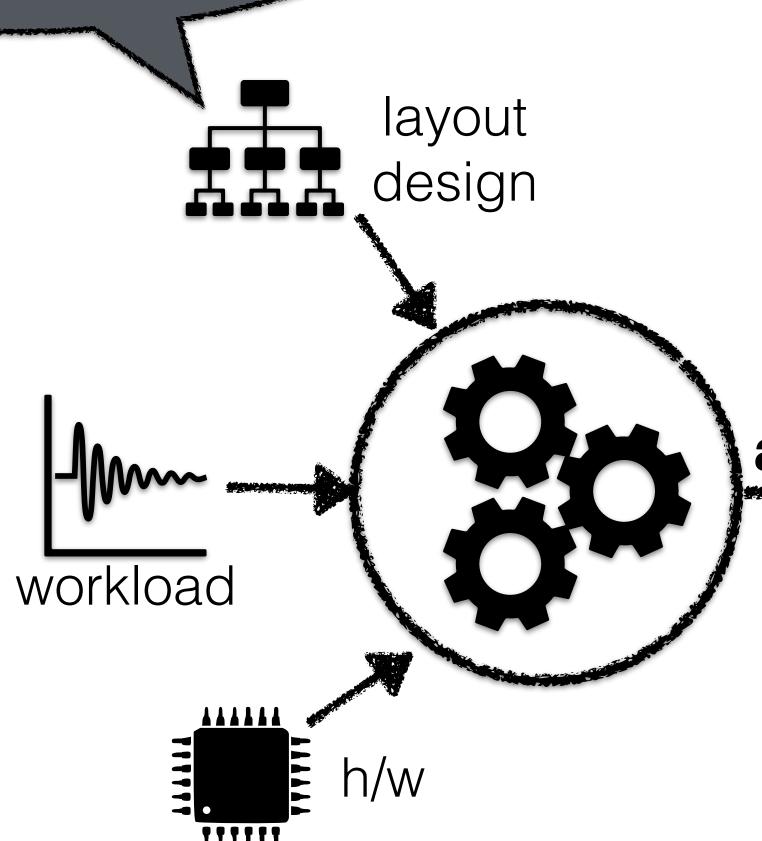




#### Data Calculator



### **DESIGN SPACE OF POSSIBLE STORAGE LAYOUTS**



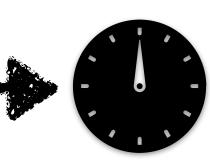
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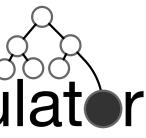
Data Calculator

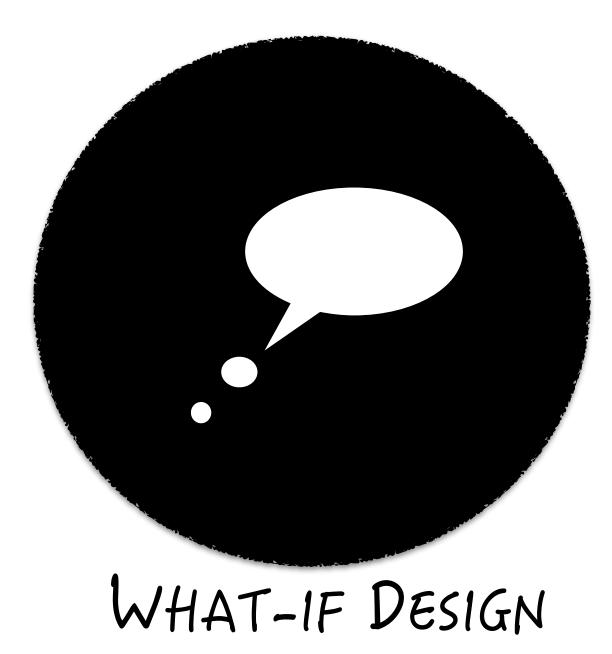
# without coding or accessing the h/w

algorithms



performance

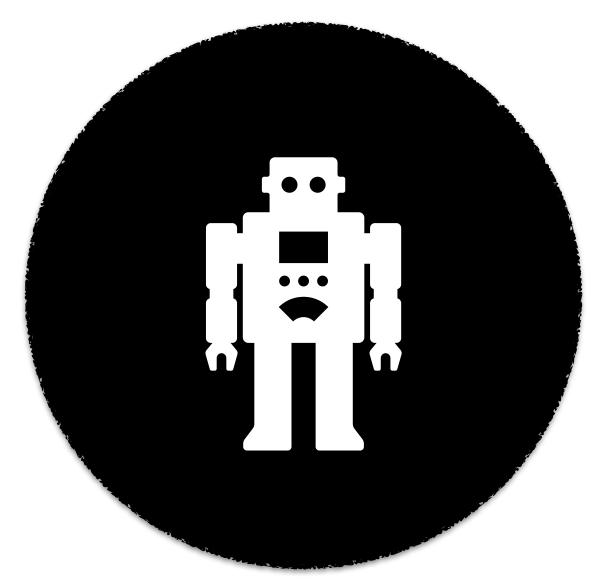




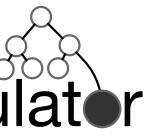




#### Data Calculater



SELF-DESIGNING SYSTEMS



# DESIGN SPACE



## COST SYNTHESIS

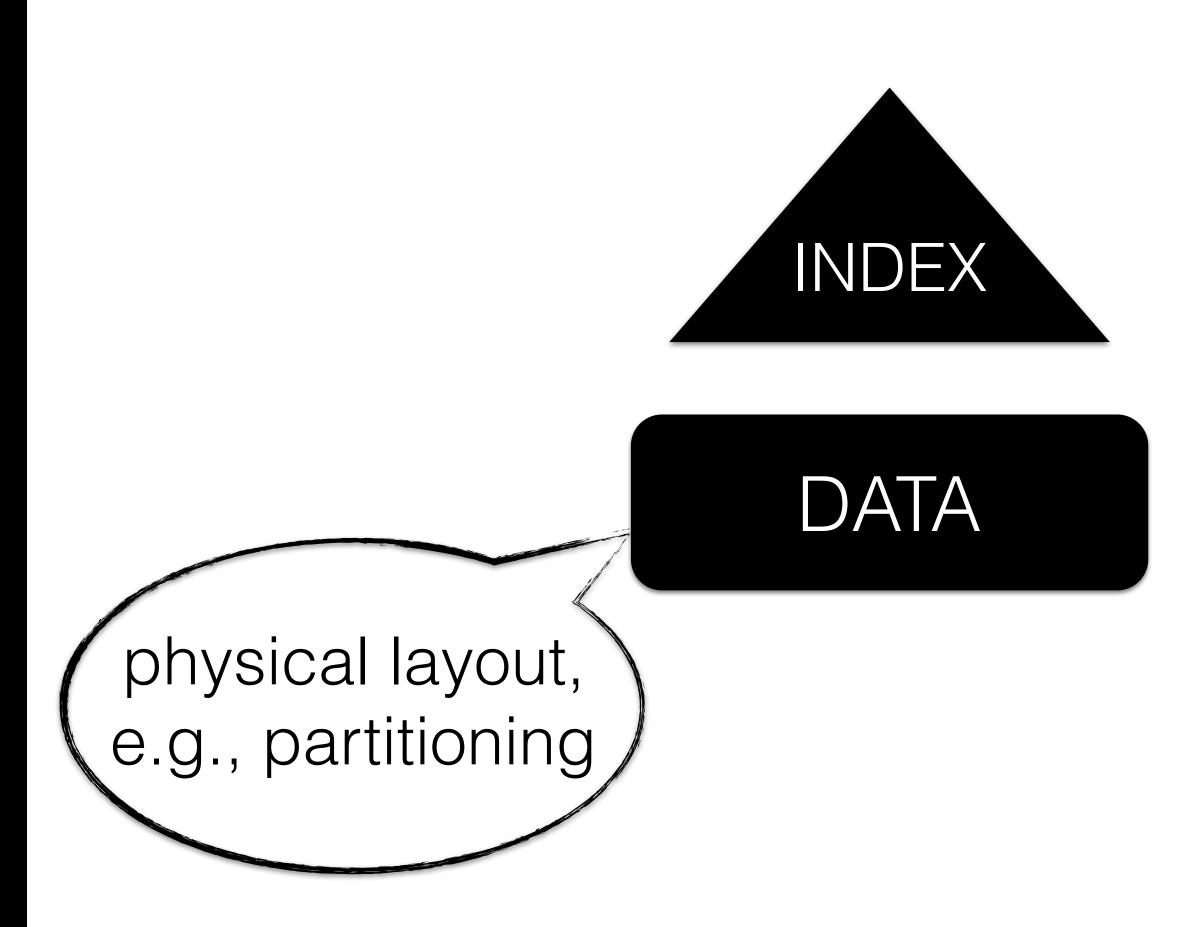
## HOW TO USE

# **B** DESIGN SPACE

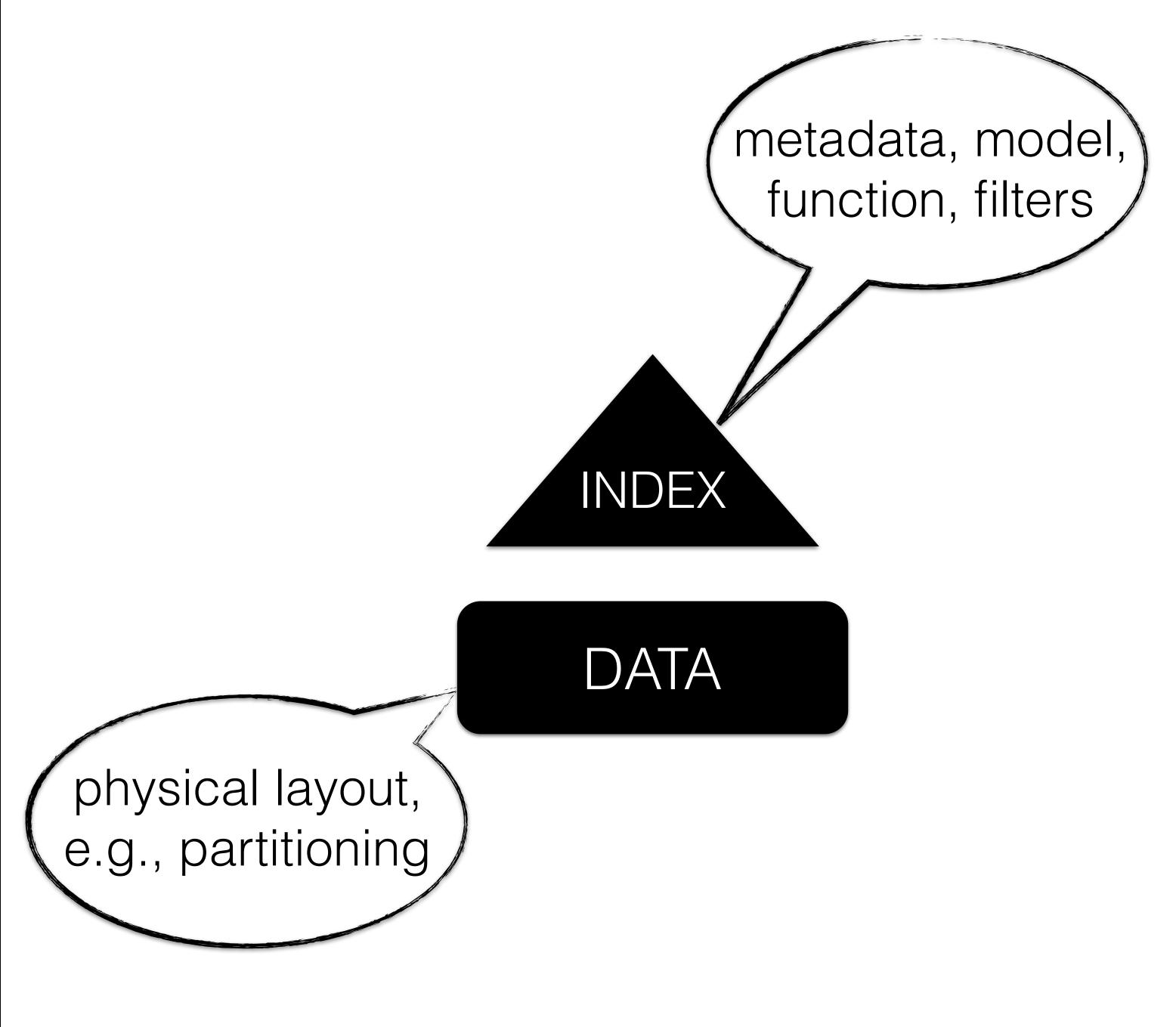




# **B** DESIGN SPACE

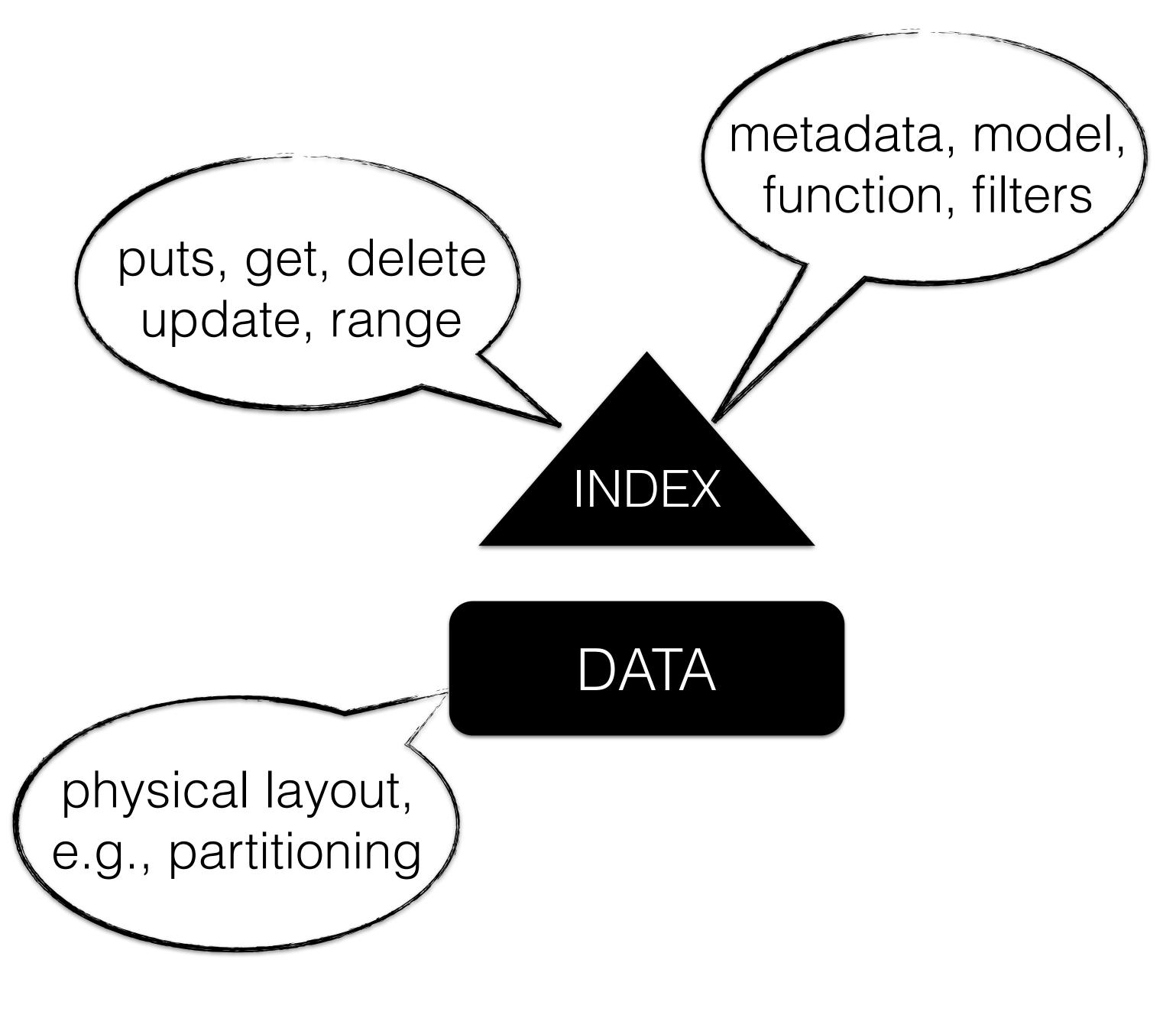


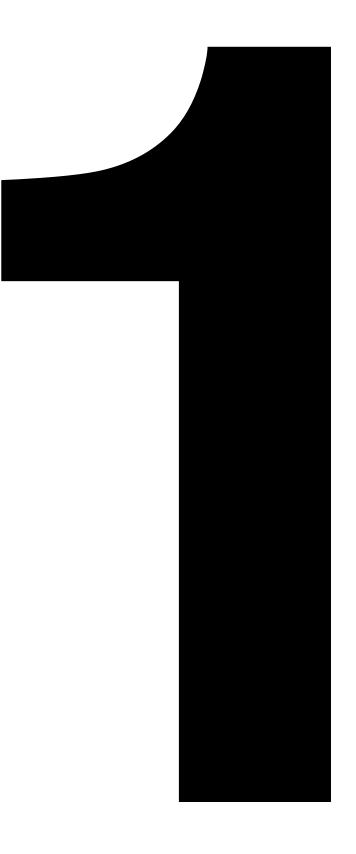
# **B** DESIGN SPACE



# 

# DESIGN SPACE









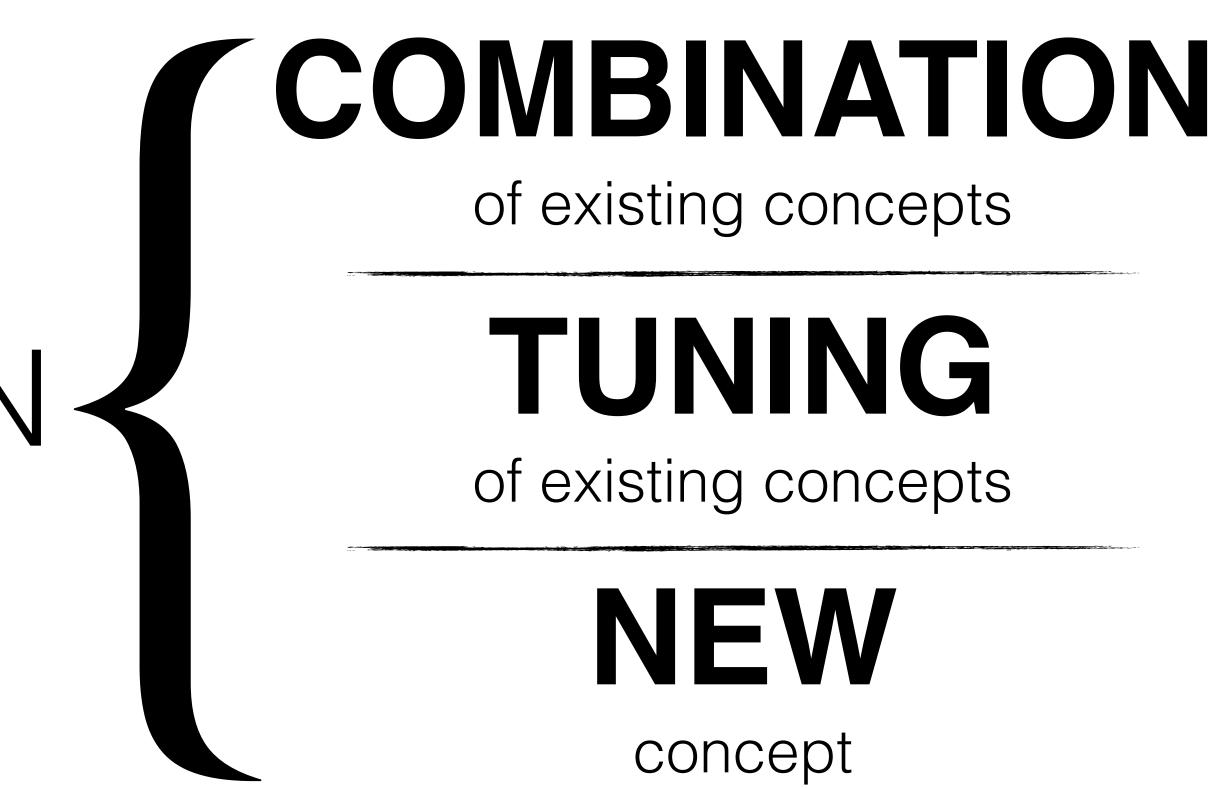
# EACH DESIGN: A **SET** OF CONCEPTS

{partitioning, links, fence pointers,...}



# DESIGN



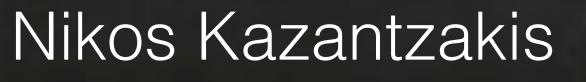








# (ALMOST) ALL DESIGNS ARE A COMBINATION/TUNING OF **EXISTING CONCEPTS**



I hope for nothing. I fear nothing. I am free.



if we know the **fundamental** building blocks,

# how they combine and their properties,



if we know the **fundamental** building blocks,

# how they combine and their properties,

### then we can **automate** the discovery of novel combinations and tunings



if we know the **fundamental** building blocks,

## DESIGN SPACE

if we know the **fundamental** building blocks, how they combine and their properties,

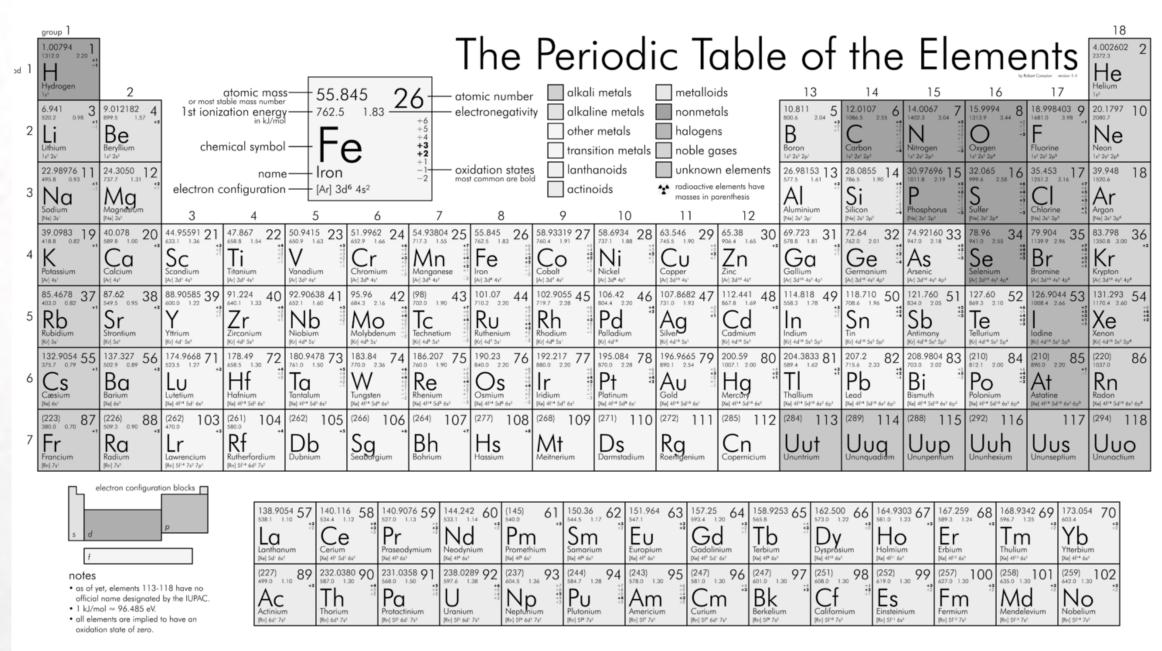
then we can **automate** the discovery of novel combinations and tunings



NAVIGATION

# PERIODIC TABLE OF ELEMENTS explains and predicts missing elements

Dimitri Mentelev



structures elements based on atomic number, electron configuration, and recurring chemical properties



5 6 7 8 9 10 11 12 13 14 15 16 17 18

	原子番号(陽子数)													2 Me
	1		5	6	7	8	9	10						
小素 元素名 (和名)										0.6		M.E.		235
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		п	1	UNICUL	- 1	13	14	15	16	17	18			
										Si	P	S	CI	Ar
	23	24	25	26	27	28	29	30	31	32	33	34	35	36
Ti	V	Cr	Mn	Fe	Со	Ni	Cu	Zn	Ga	Go	LE.	tuy Co	Of De	20262
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Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In		Sb	10000	A CONTRACTOR	Xe
2	73	74	75	76	77	78	79	80	81	82	83	84	85	86
1.15	7.29%	101	De	122.20	2.2	Di	A	200	2001.	0	1292	1401.00	1.000	282
Hf	Ta	W	Re	Os	lr	Pt	Au	Hg	T	Pb	B	Po	At	Rn
04	105	106	107	108	109	110	111	112	113	114	115	116	117	118
Rf	Db	11.			10 million (10 million)				118	F		5 L	/ 117	118
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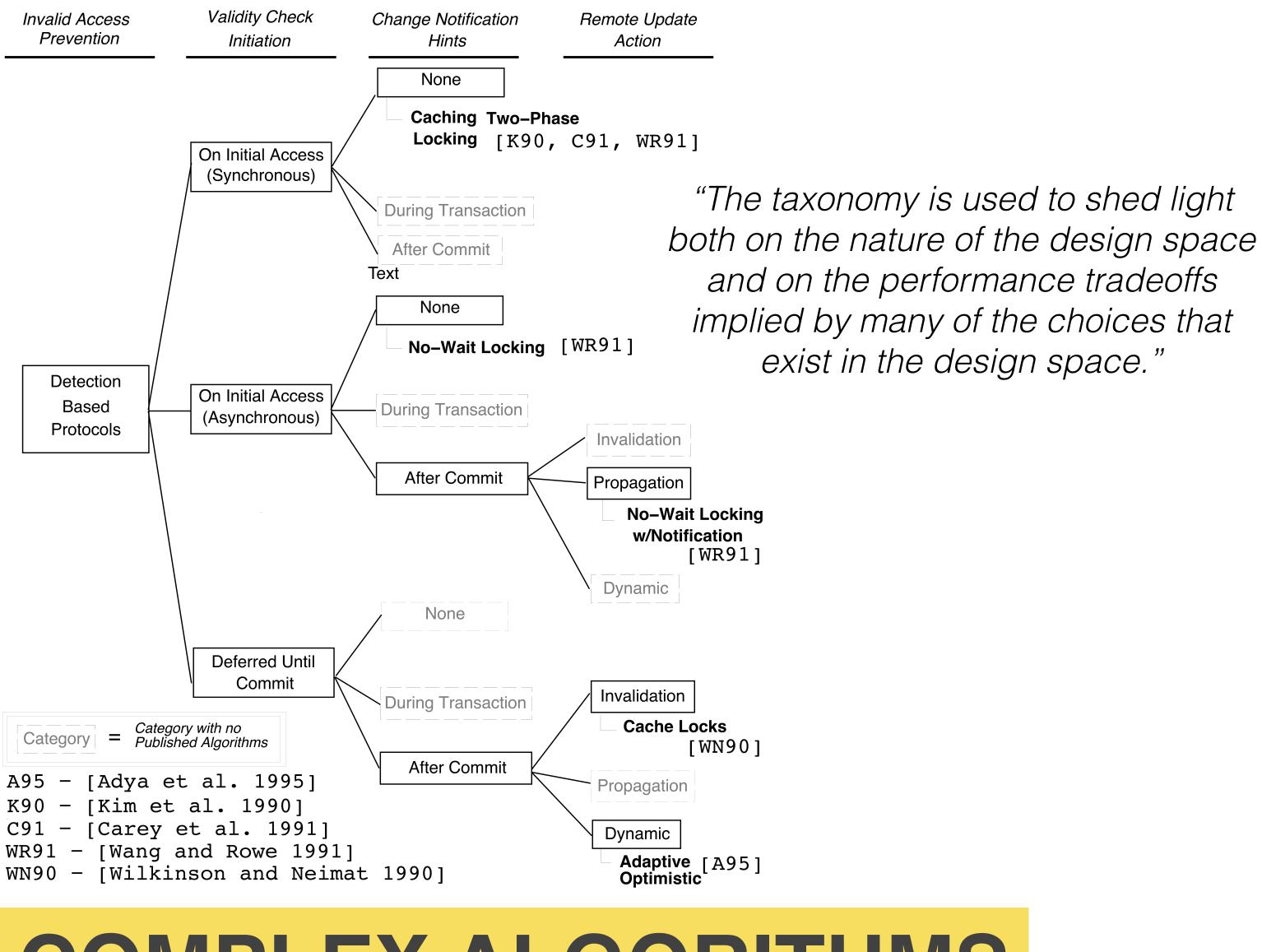




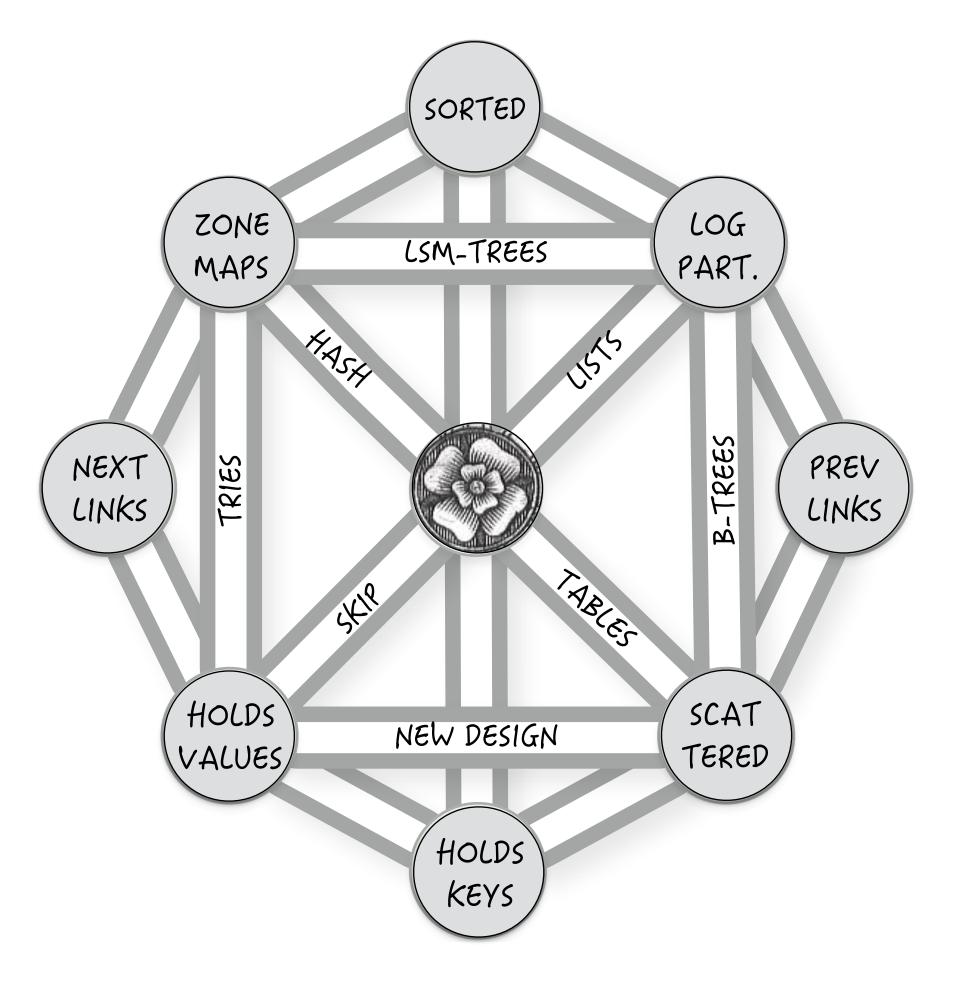
Detection Based Protocols Category = Category with no Published Algorithms A95 - [Adya et al. 1995] K90 - [Kim et al. 1990] C91 - [Carey et al. 1991]

Invalid Access Prevention

# TAXONOMY OF transactional cache consistency maintenance Mike Franklin













## FIRST PRINCIPLE: DESIGN CONCEPT THAT IS NOT POSSIBLE OR MEANINGFUL TO BREAK FURTHER









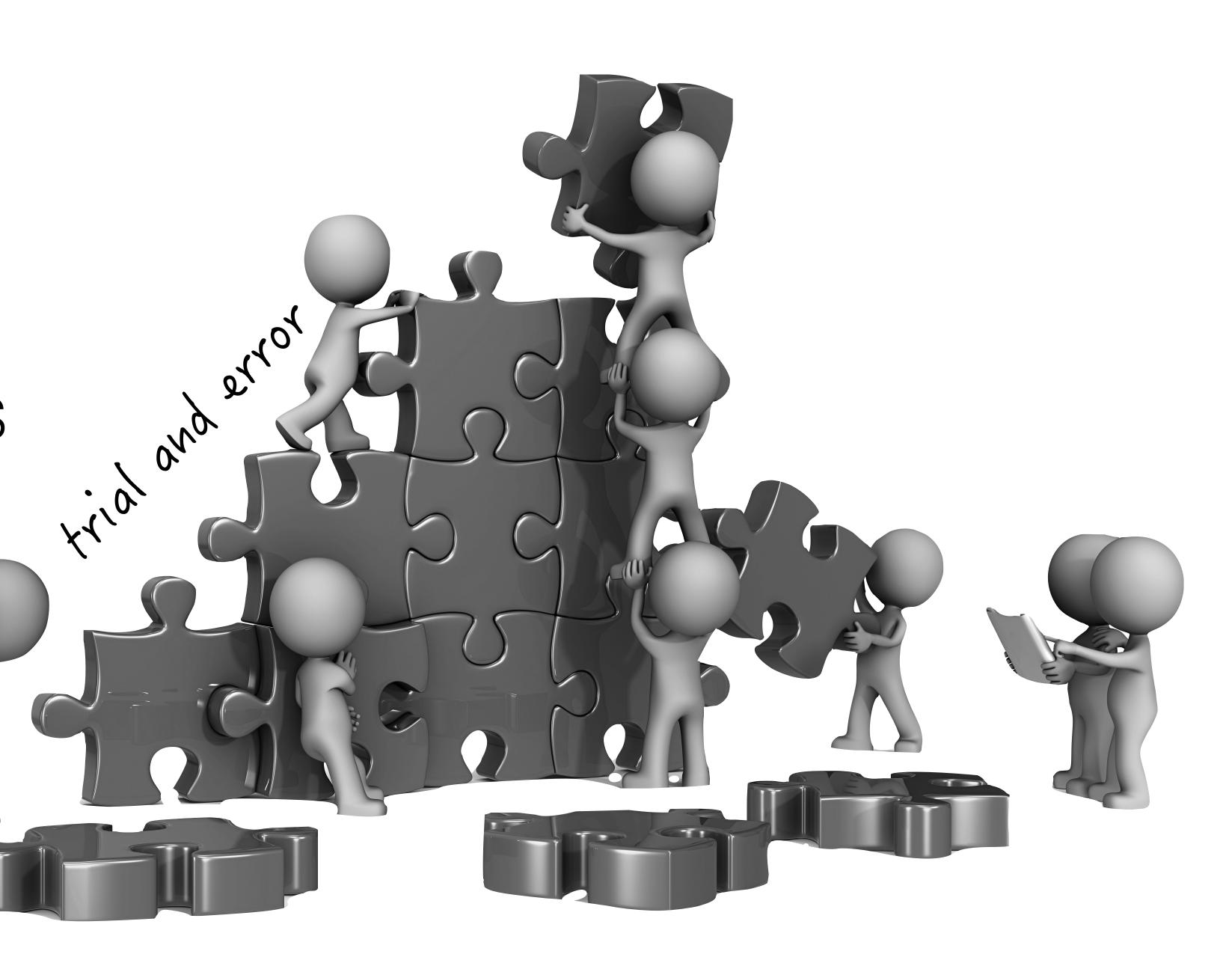
## **MAP LAYOUT FIRST**







2



## {arrays, logs, lsm-trees, b-trees}, filters, bitmaps, compression, stats

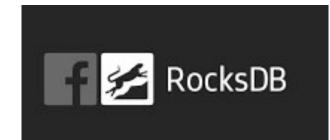
e.g., 1000x NoSQL k-v: bloom filter bits, merging policy e.g., access path selection: scans vs b-tree depends on concurrency e.g., robust scans with value by value lossy compression e.g., updatable bitmap indexes e.g., fast statistics/ML . . .





## EXAMPLE: The design space of **NoSQL Key-value Stores**

## Google **BigTable**













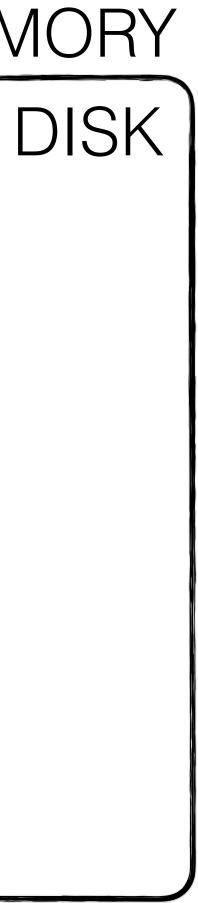


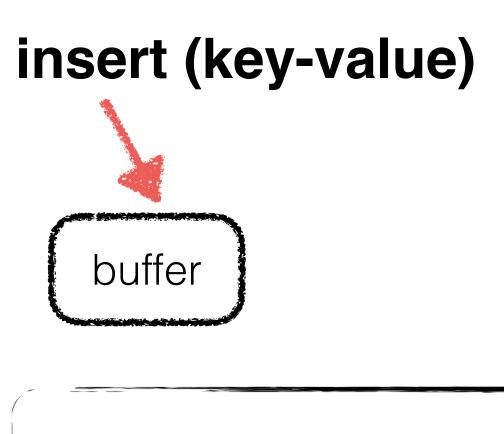




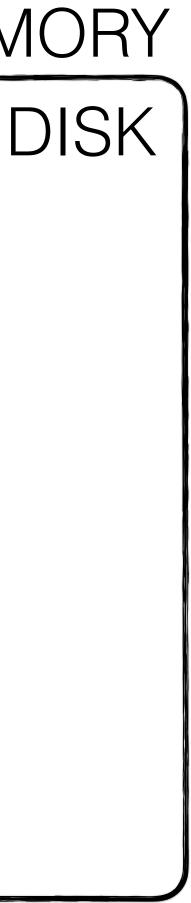
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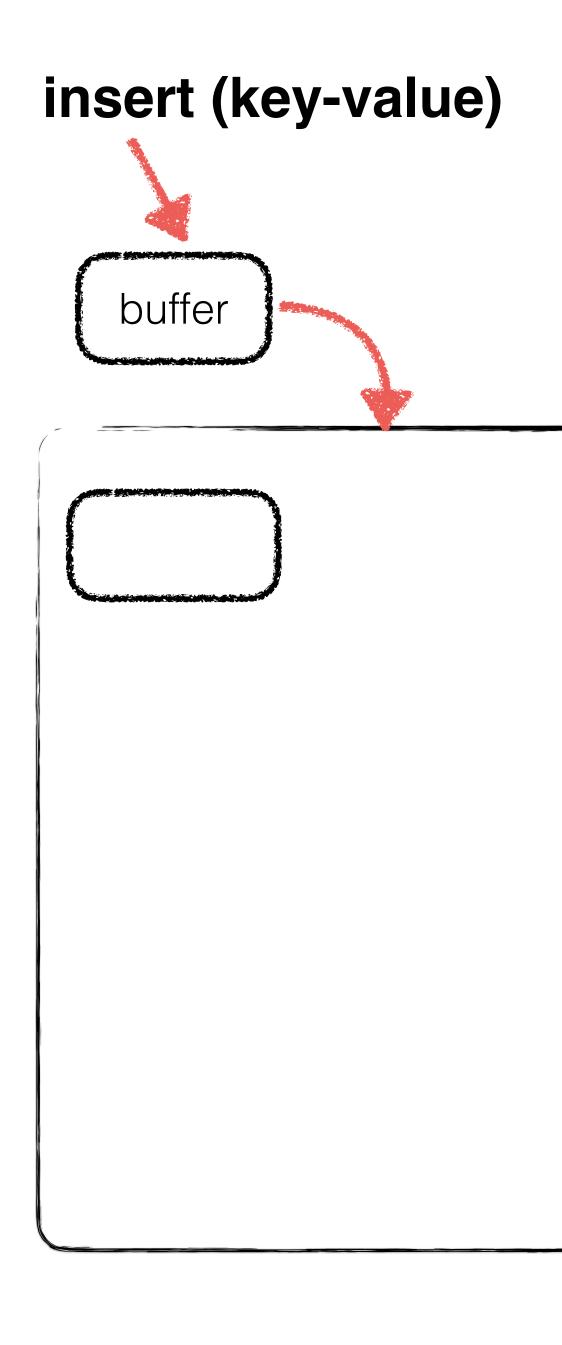




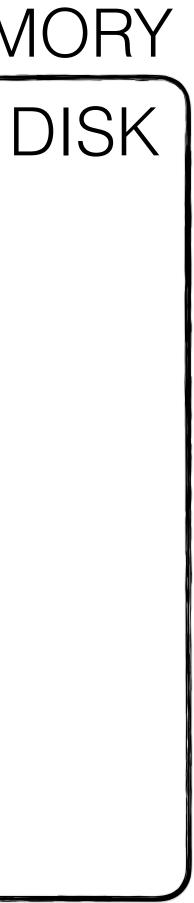


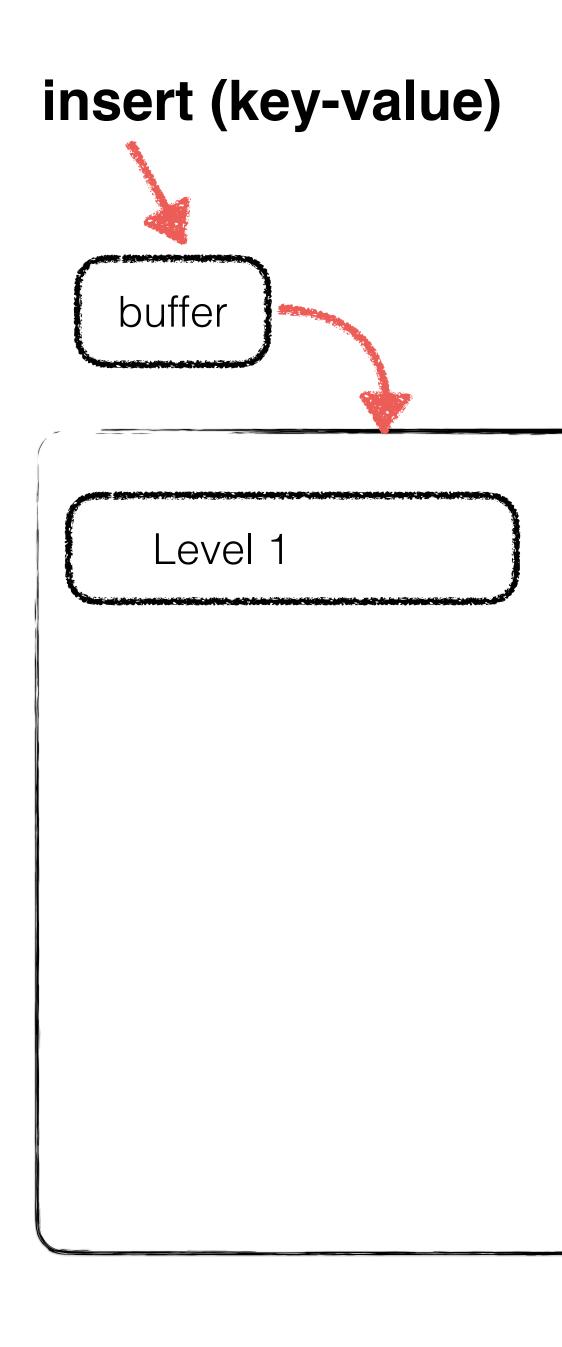




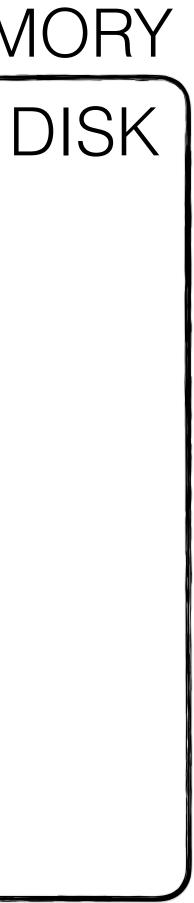






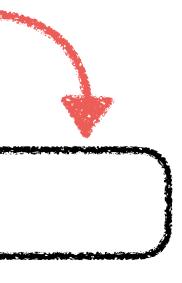


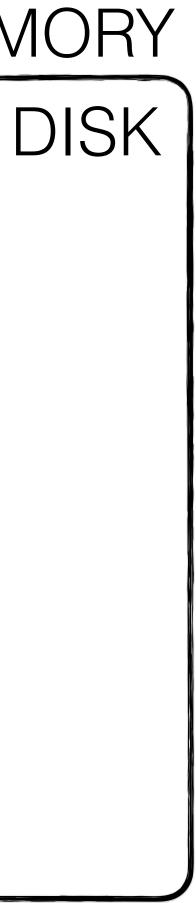




in	sert (key-valu	<b>e)</b>
	buffer	
	Level 1	
	Level 2	

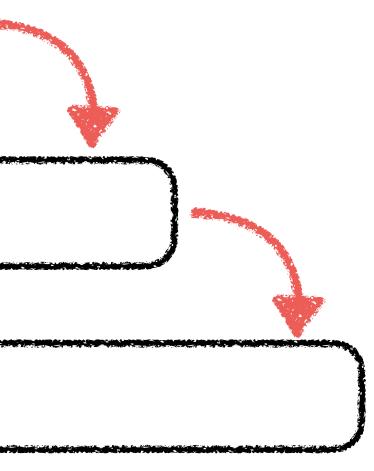


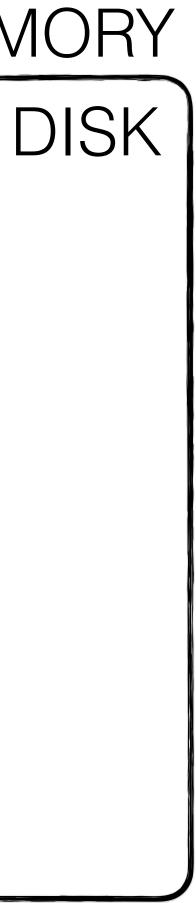




in	sert (key-value)	
	buffer	
	Level 1	
	Level 2	
	Level 3	

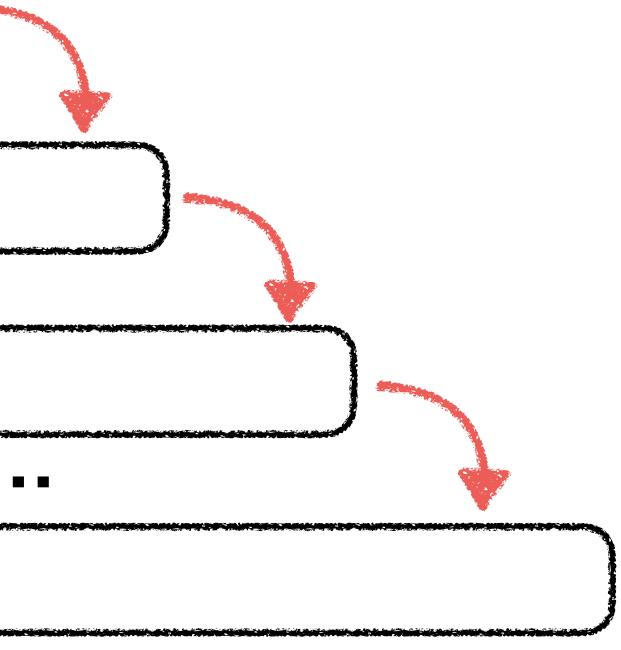


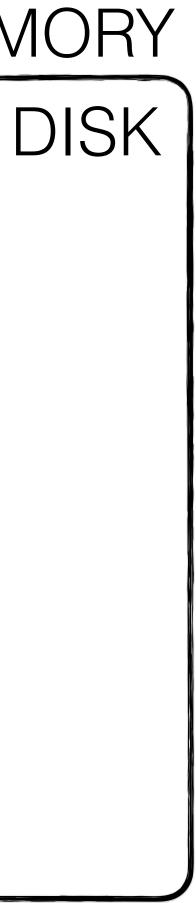




insert (key-value)			
	buffer		
	Level 1		
	Level 2		
	Level 3		
	Level N		

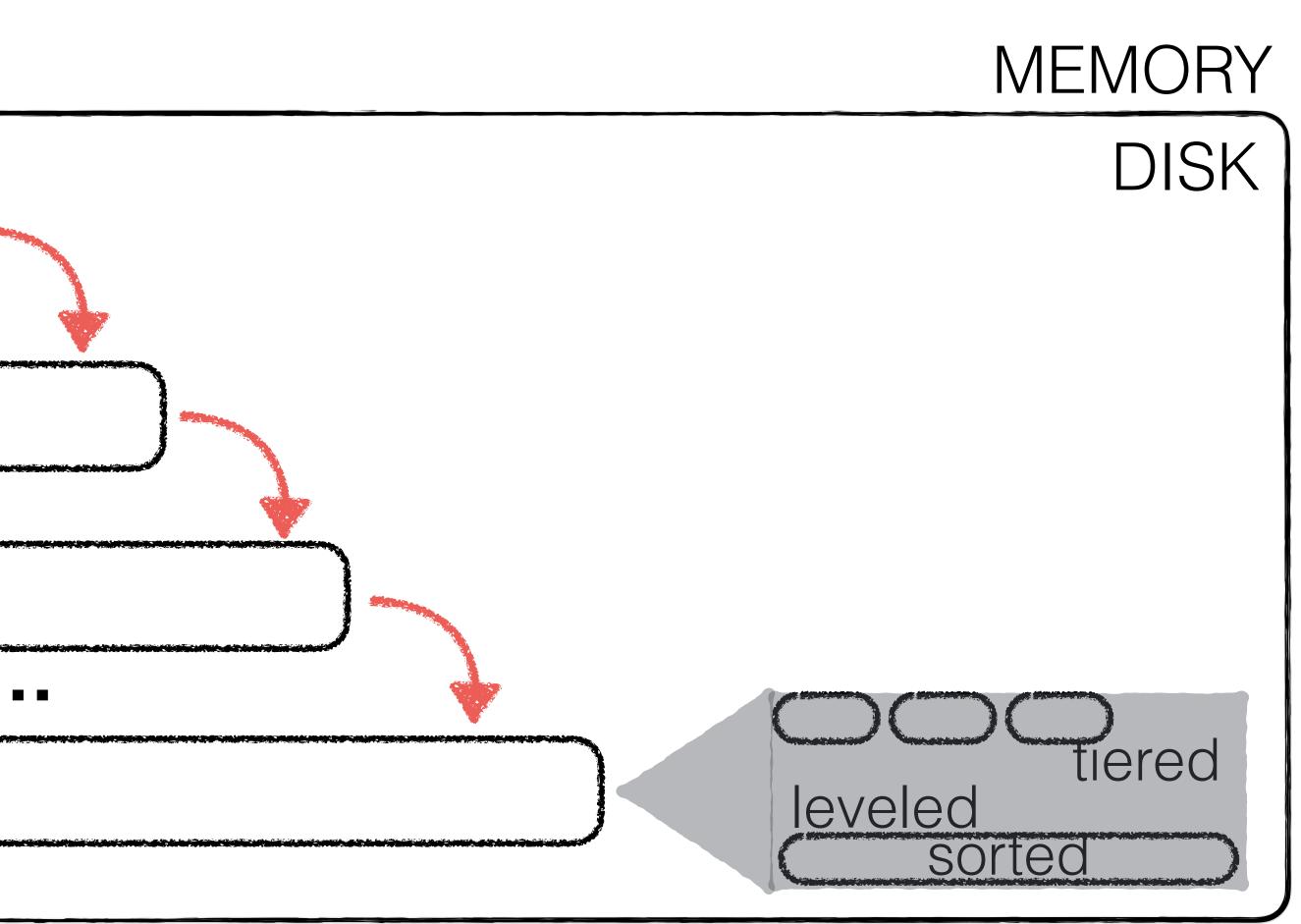






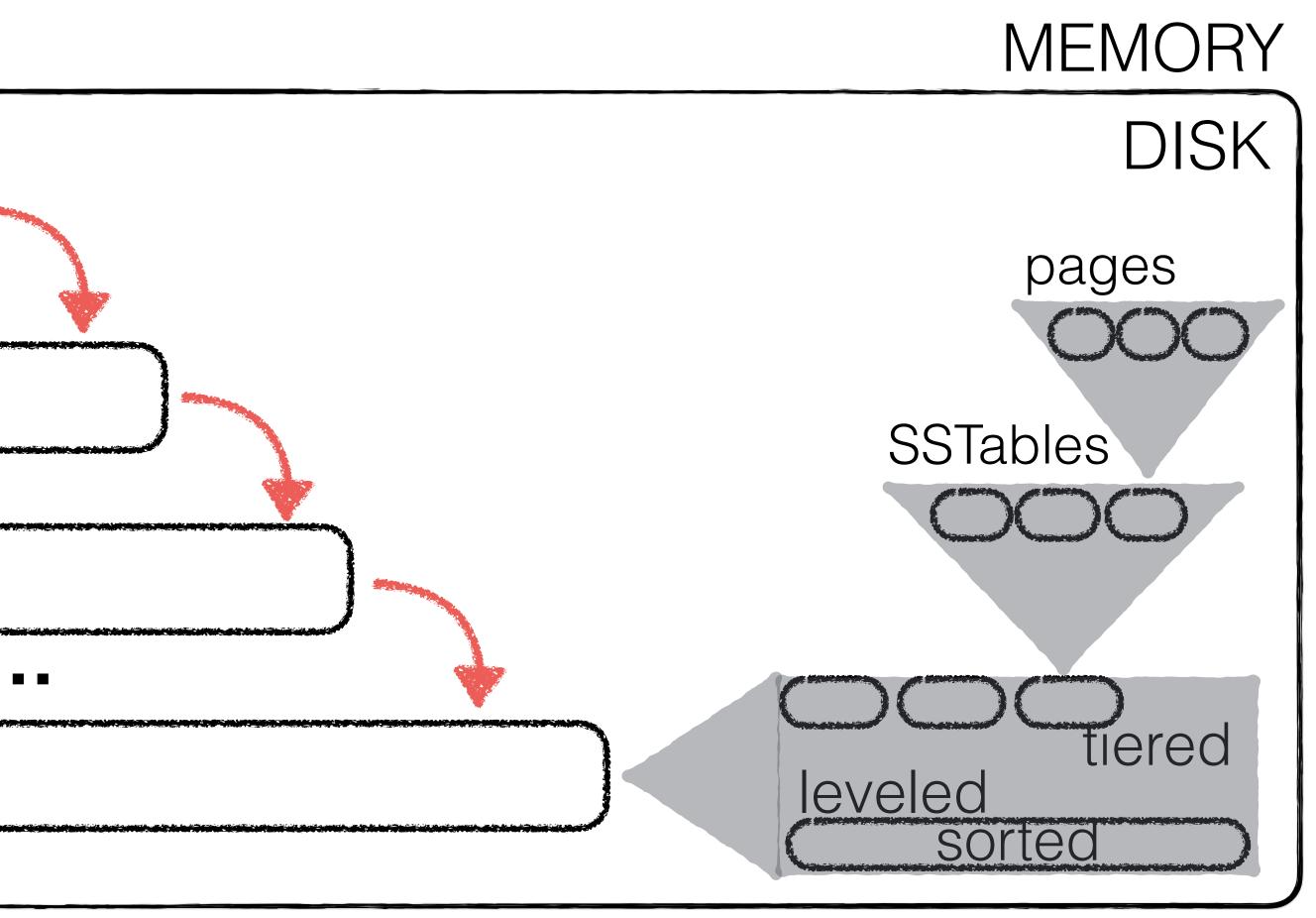
insert (key-value)			
	buffer		
	Level 1		
	Level 2		
	Level 3		
	Level N		





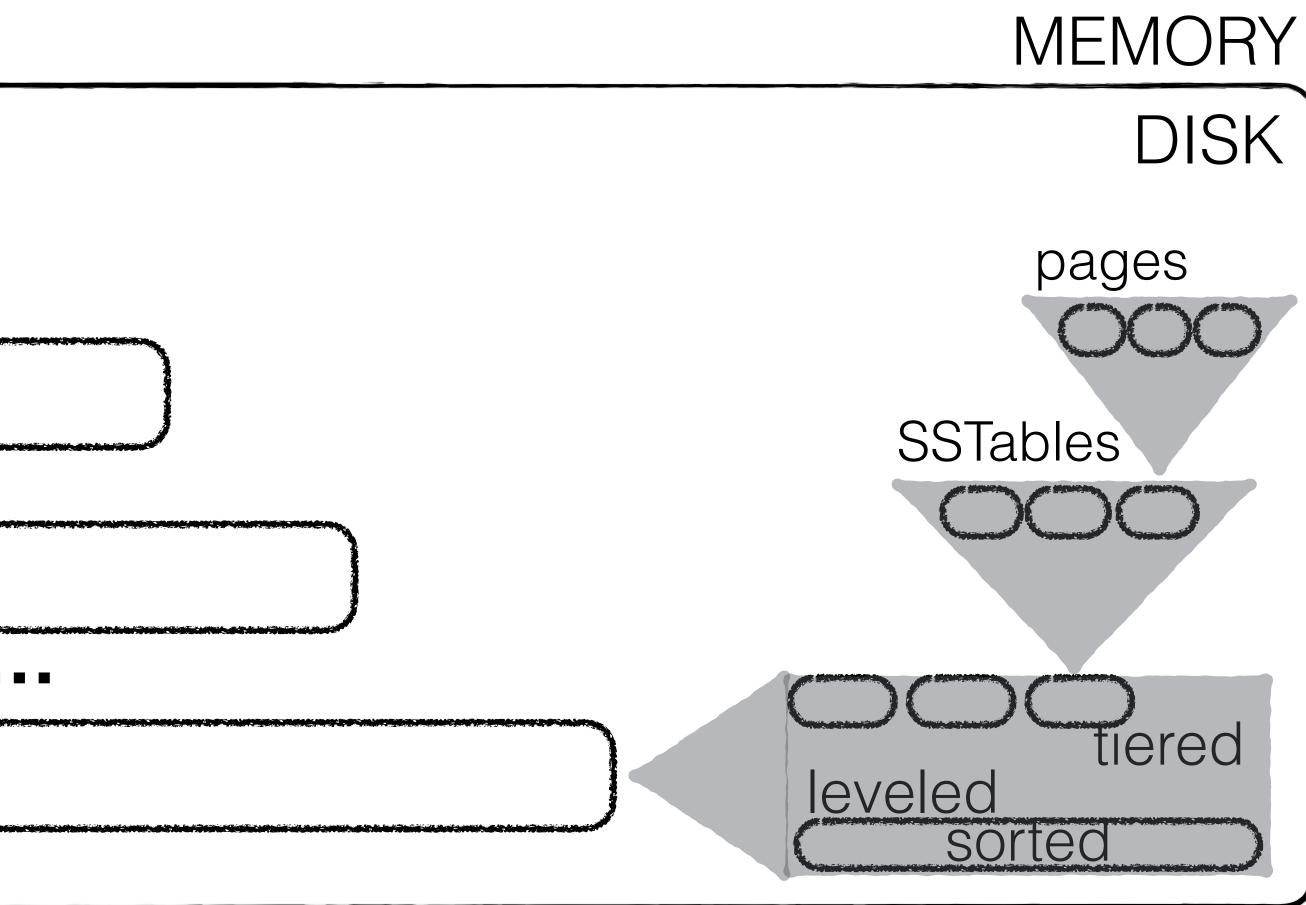
insert (key-value)			
	buffer		
	Level 1		
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	Level 3		
	Level N		

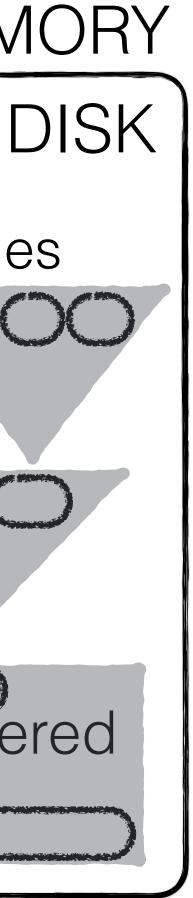


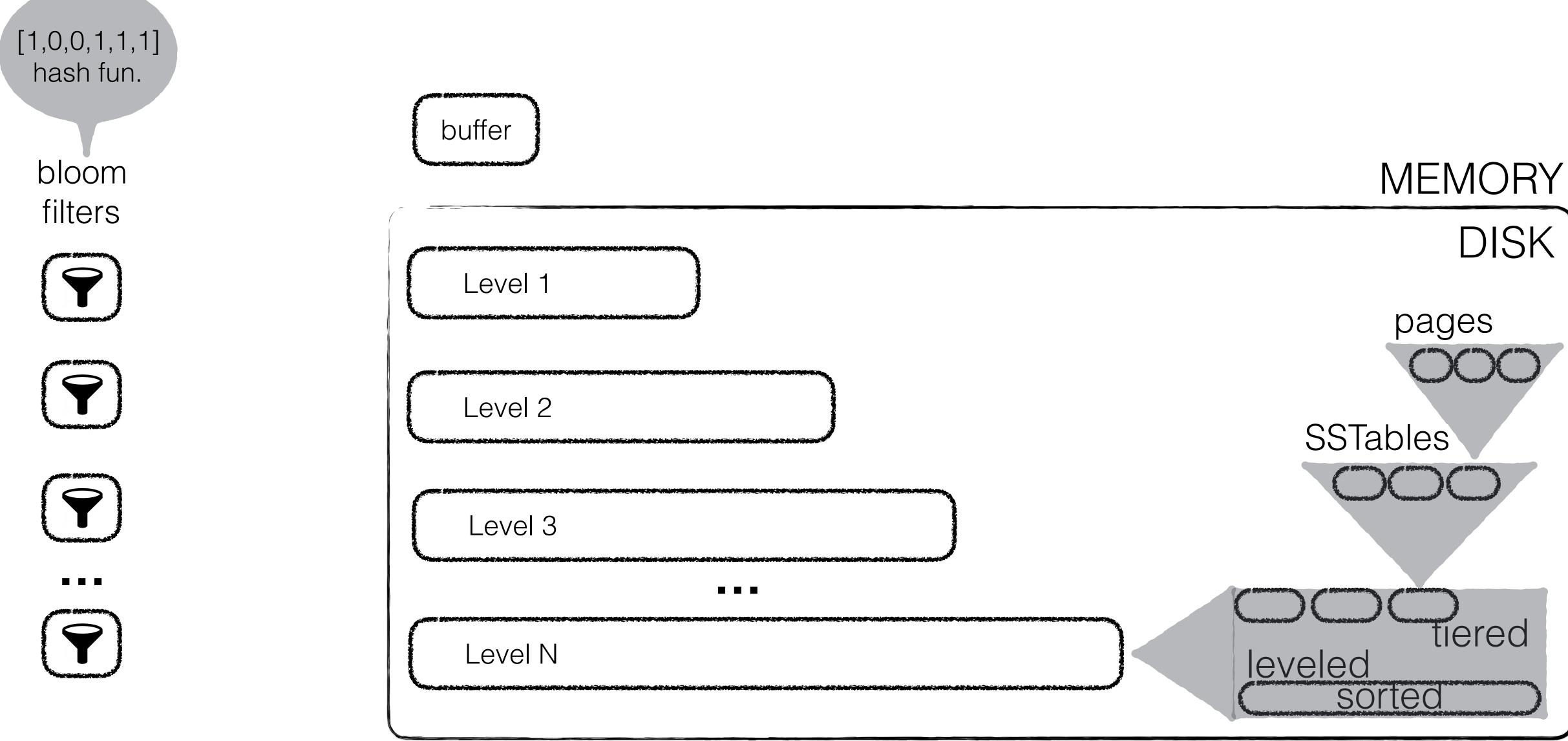


buffer	
Level 1	
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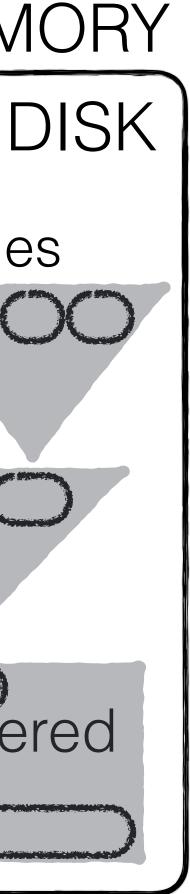


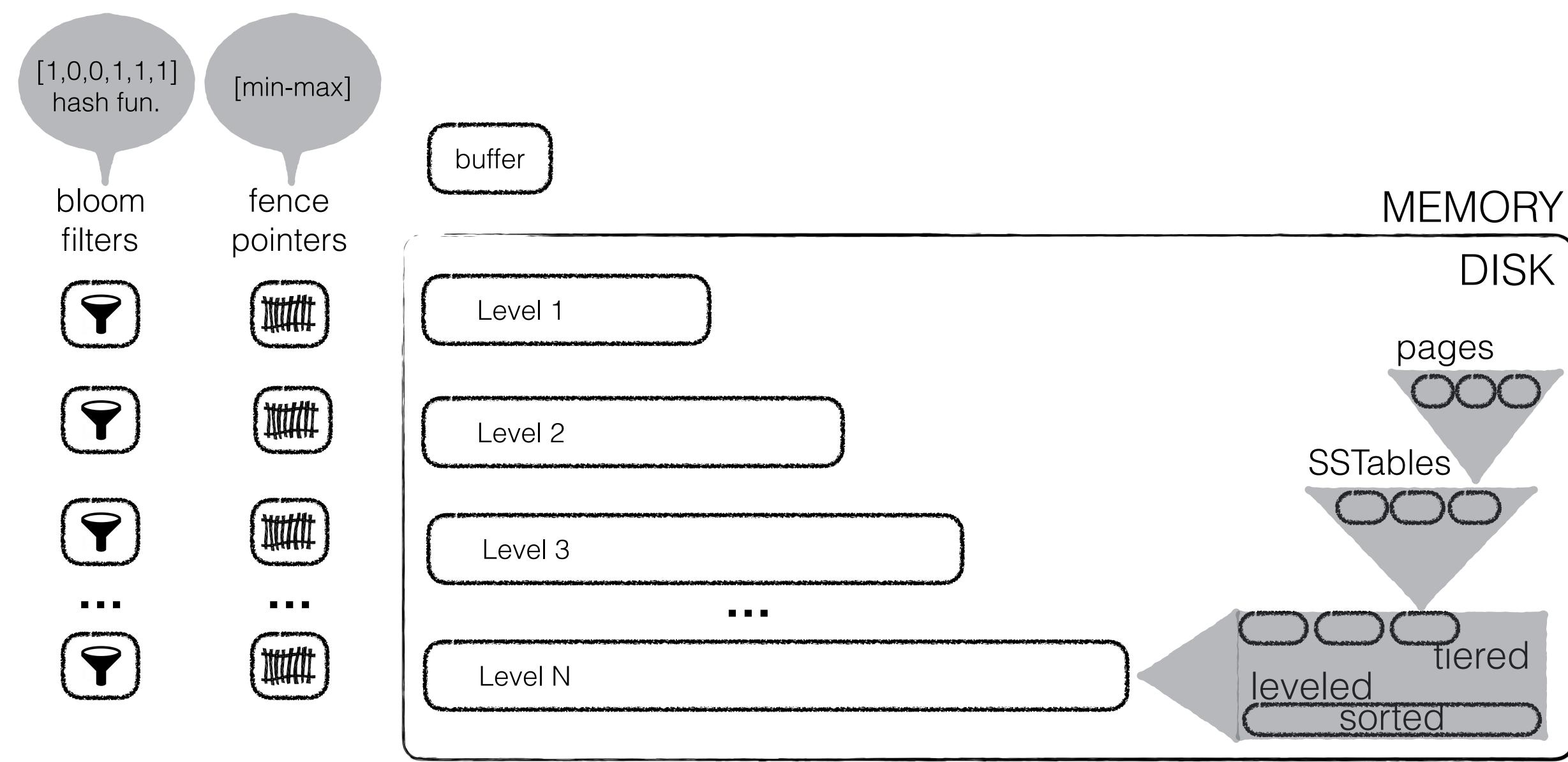




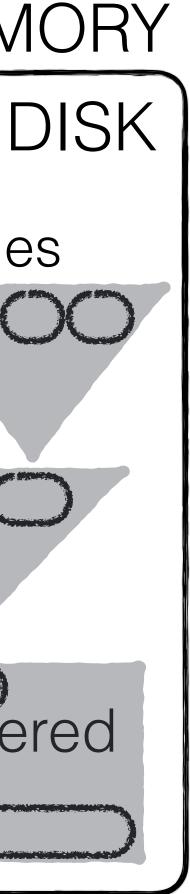


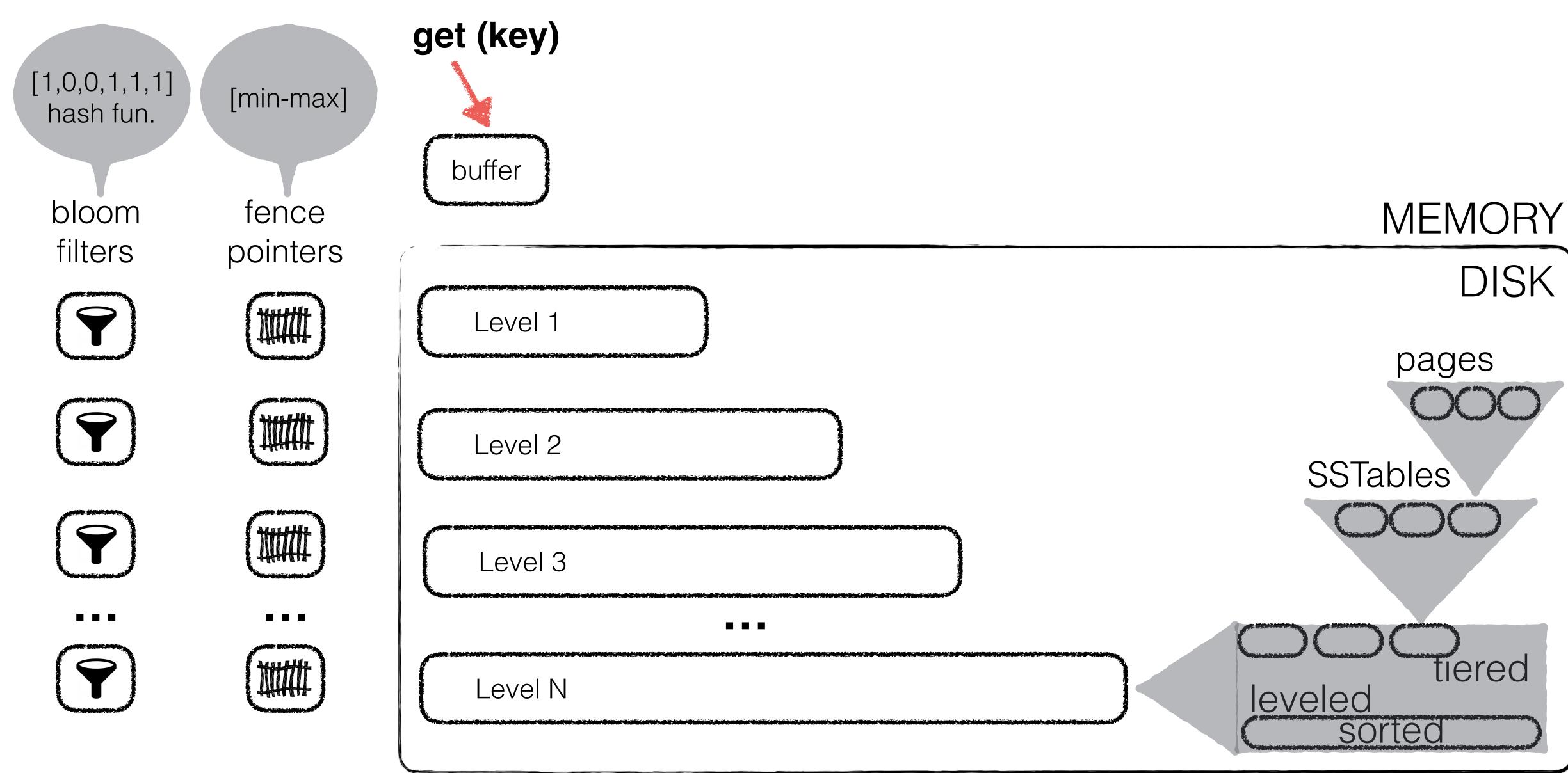




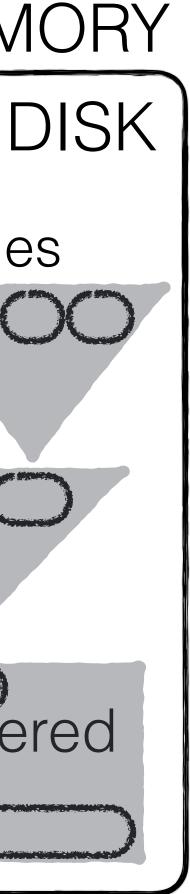


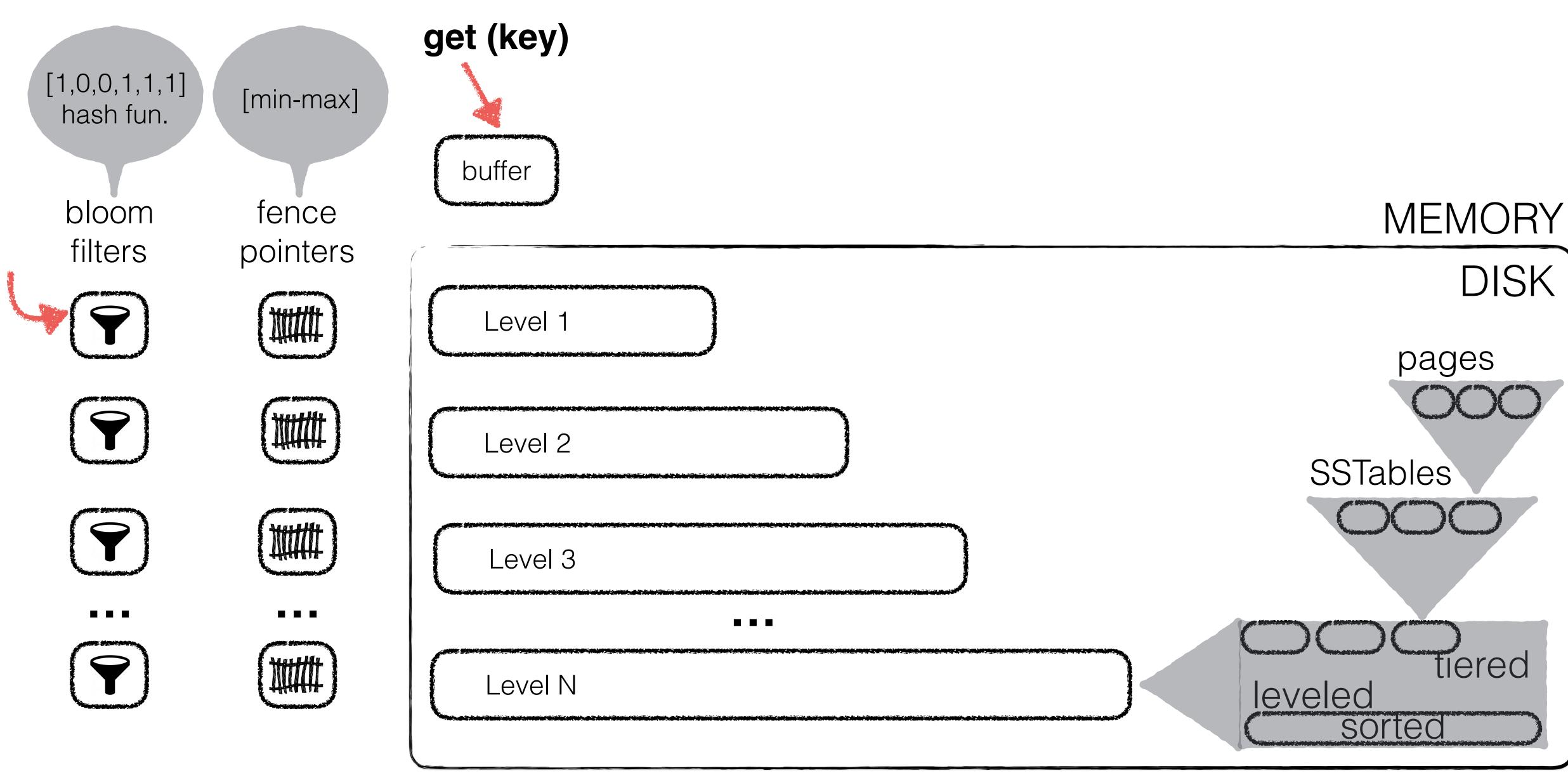




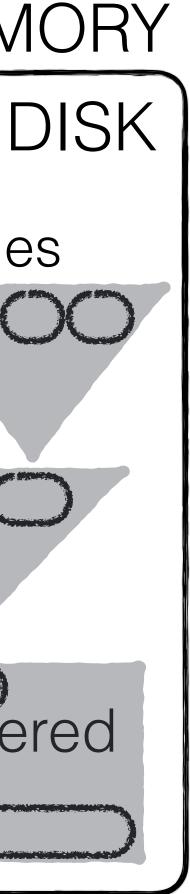


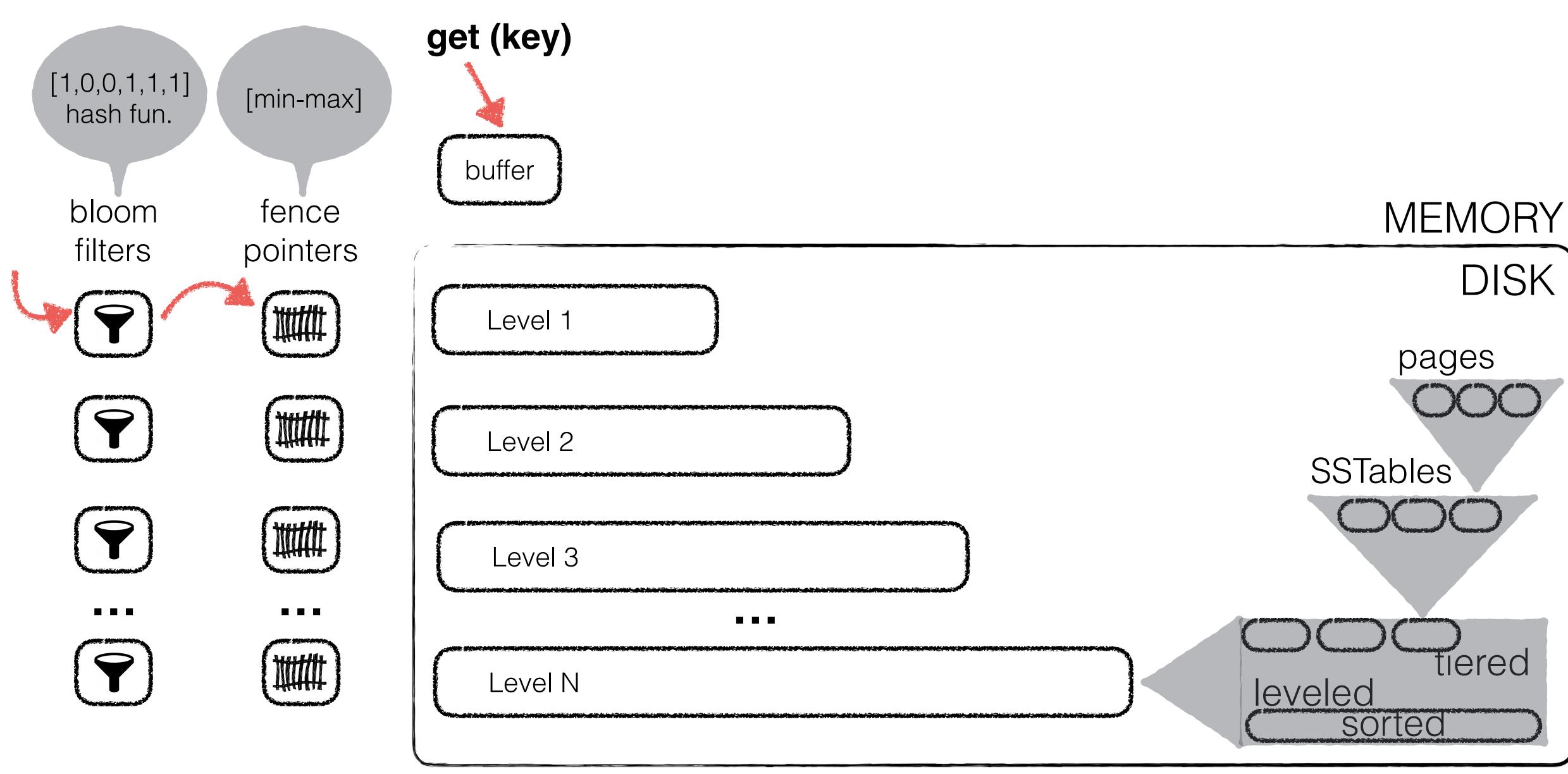




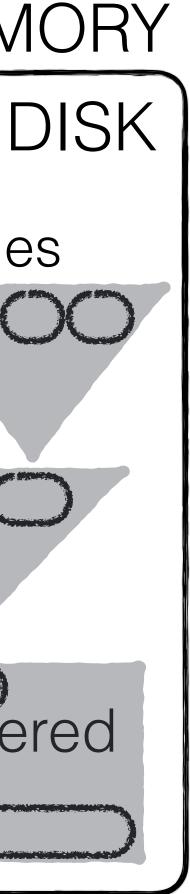


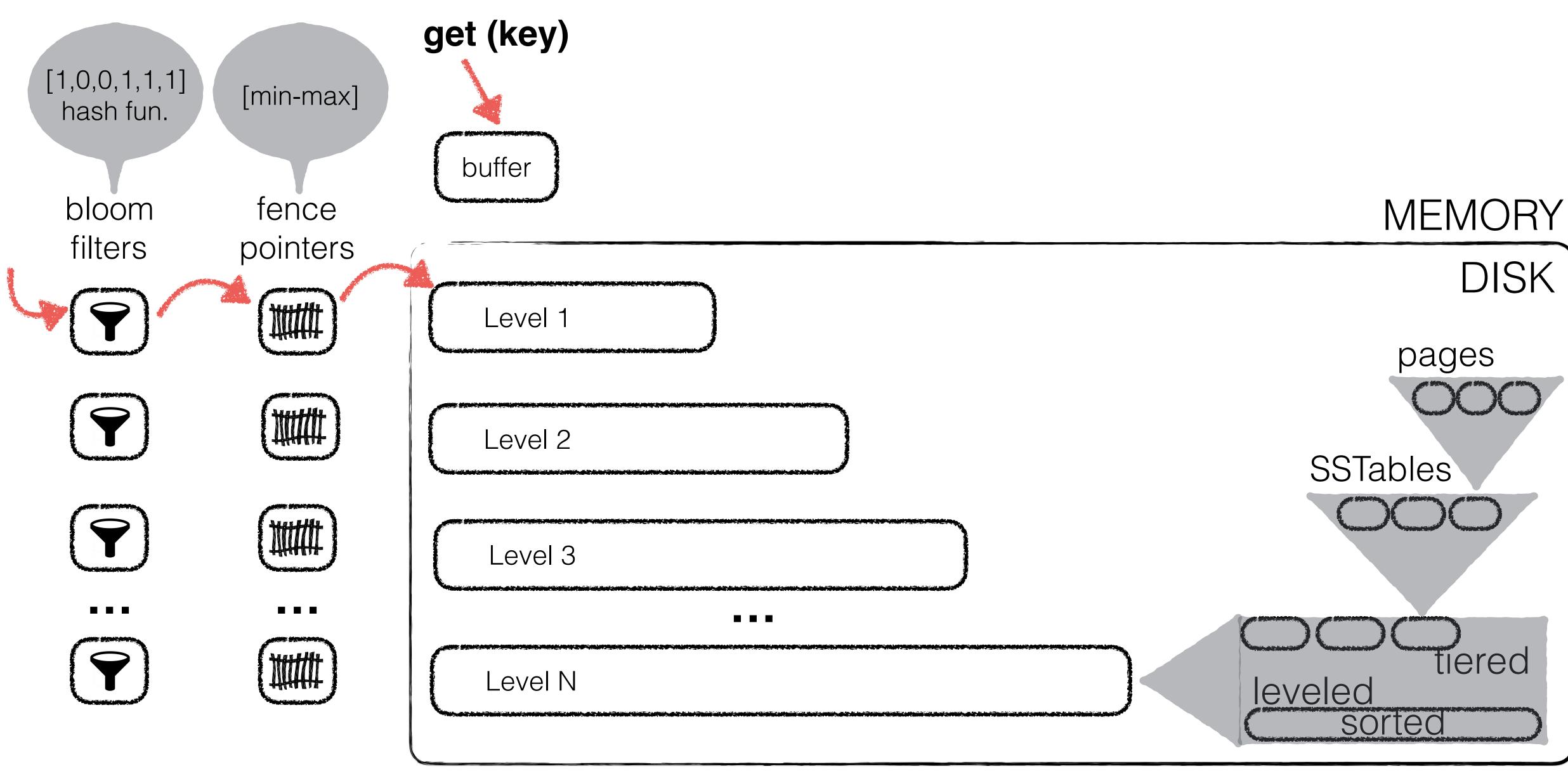




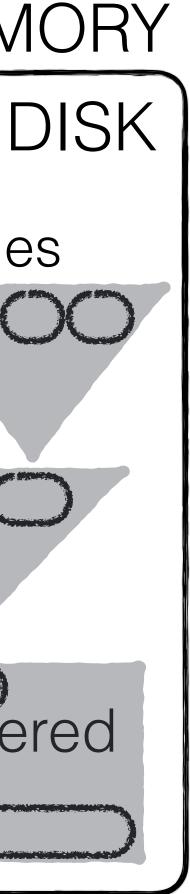


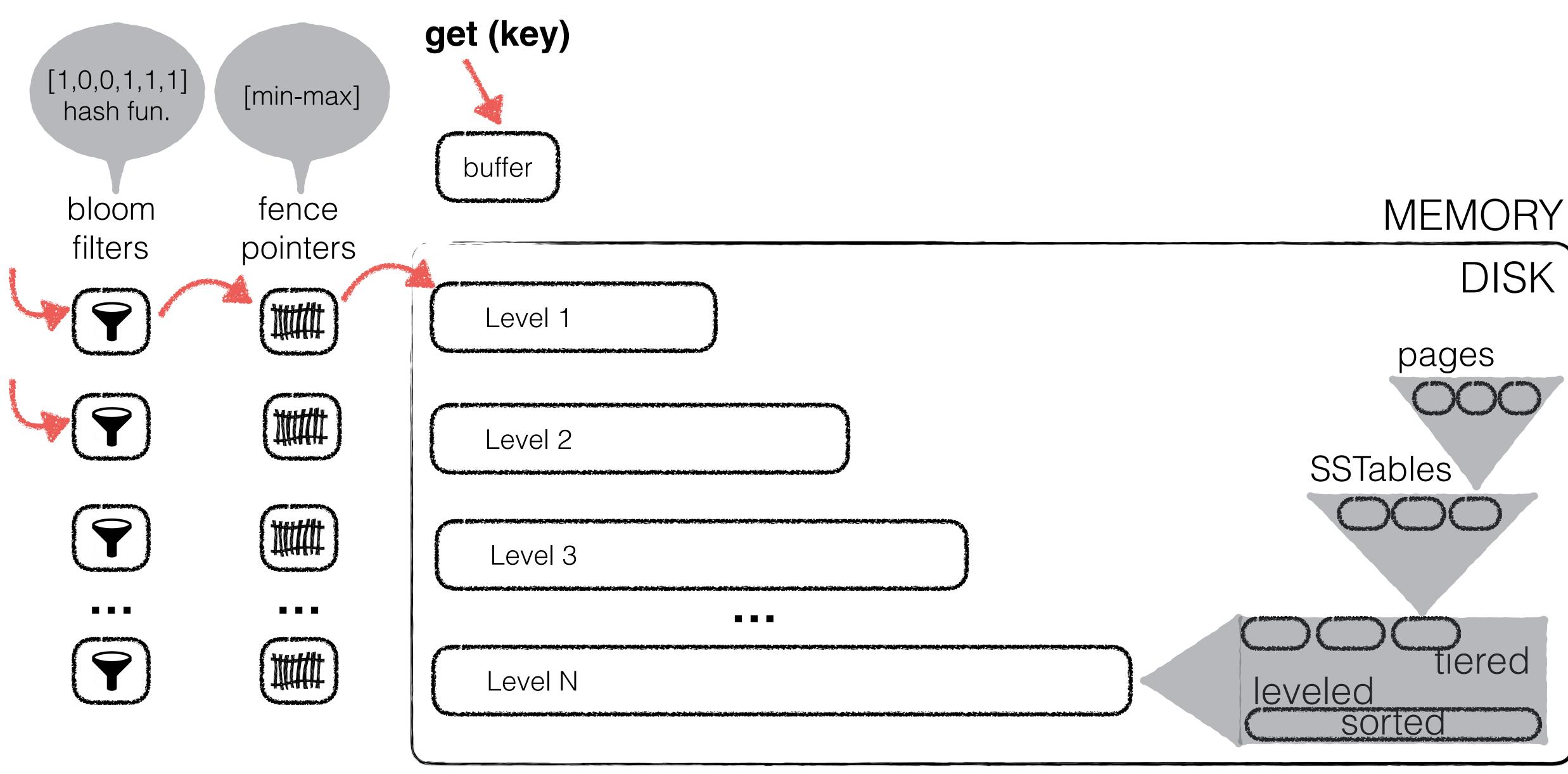




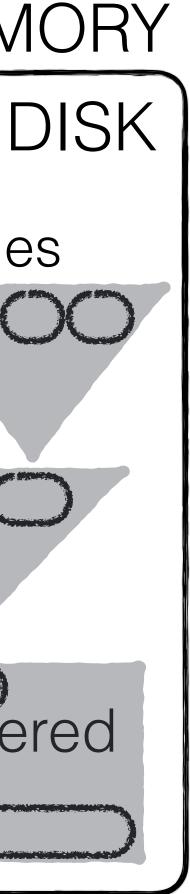


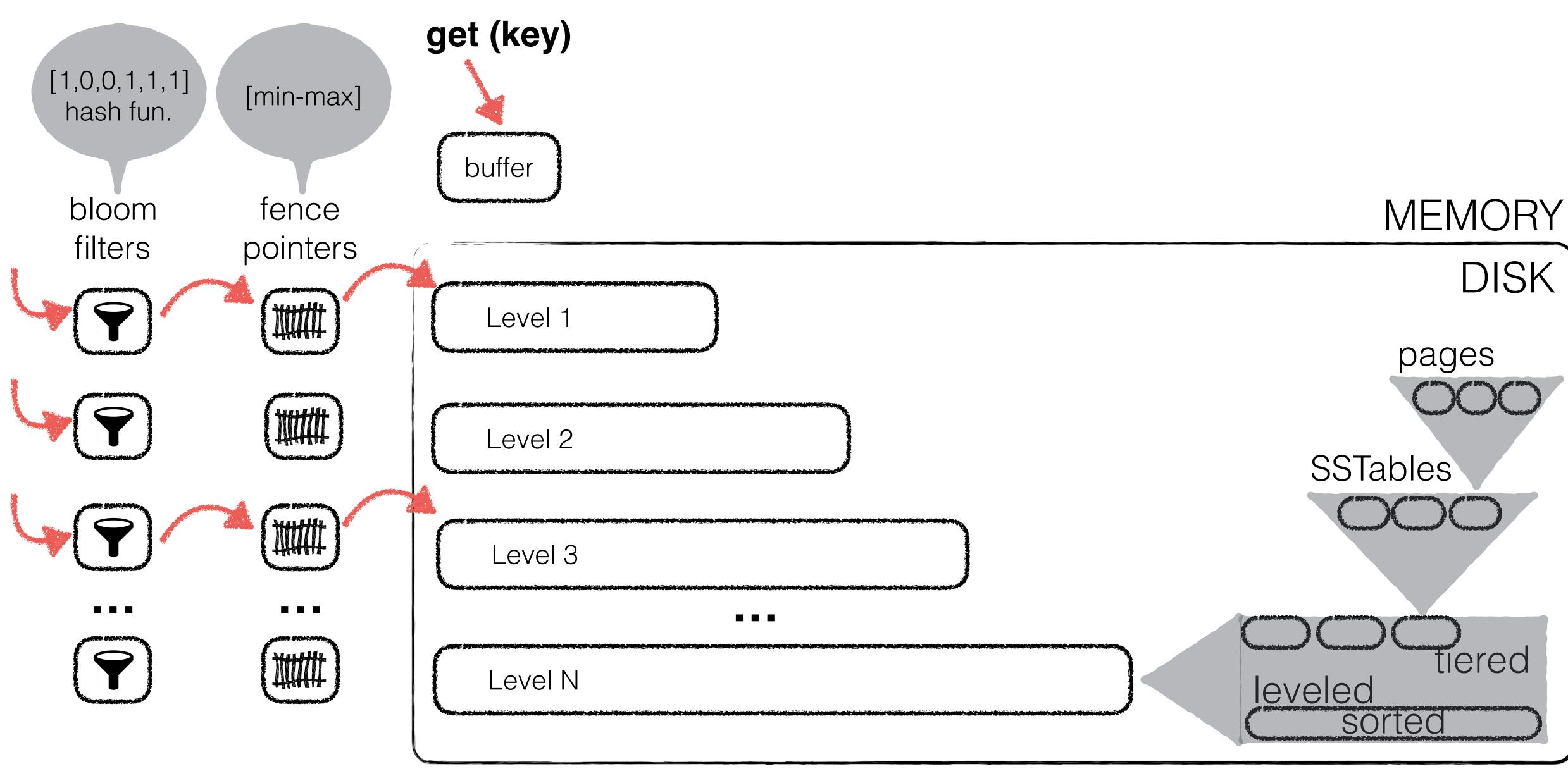




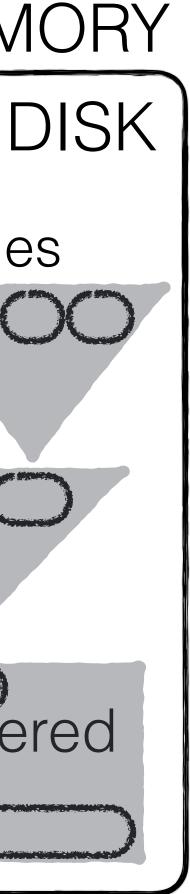


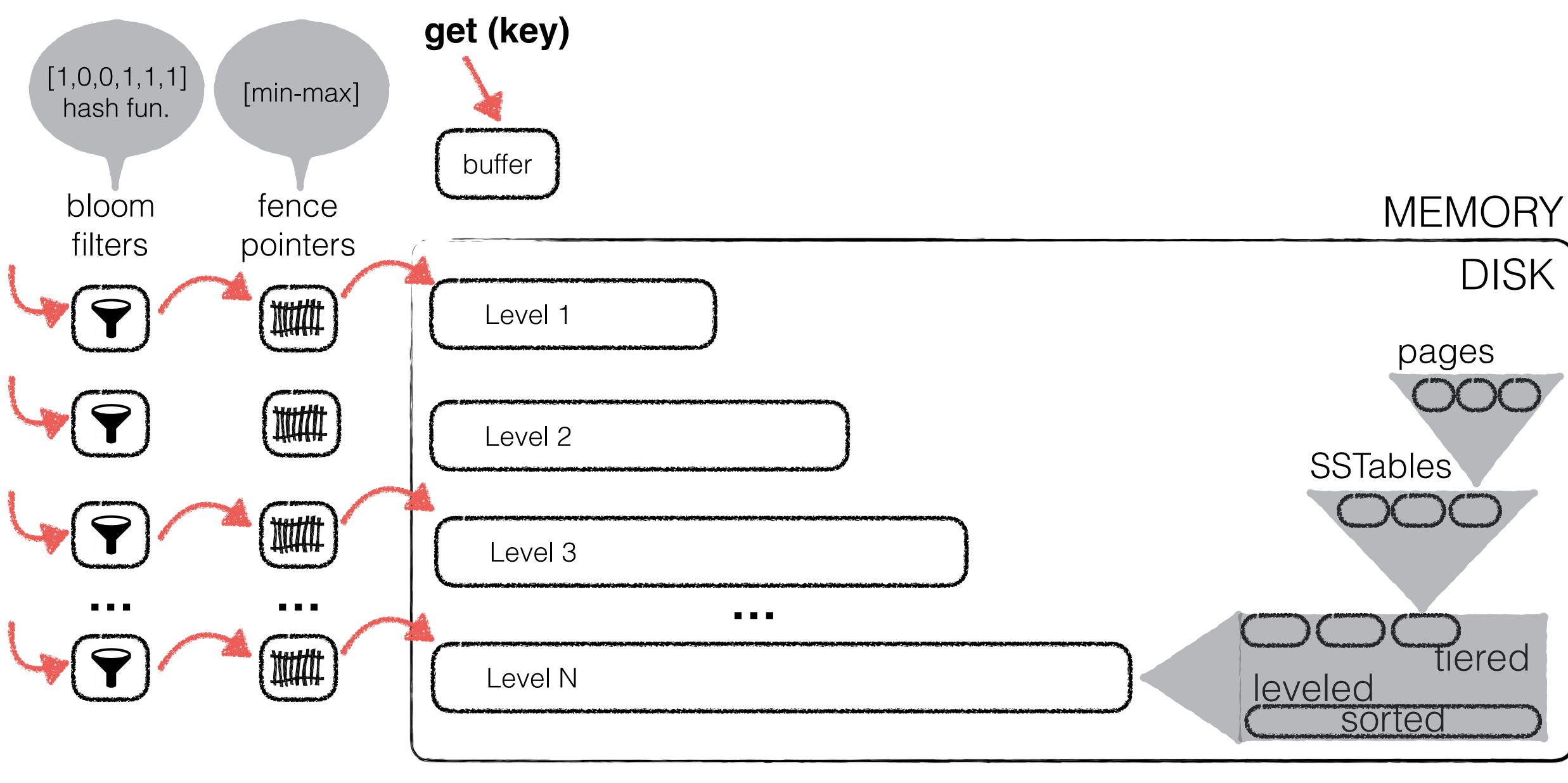




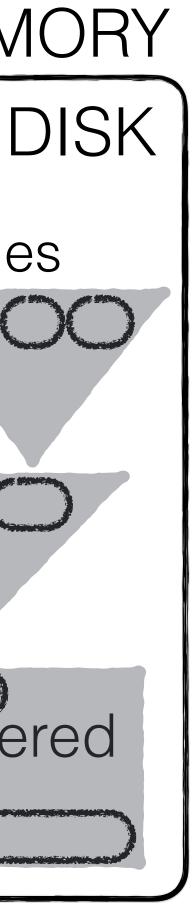




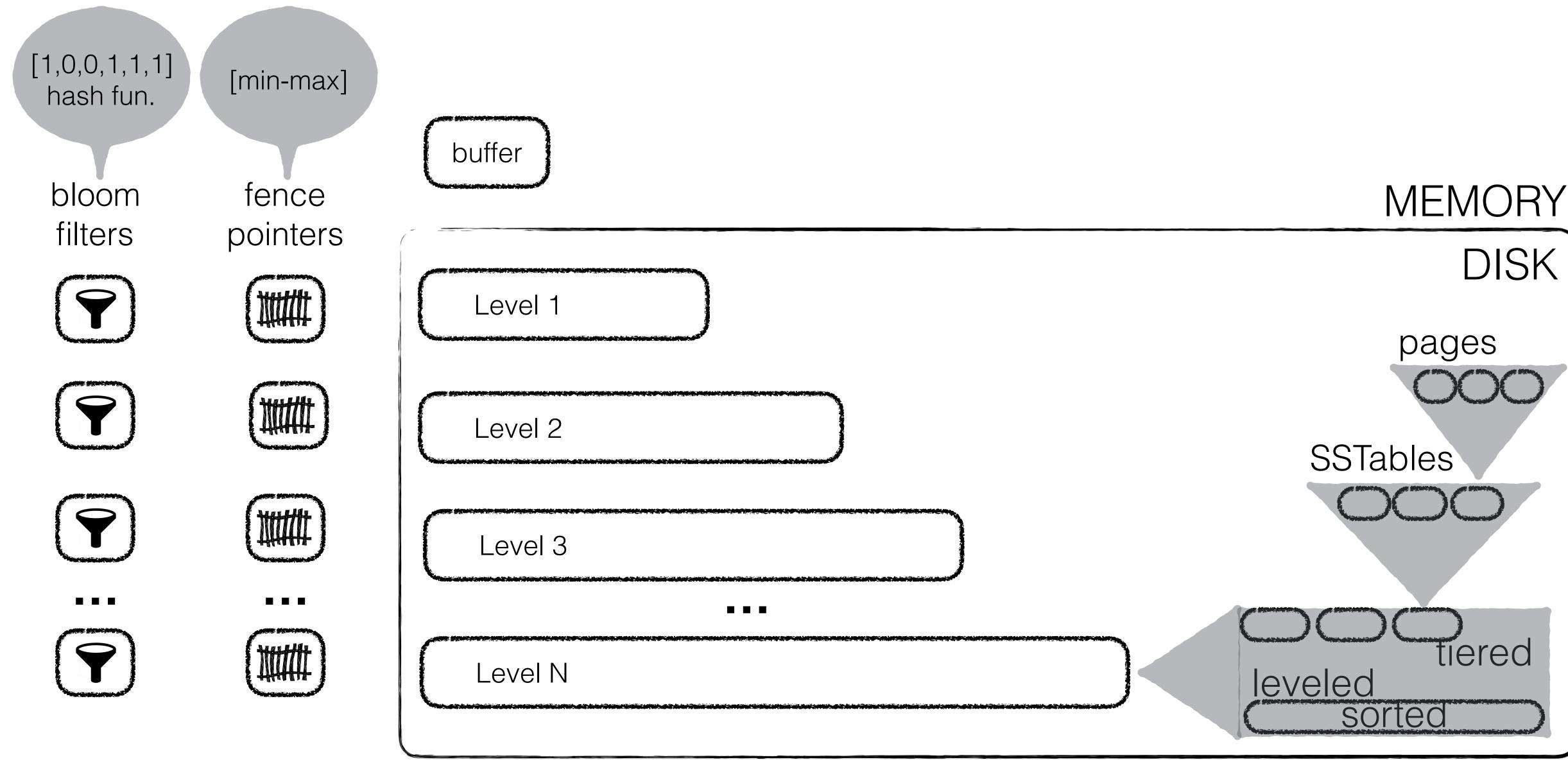




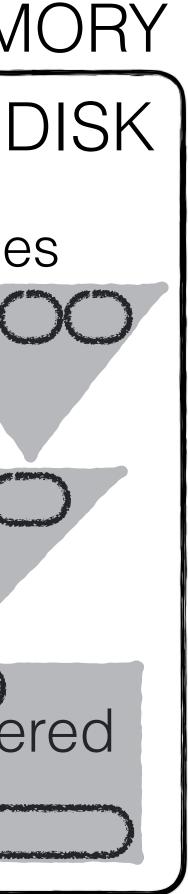




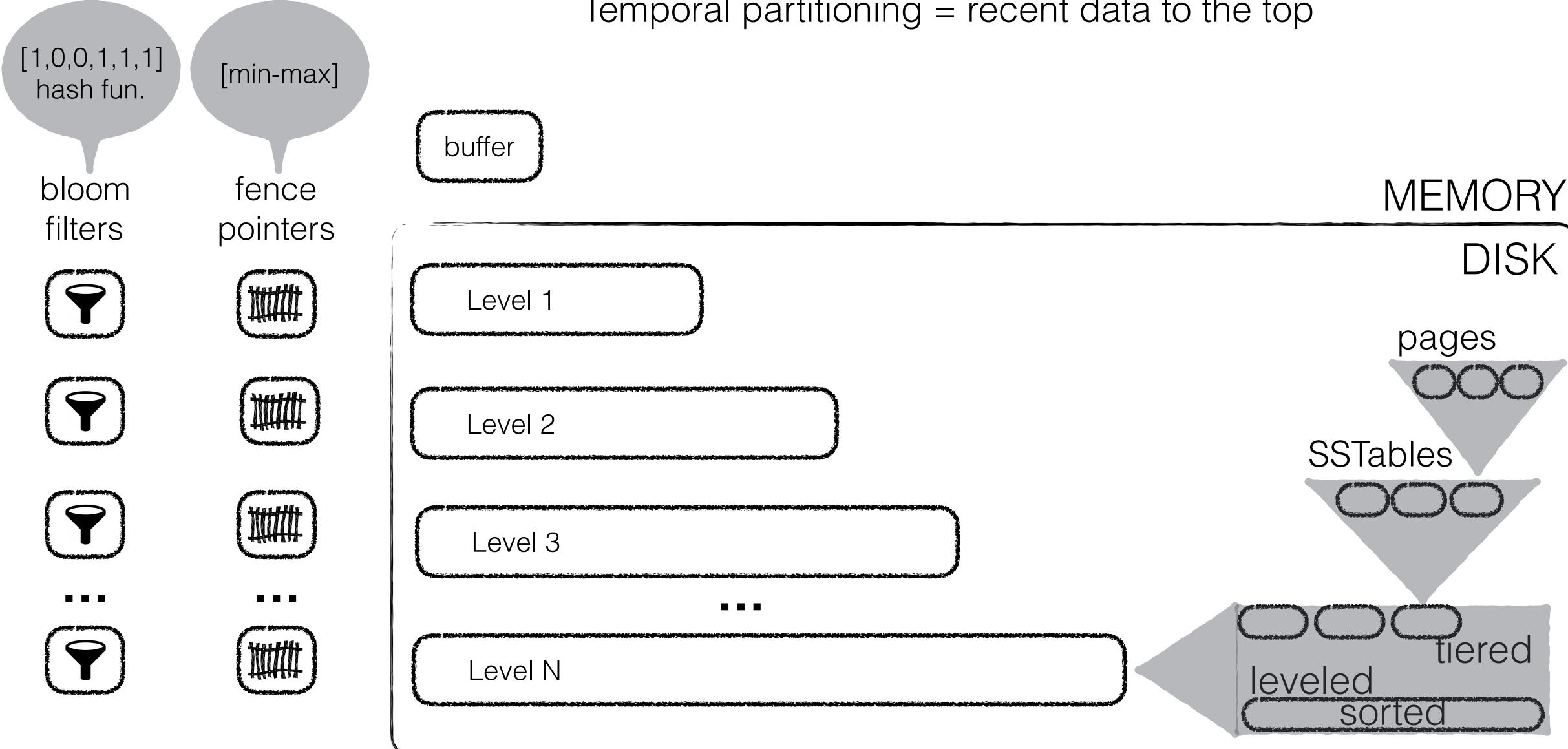
#### Instant writes, but overtime have to be merged >1





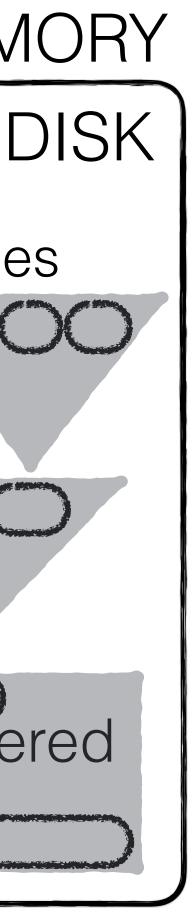


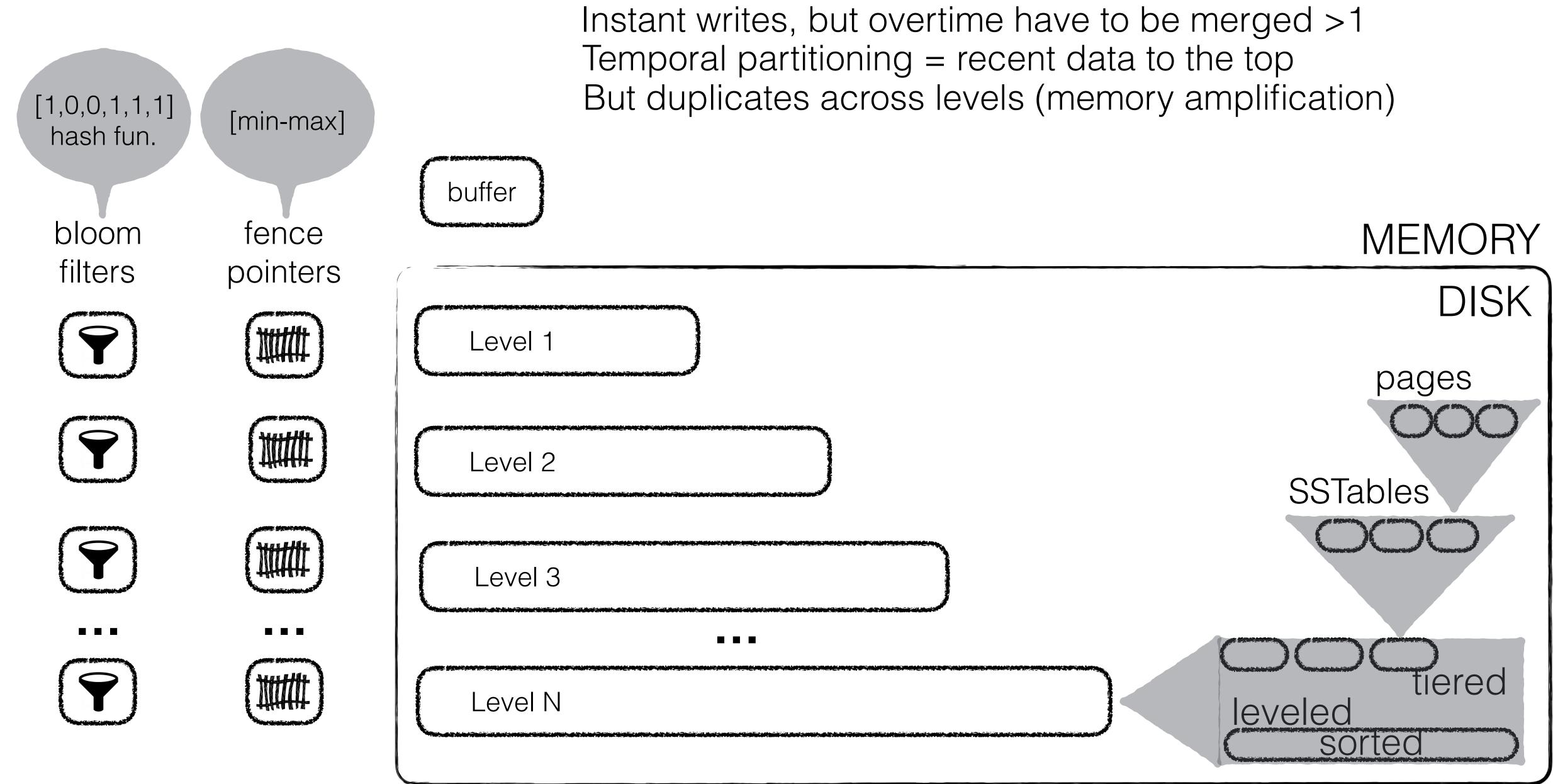




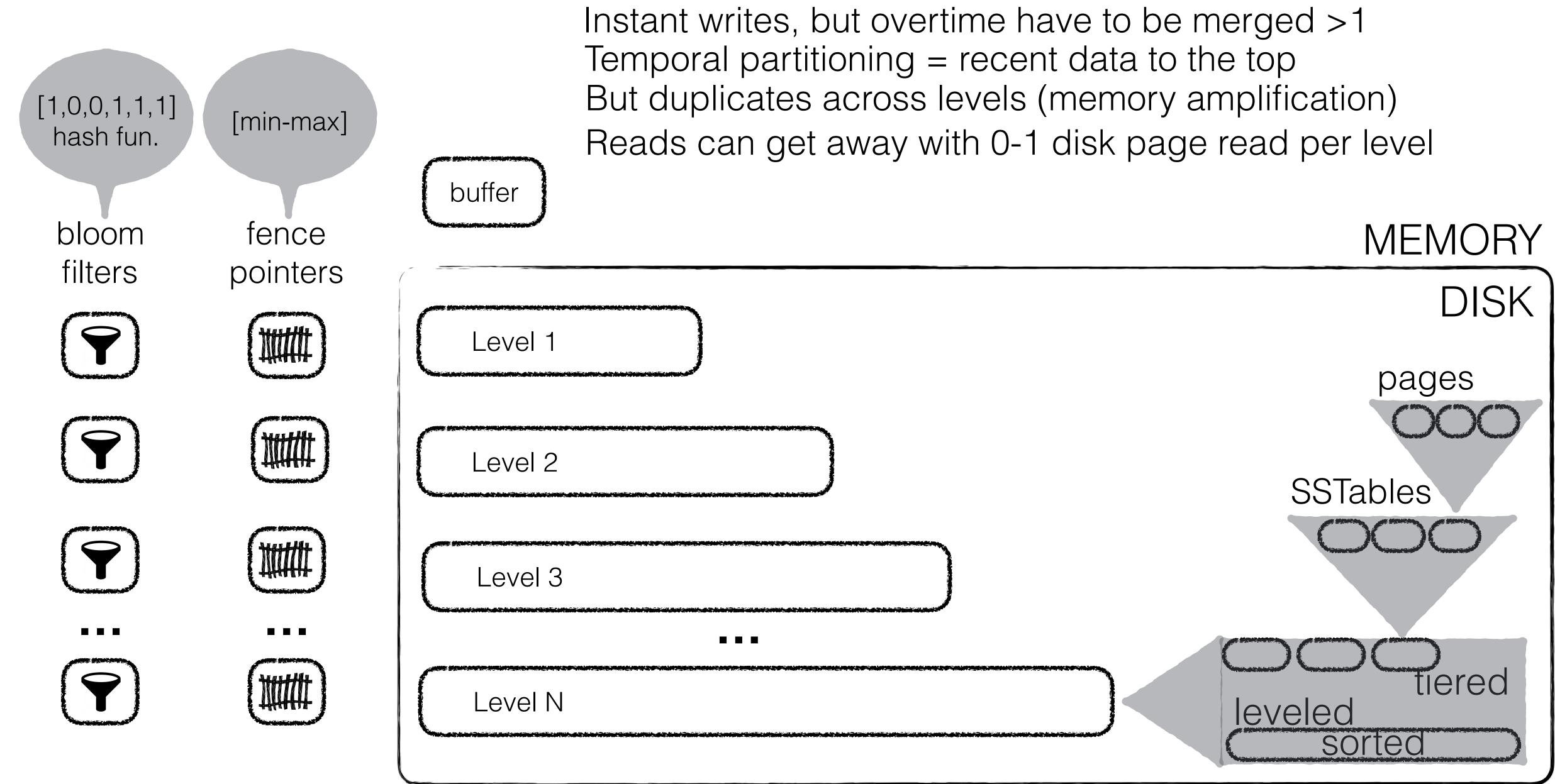


#### Instant writes, but overtime have to be merged >1 Temporal partitioning = recent data to the top

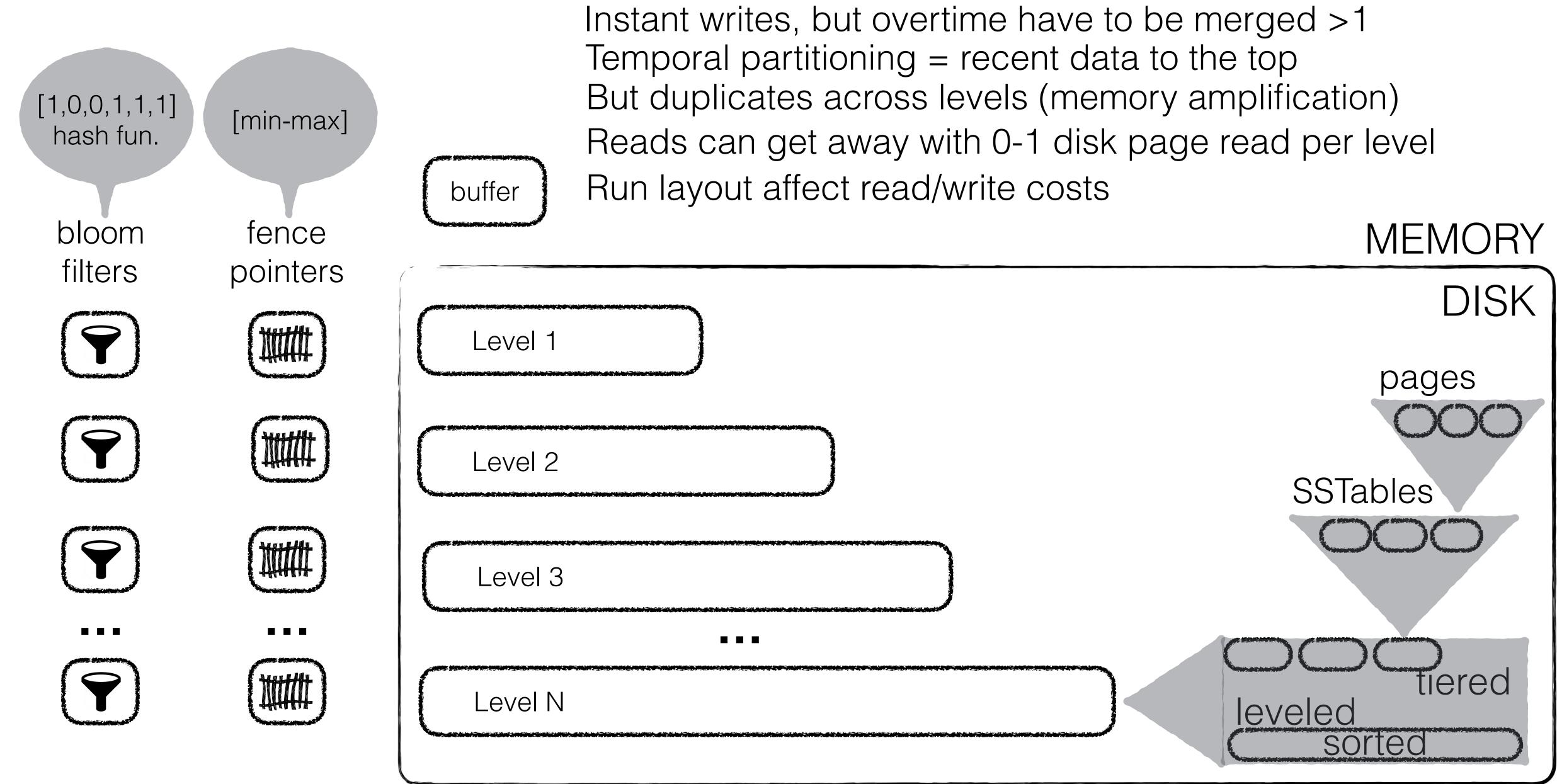




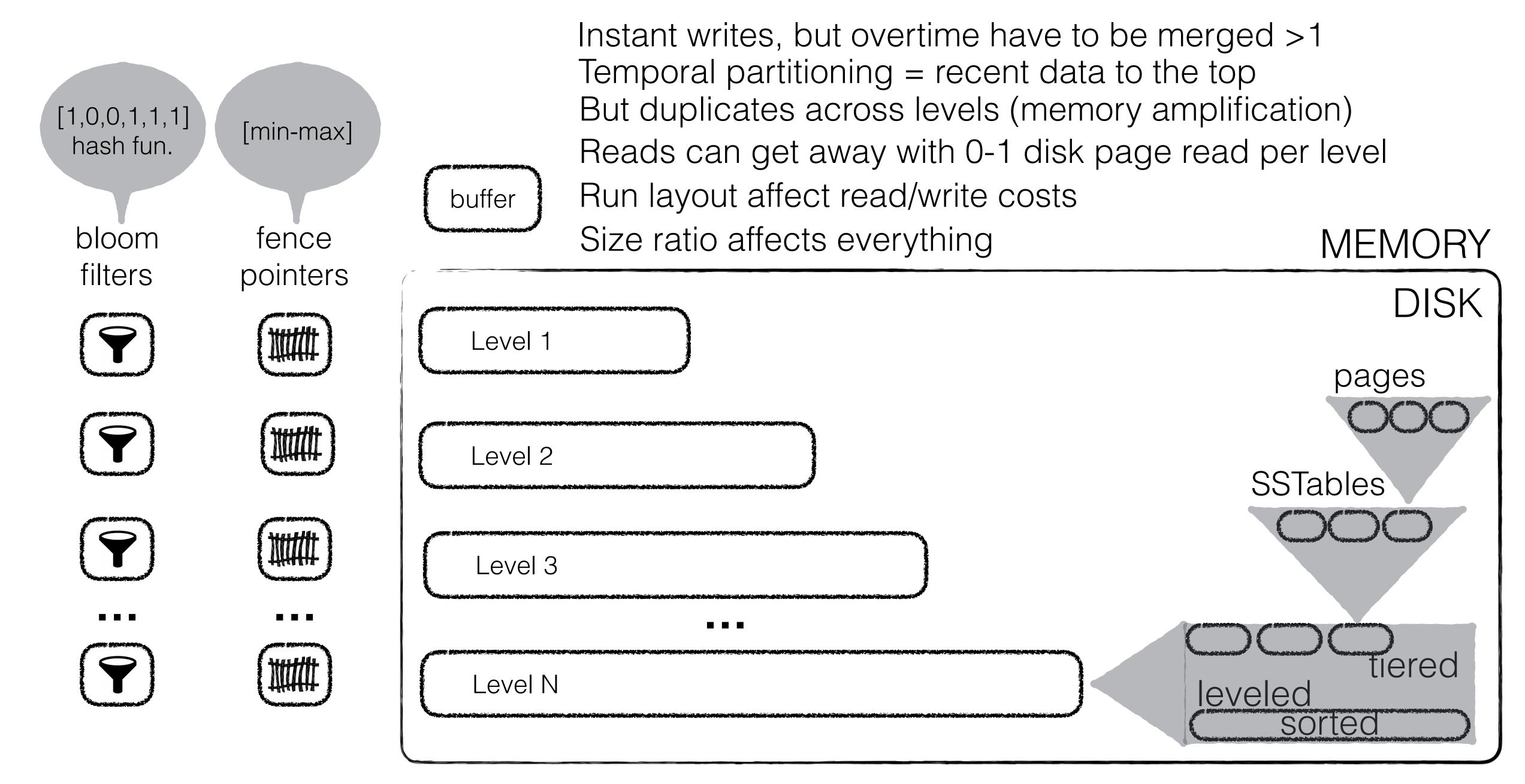




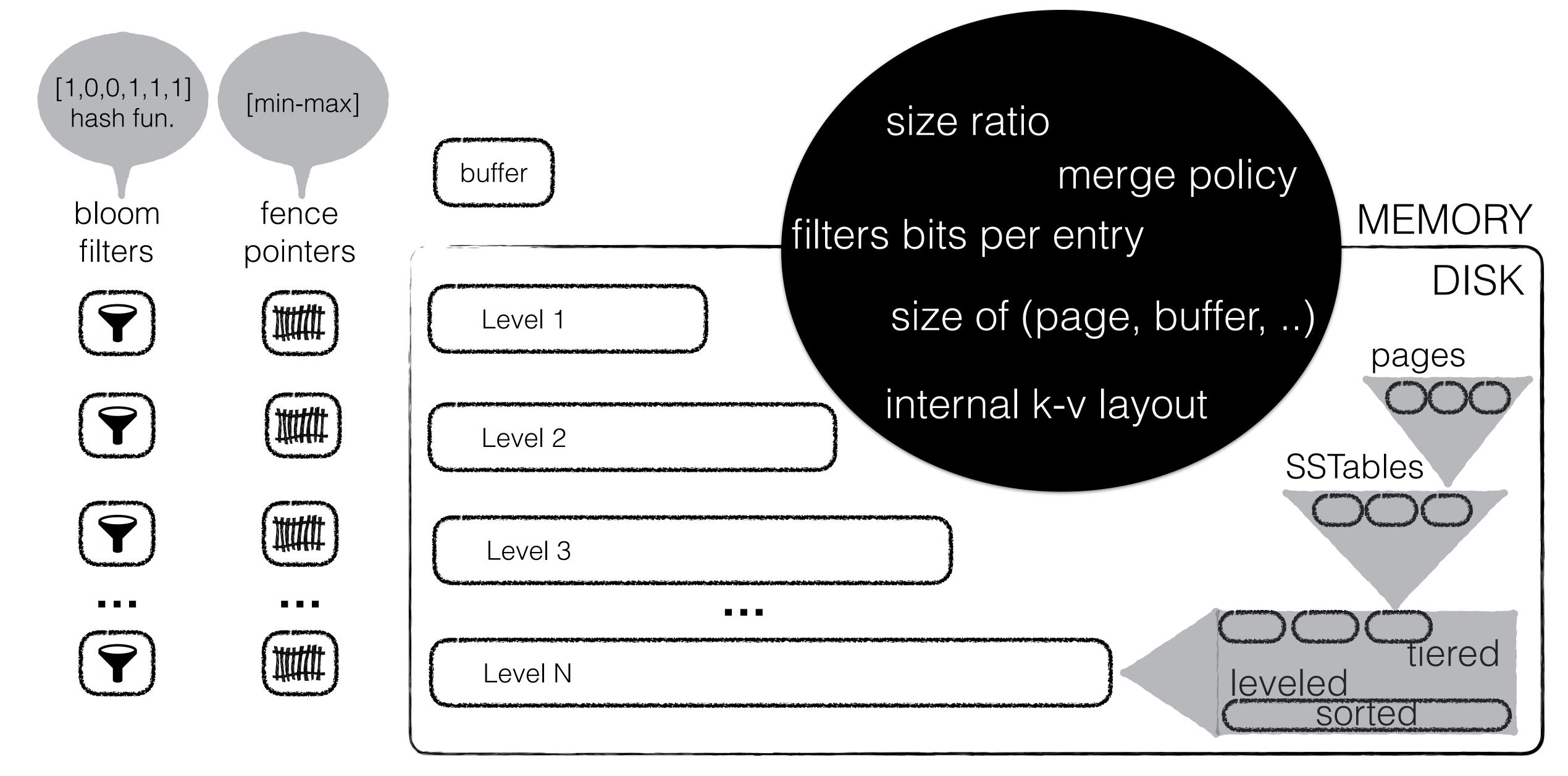














### size ratio merge policy filters bits per entry size of (page, buffer, ..) internal k-v layout



#### For every design principle X:

- 1. Which are X's meaningful values?
- 2. How does X affect read, update and memory amplification?
- 3. Should X be a design principle or can it be optimized out?



#### standard design: fixed per run

#### at most one I/O per level worst case I/O: sum of false positive rates

	buffer	
	Level 1	
	Level 2	
	Level N	
t	its per entry in bloom filter	



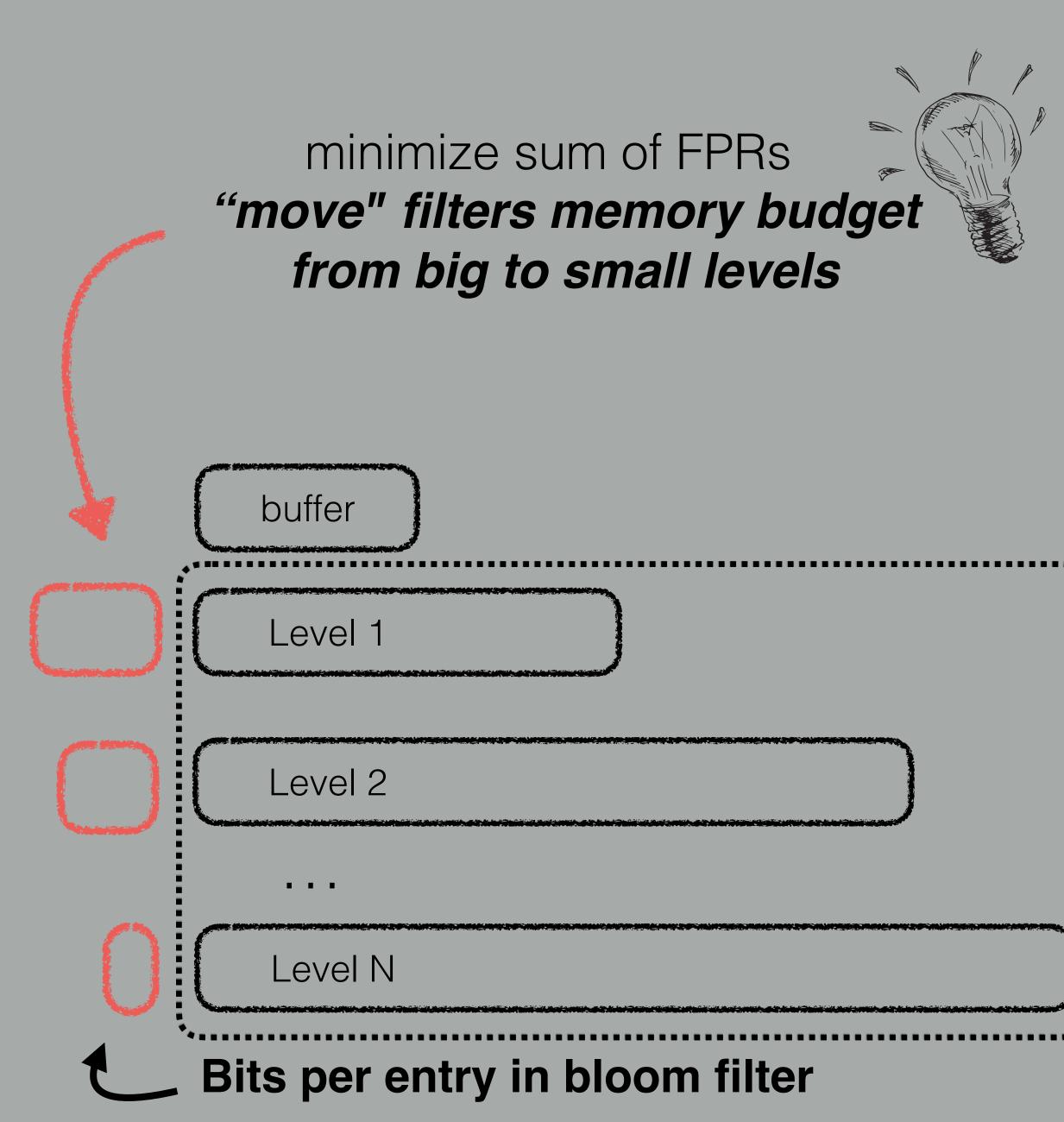
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### minimize sum of FPRs *"move" filters memory budget from big to small levels*

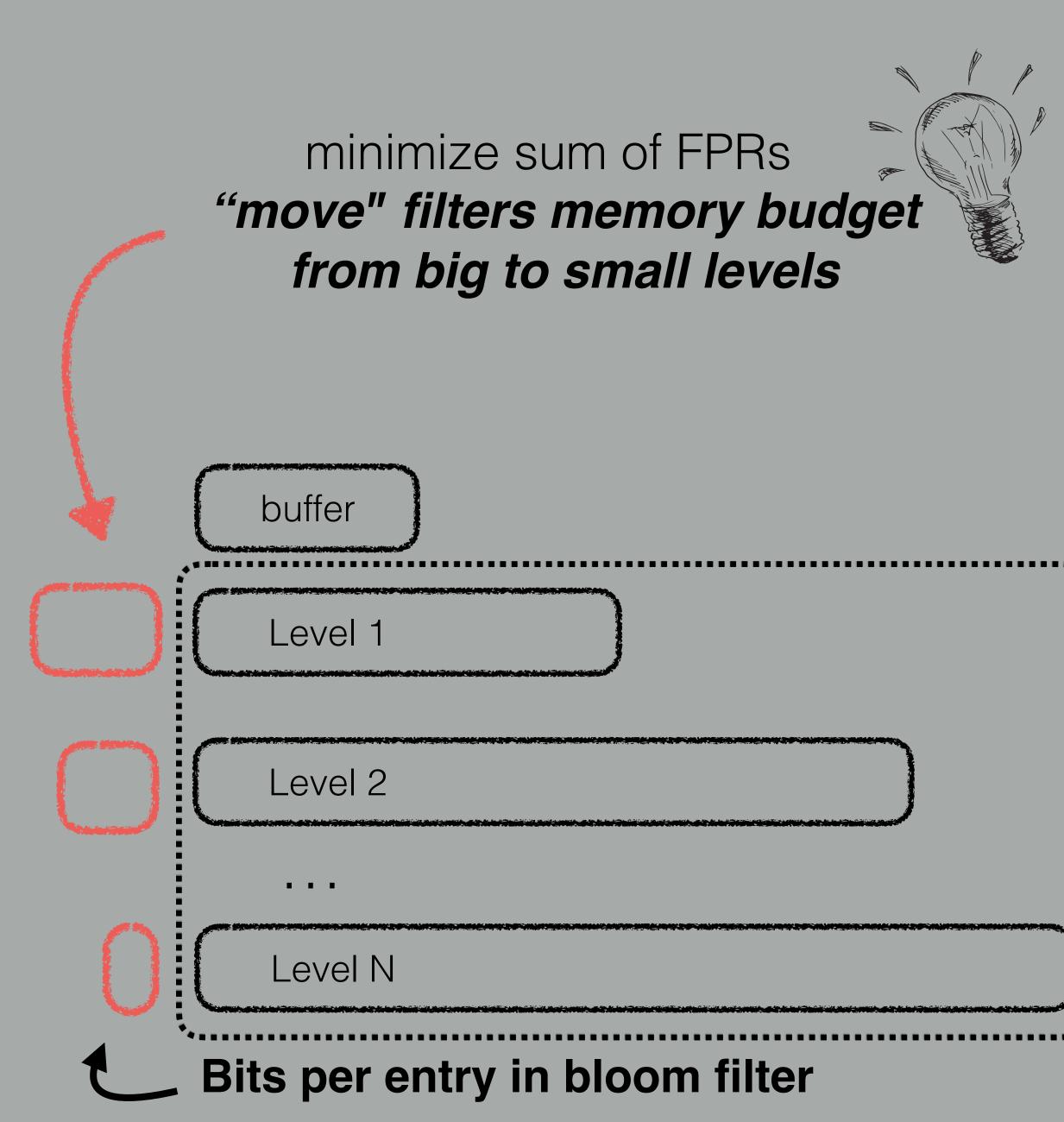
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	Bi	ts per entry in bloom filter	



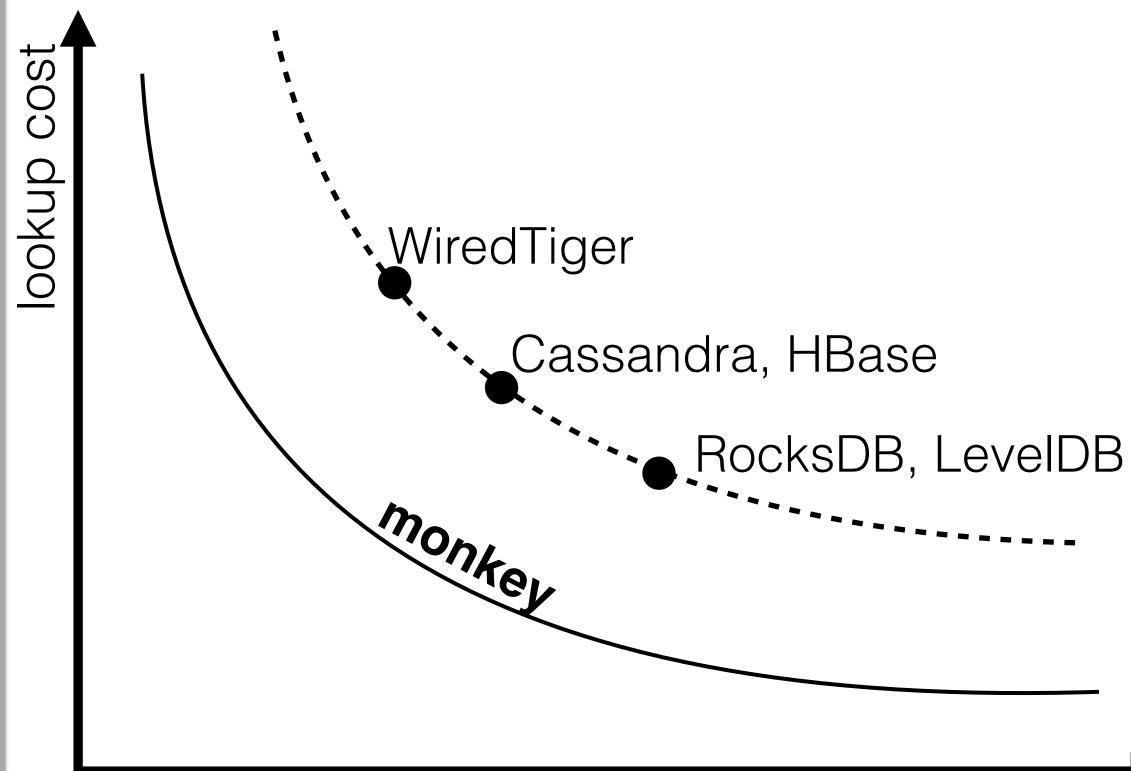
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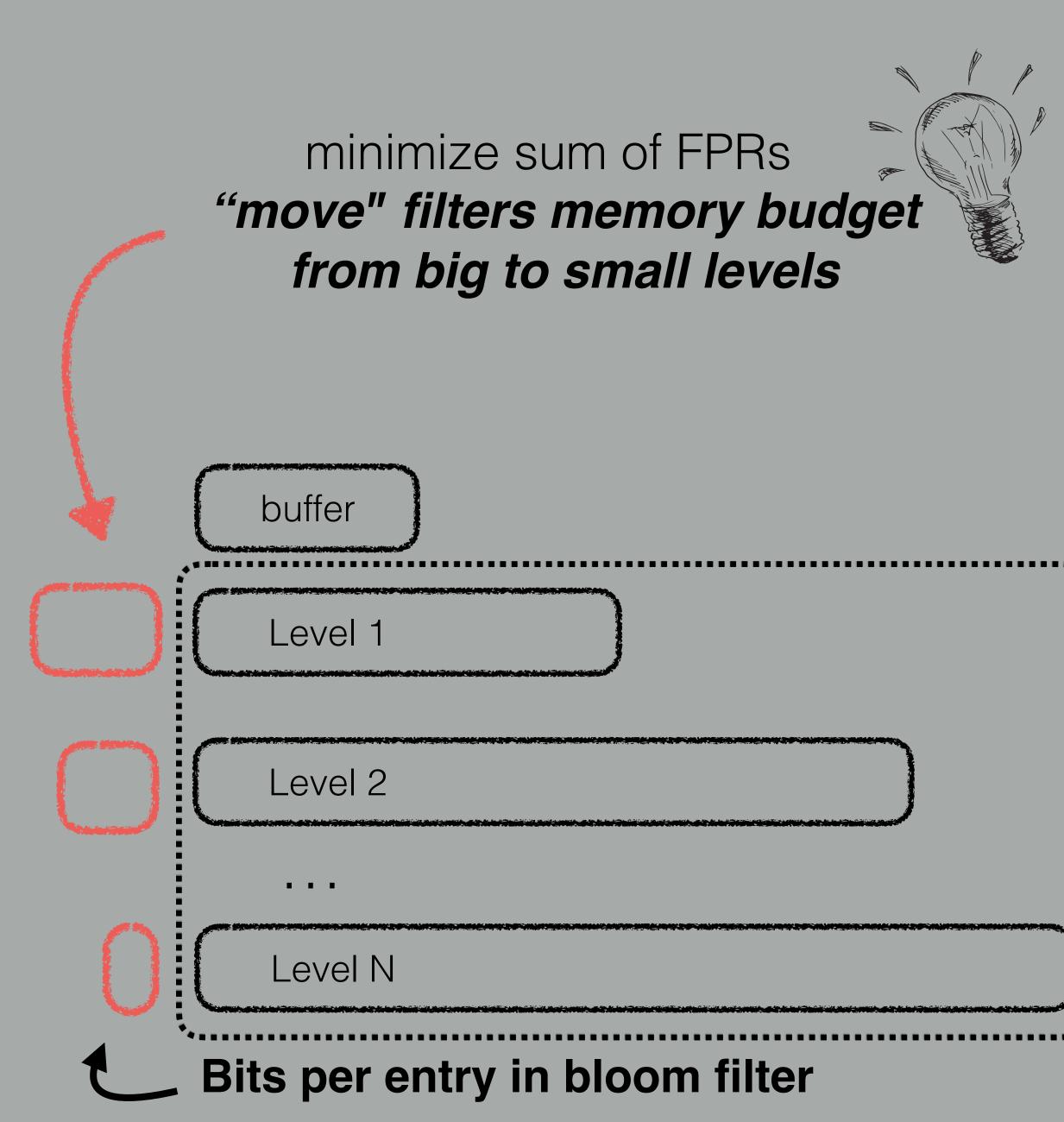




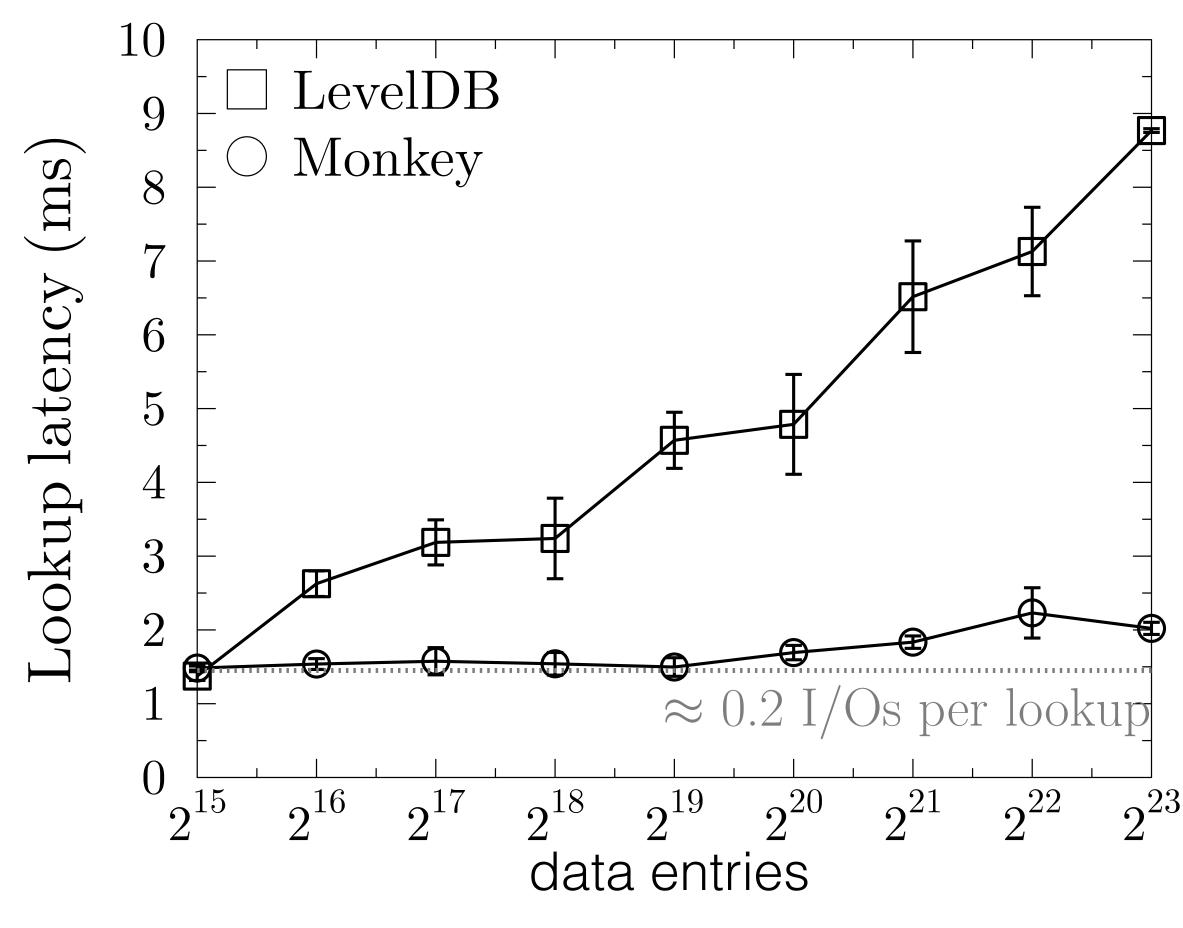


update cost







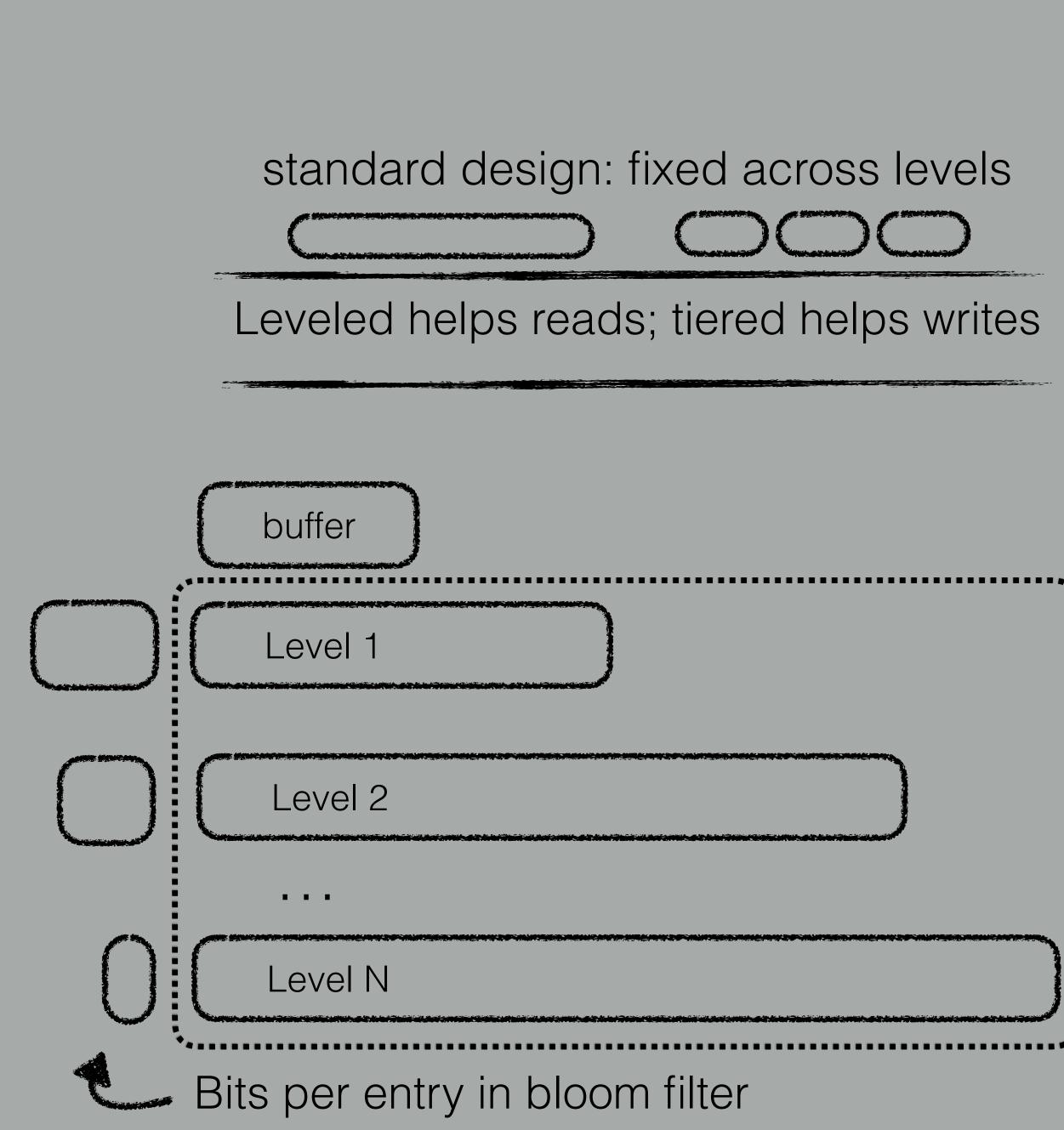


uniform, zero result, point queries, entry size=1KB



#### merge policy dostoevsky@SIGMOD2018 **Do**stoevsky: **S**pace-**T**ime **O**ptimized Evolvable Scalable Key-Value Store







#### merge policy dostoevsky@SIGMOD2018 **Do**stoevsky: **S**pace-**T**ime **O**ptimized Evolvable Scalable Key-Value Store





	buffer	
	Level 1	
	Level 2	
()	Level N	
	Bits per entry in bloom filter	

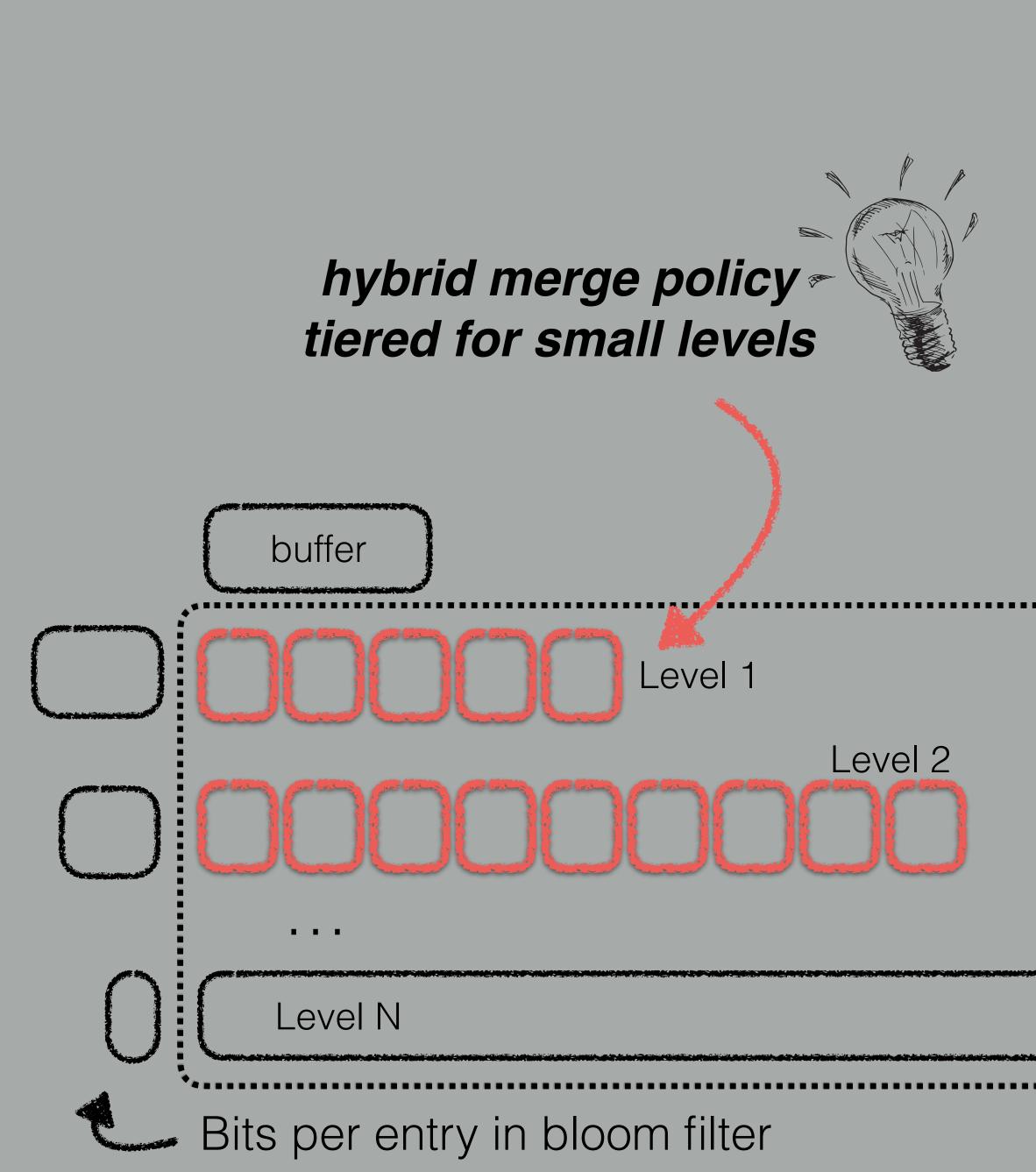


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#### merge policy dostoevsky@SIGMOD2018 **Do**stoevsky: **S**pace-**T**ime **O**ptimized Evolvable Scalable Key-Value Store

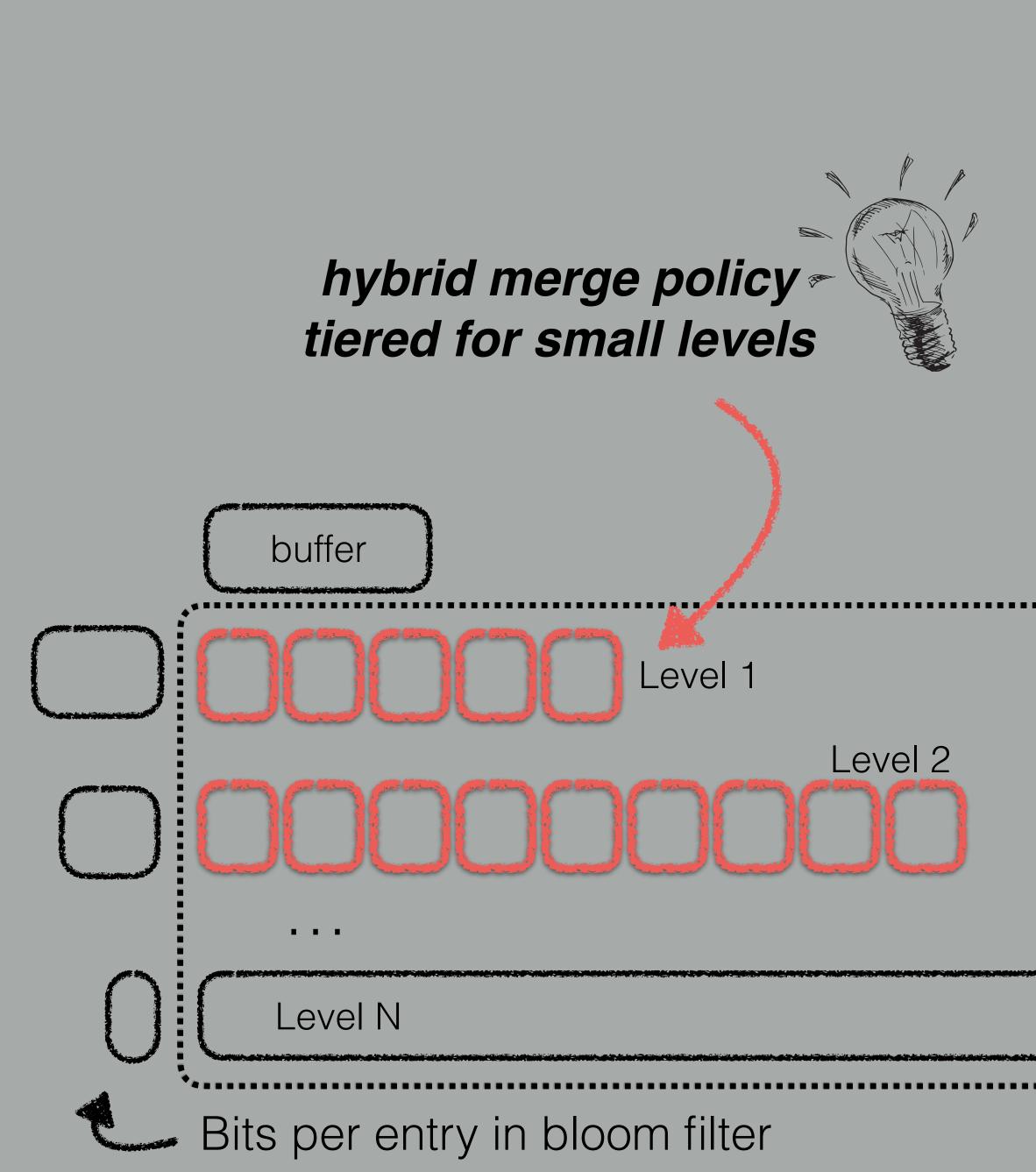






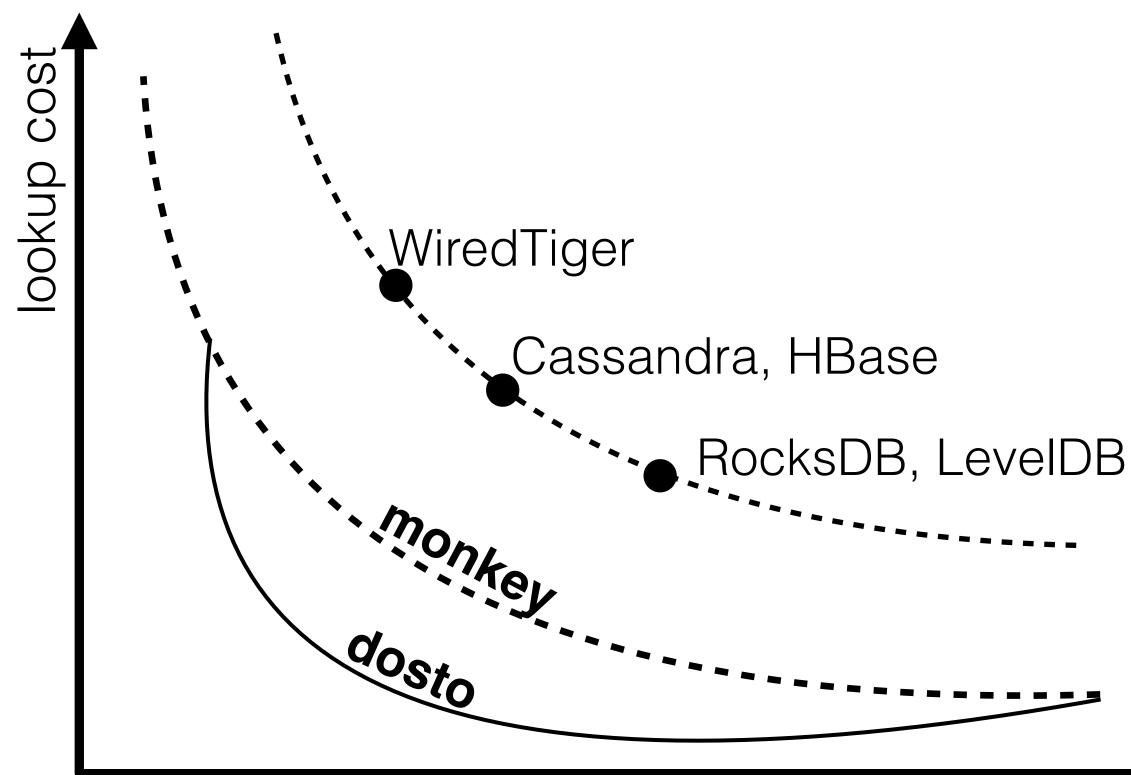
## merge policy dostoevsky@SIGMOD2018 **Do**stoevsky: **S**pace-**T**ime **O**ptimized Evolvable Scalable Key-Value Store







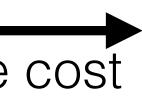
merge policy dostoevsky@SIGMOD2018 **Do**stoevsky: **S**pace-**T**ime **O**ptimized Evolvable Scalable Key-Value Store

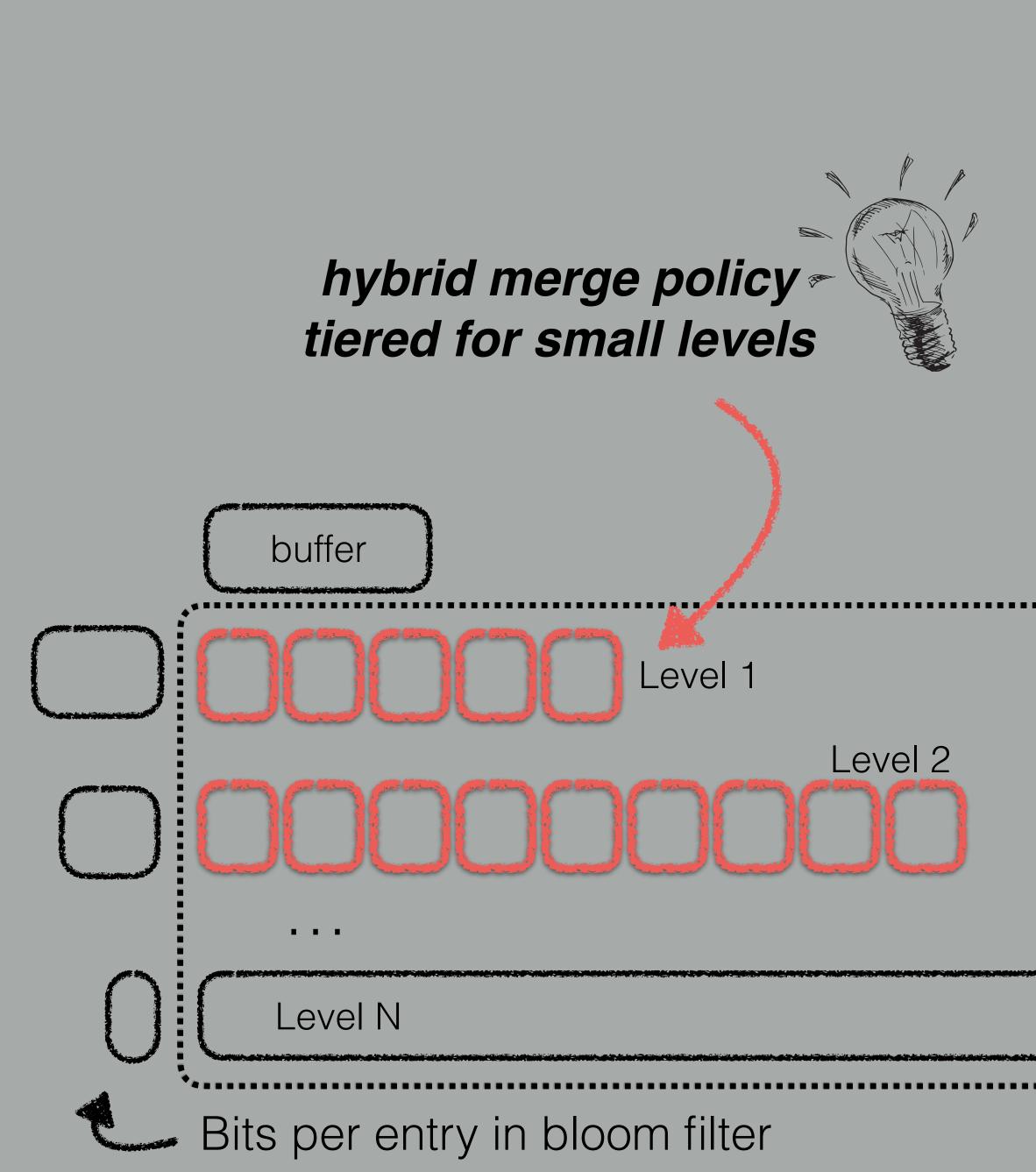


update cost



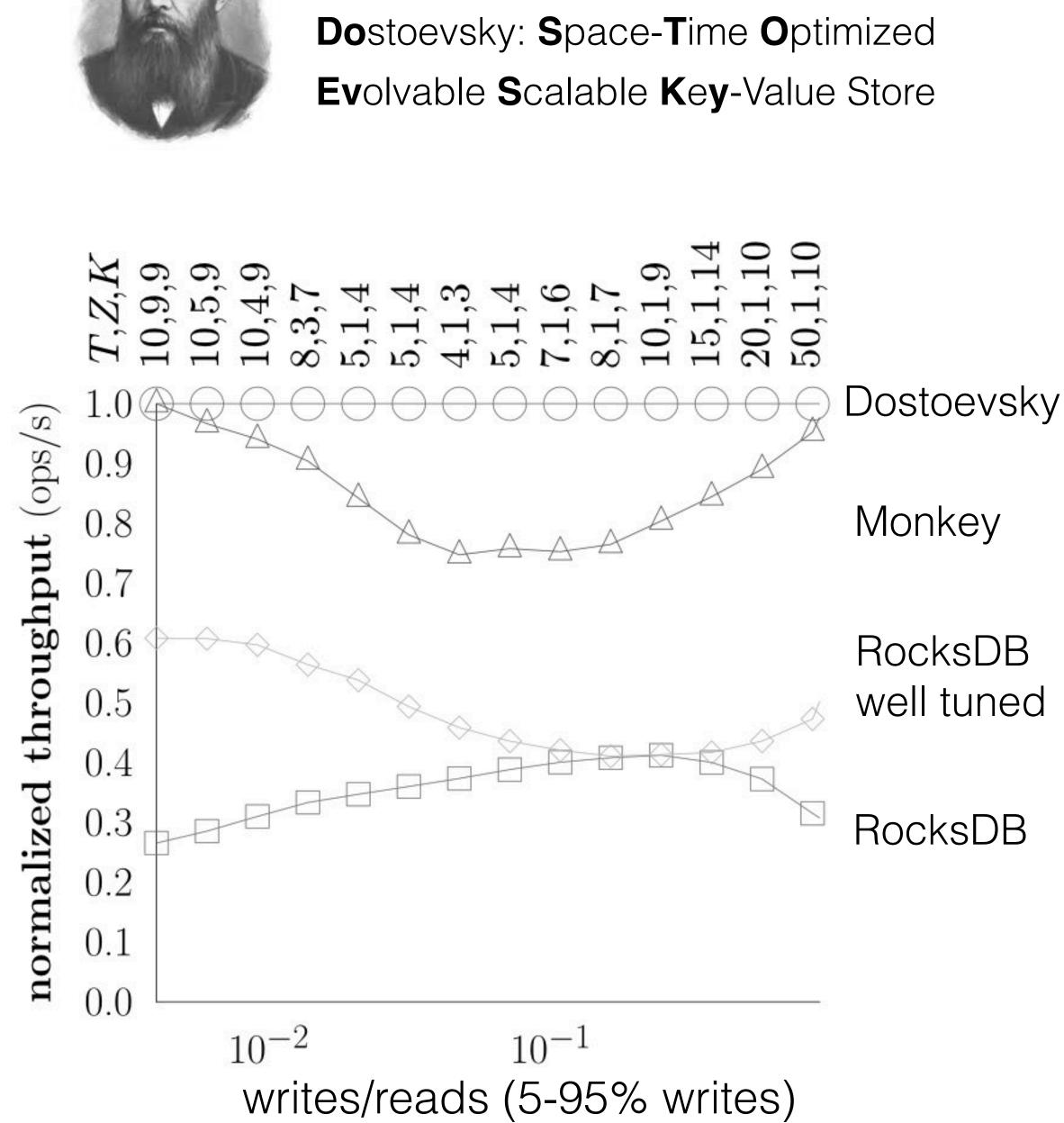








merge policy dostoevsky@SIGMOD2018

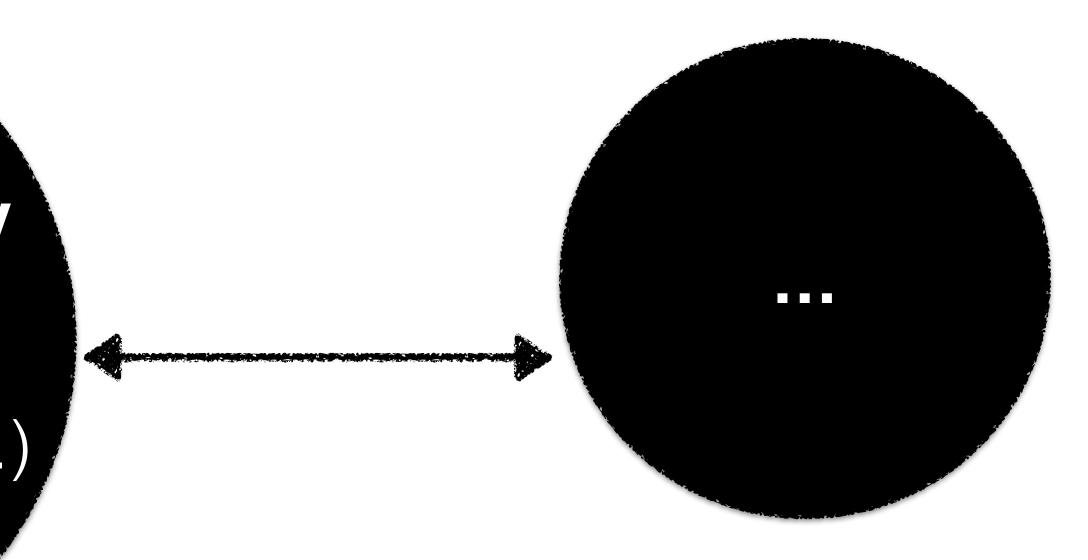


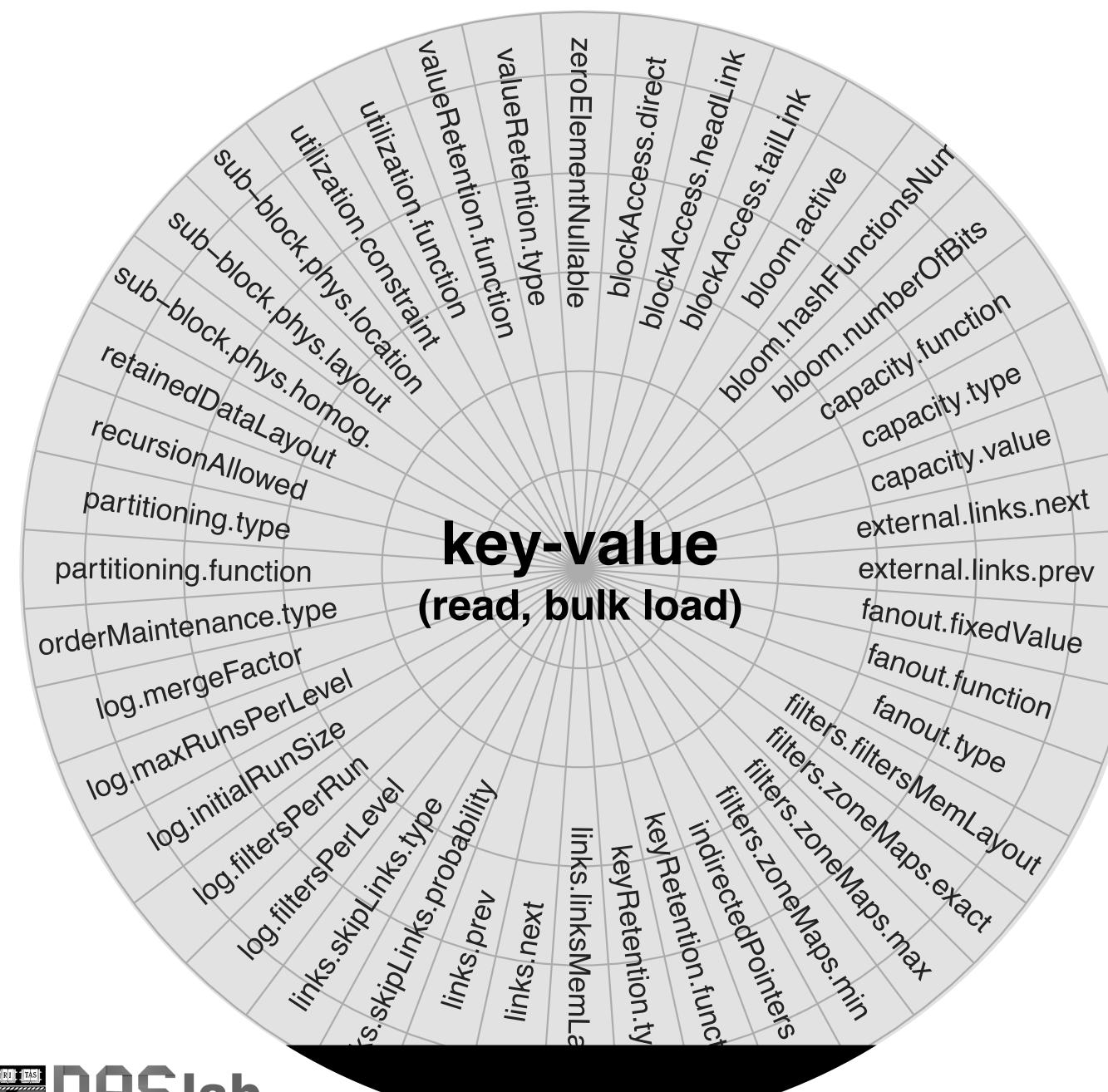
### arrays

# size ratio merge policy filters bits per entry size of (page, buffer, ..) internal k-v layout



# b-trees



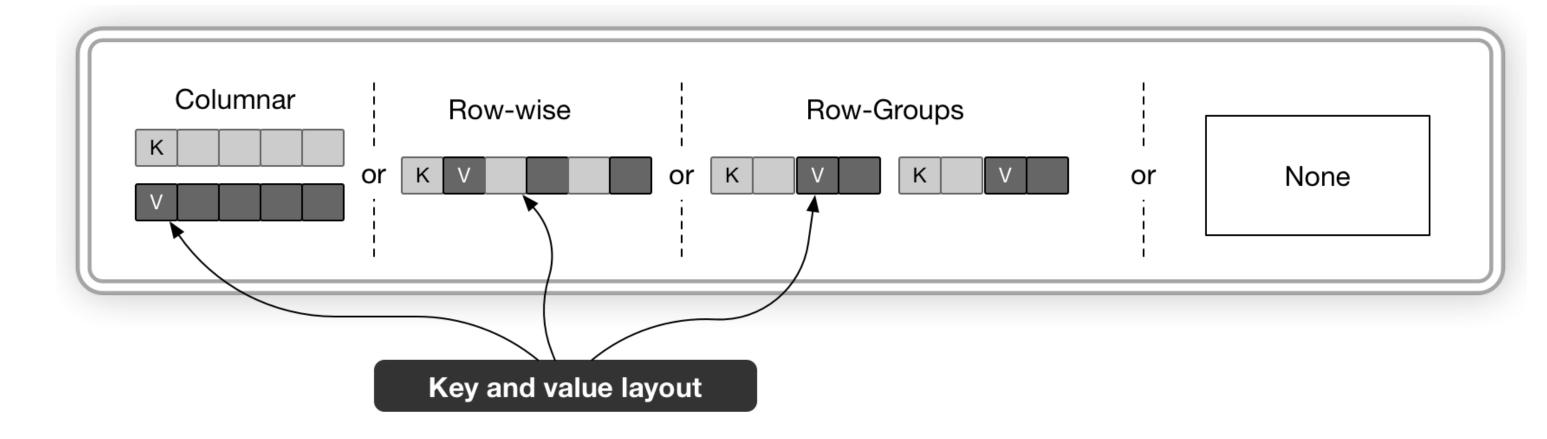


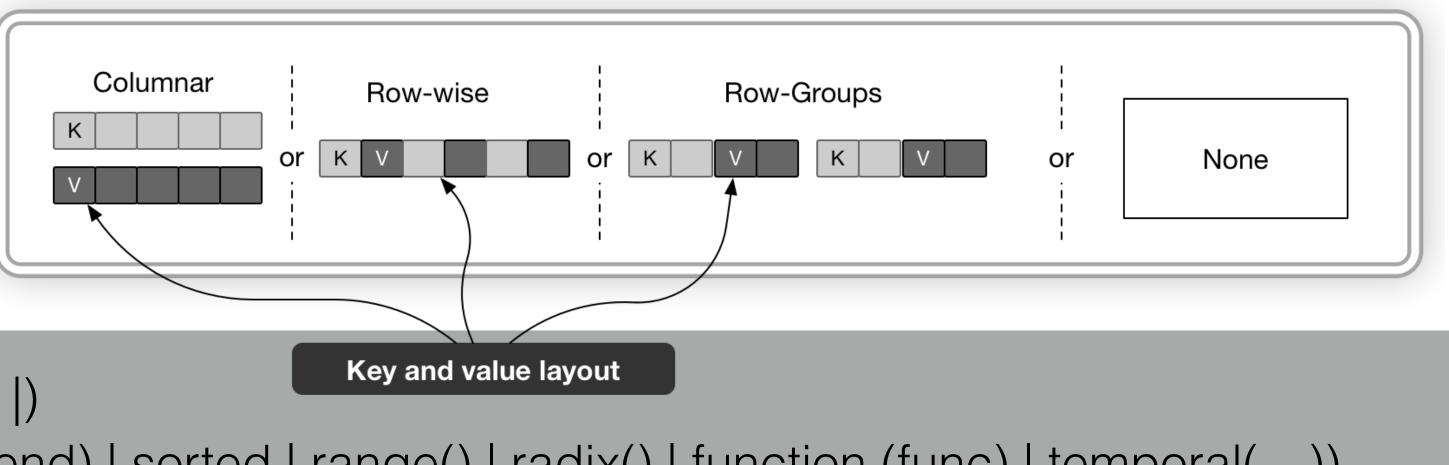


@SIGMOD18

# DESCRIBE ONE DATA BLOCK AT A TIME AS A SET OF CONCEPTS physical layout and domain partitioning

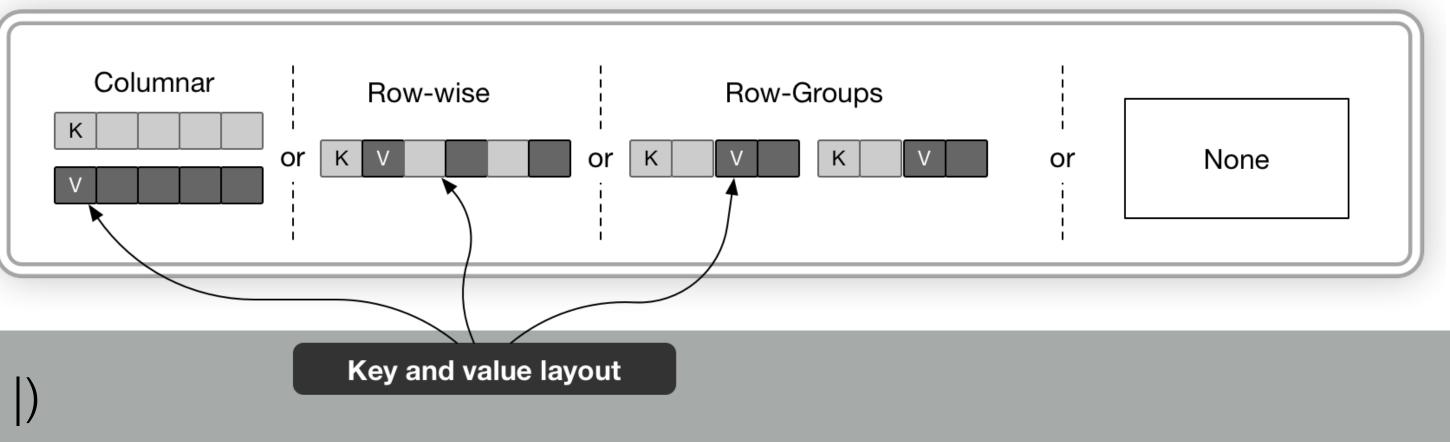






**Fanout** (fixed/functional | unlimited | terminal |) Key partitioning (none(fw-append | bw-append) | sorted | range() | radix() | function (func) | temporal(...))



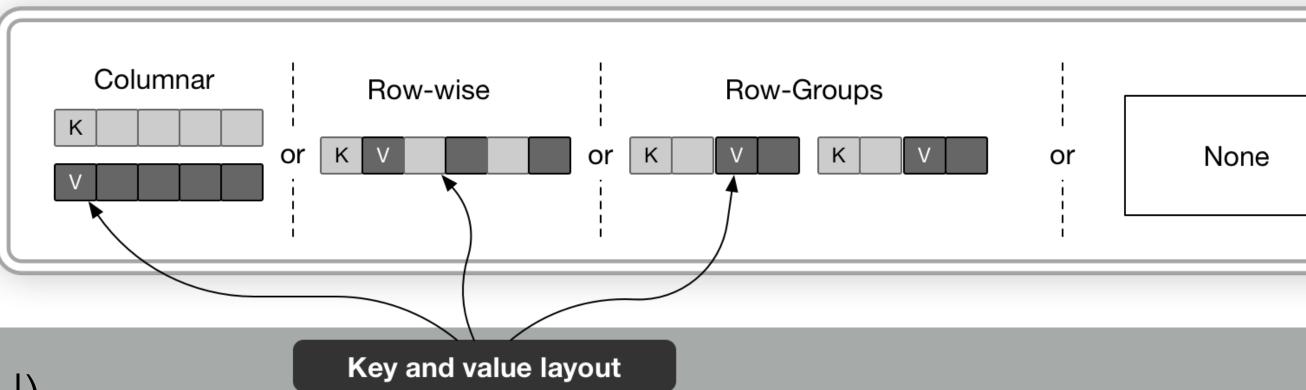


**Fanout** (fixed/functional | unlimited | terminal |)

**Intra node access** (direct | head\_link | tail\_link | link\_function(func))

# Key partitioning (none(fw-append | bw-append) | sorted | range() | radix() | function (func) | temporal(...))



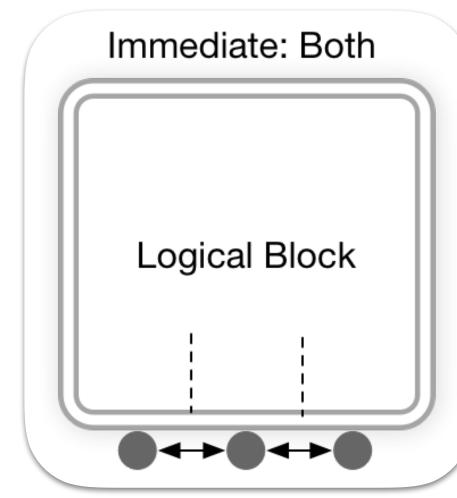


Fanout (fixed/functional | unlimited | terminal |)
Key and value layout
Key and value layout
Key and value layout
Key and value layout

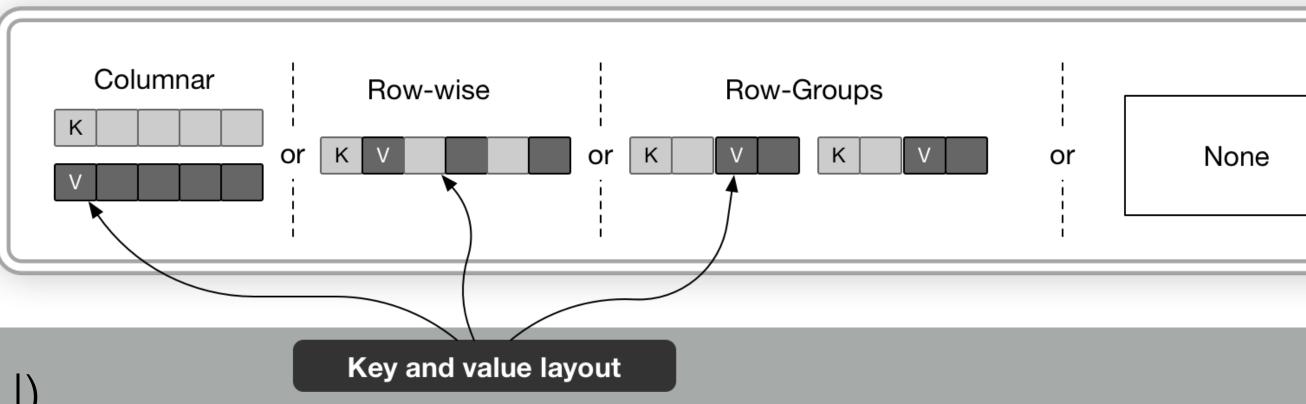
Intra node access (direct | head\_link | tail\_link | link\_function(func))

Sub block links (next | previous | both | none)

Sub block skip links (perfect | randomized(prob: double) | function(func) | none)







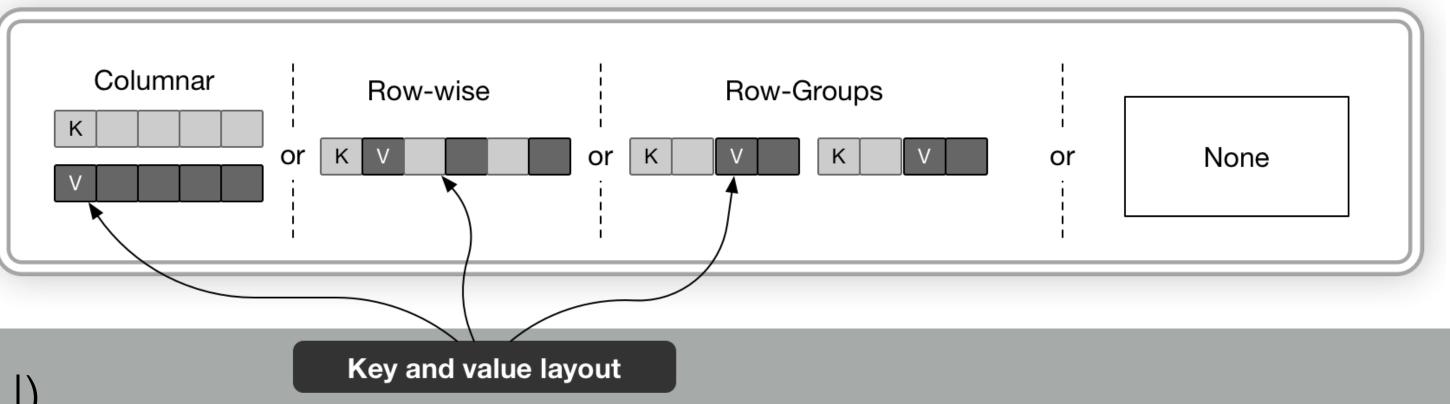
**Fanout** (fixed/functional | unlimited | terminal |) Key partitioning (none(fw-append | bw-append) | sorted | range() | radix() | function (func) | temporal(...))

**Intra node access** (direct | head\_link | tail\_link | link\_function(func))

Sub block links (next | previous | both | none) **Sub block skip links** (perfect | randomized(prob: double) | function(func) | none)

Consolidate Scatter **Zone Maps** (min | max | both | exact | off) **Bloom filters** (off | on(num\_hashes: int, num\_bits: int)) BF BF **Filters layout** (consolidate | scatter) **Links layout** (consolidate | scatter) BF | BF





**Fanout** (fixed/functional | unlimited | terminal |) Key partitioning (none(fw-append | bw-append) | sorted | range() | radix() | function (func) | temporal(...))

**Intra node access** (direct | head\_link | tail\_link | link\_function(func))

Sub block links (next | previous | both | none) **Sub block skip links** (perfect | randomized(prob: double) | function(func) | none)

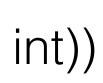
**Zone Maps** (min | max | both | exact | off)

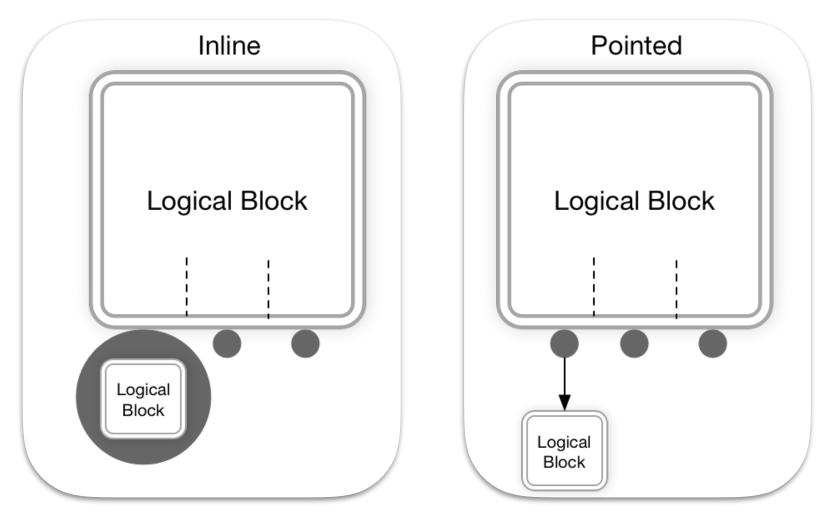
**Bloom filters** (off | on(num\_hashes: int, num\_bits: int))

**Filters layout** (consolidate | scatter)

**Links layout** (consolidate | scatter)

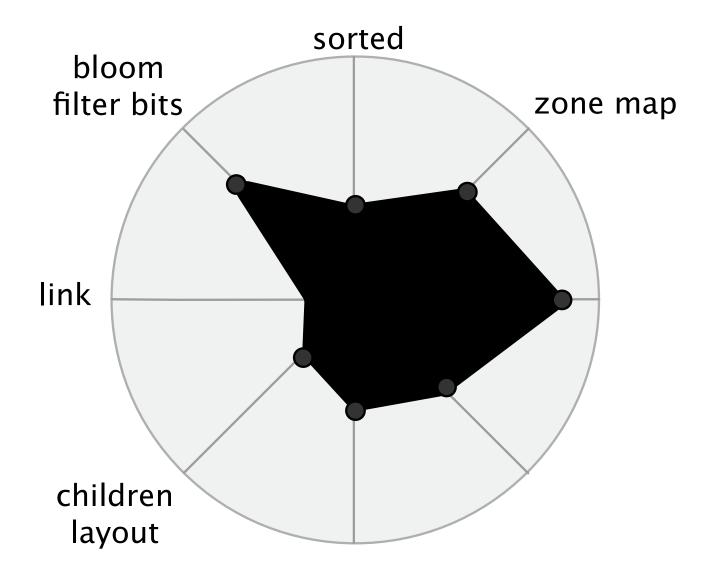
**Physical location** (inline | pointed | double- pointed) **Physical layout** (BFS | scatter)





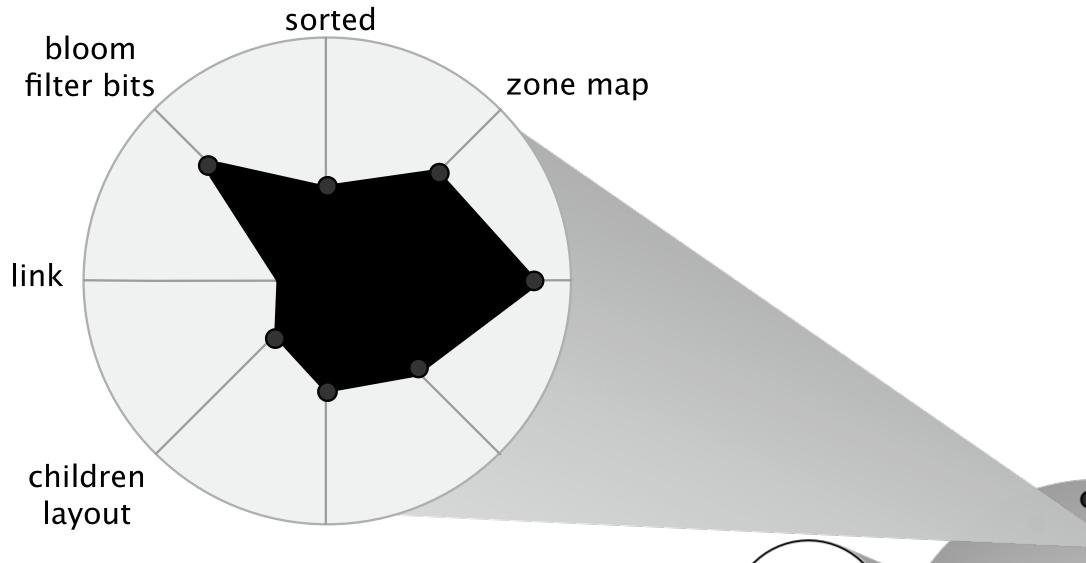


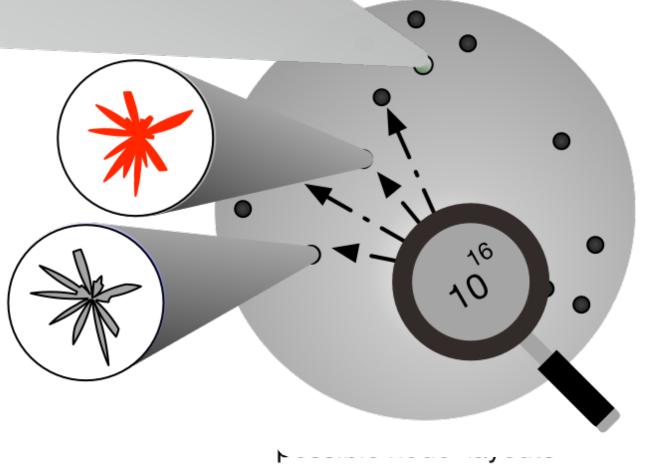
# SETS OF CONCEPTS





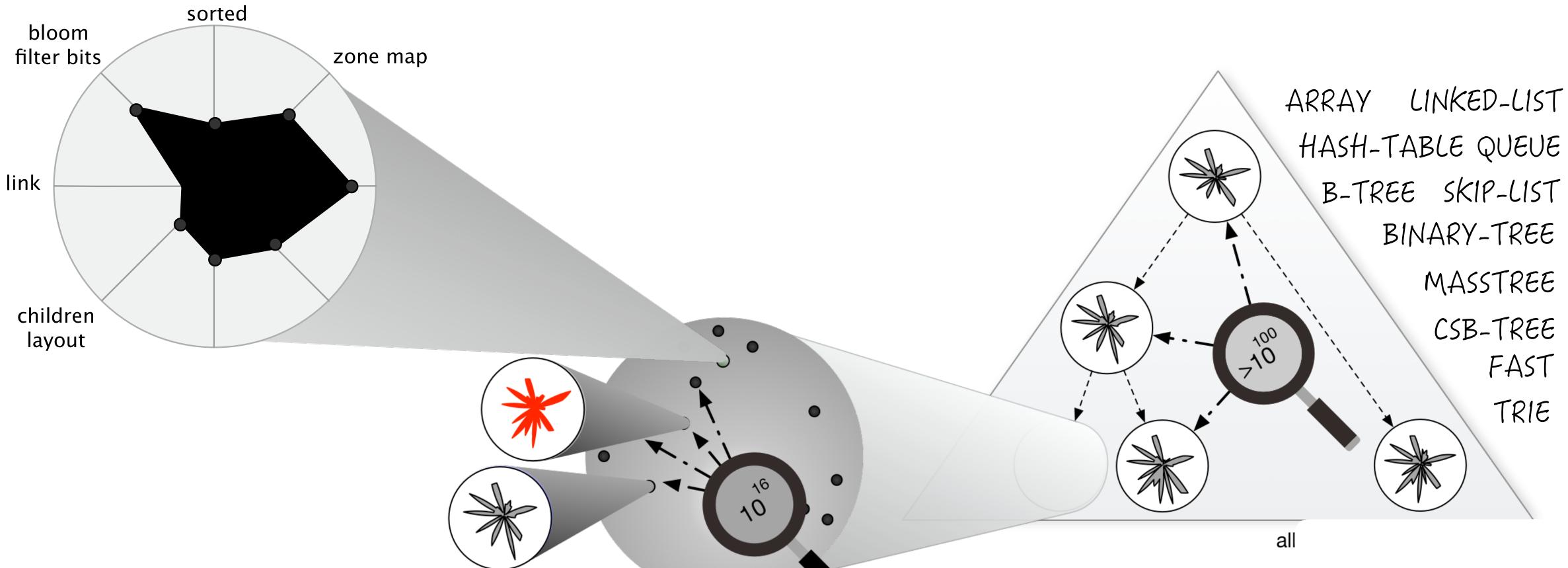
# SETS OF CONCEPTS POSSIBLE NODE DESIGNS

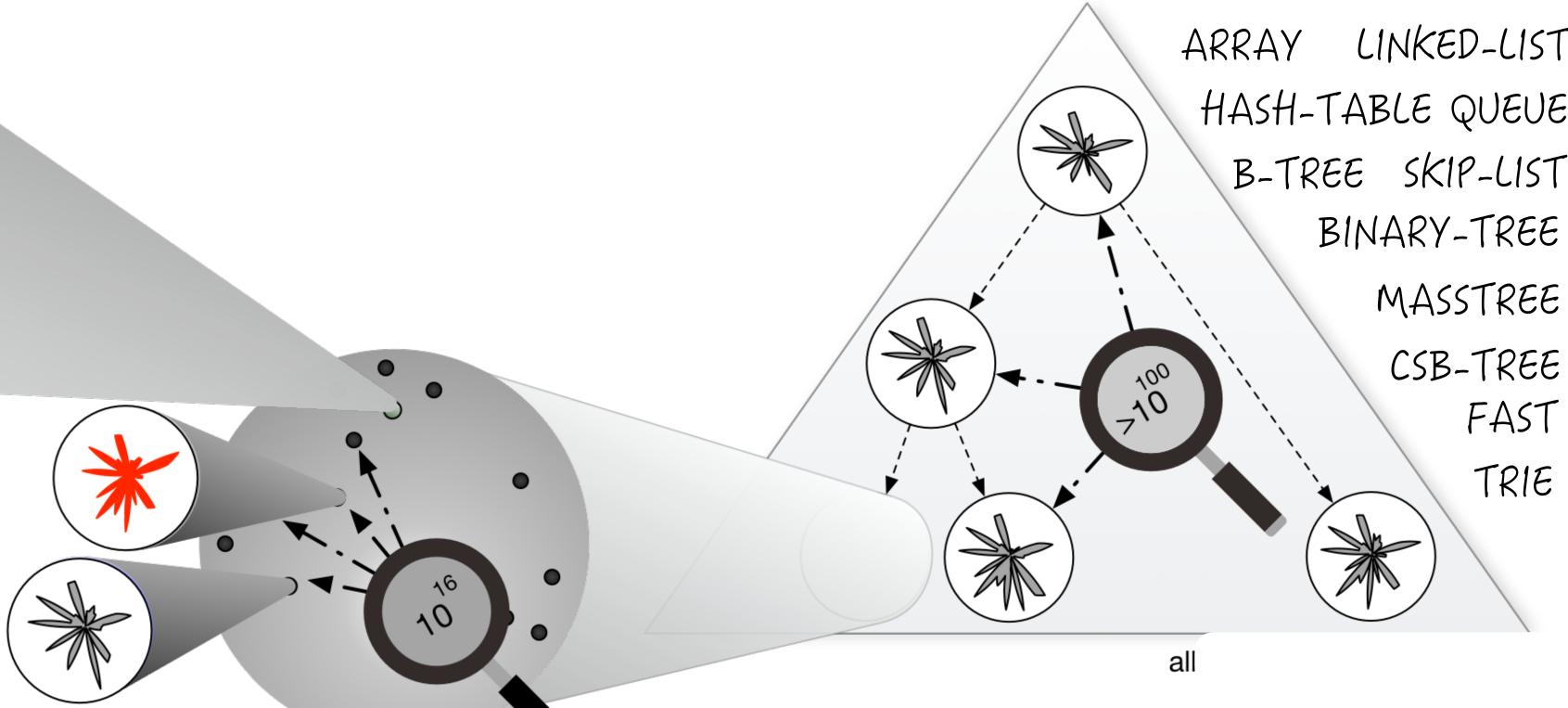






### SETS OF CONCEPTS POSSIBLE NODE DESIGNS POSSIBLE STRUCTURES









# the perio

classes of designs classes Tries **LSM-Trees B-trees** of primitives & Variants & Variants & Variants DONE DONE DONE Partitioning Logarithmic DONE DONE DONE Design DONE DONE Fractional Cascading Log-DONE DONE Structured DONE Buffering Differential DONE Updates Sparse DONE Indexing

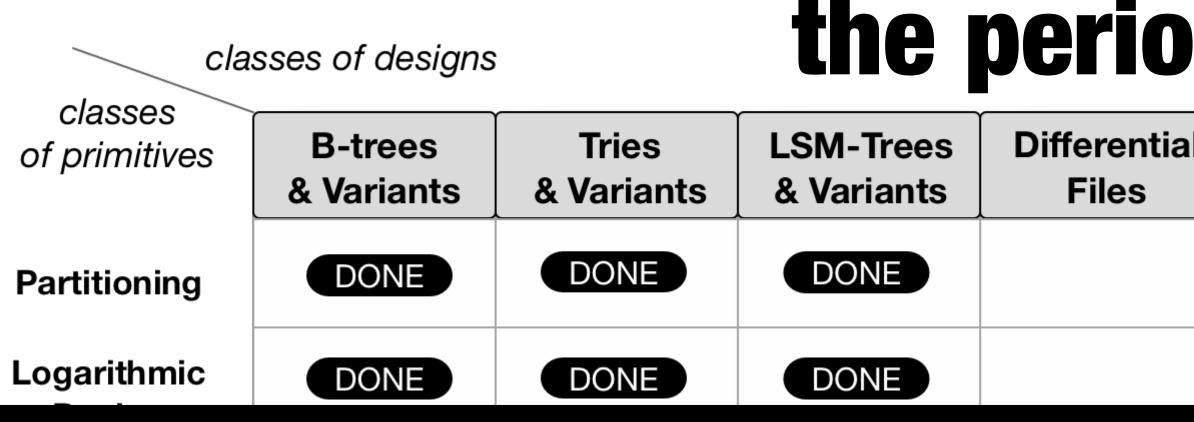
DONE

Adaptivity





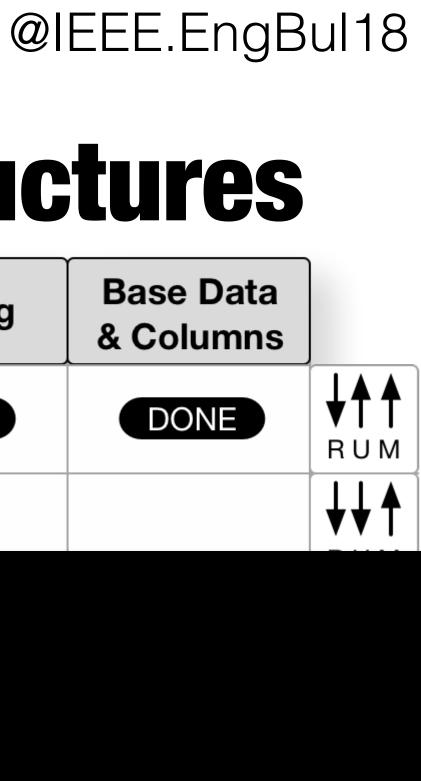
)erio(	dic tal	ble of	data	<b>struc</b>	tures	)
Differential Files	Membership Tests	Zone maps & Variants	Bitmaps & Variants	Hashing	Base Data & Columns	
				DONE	DONE	<b>↓</b> ↑↑ RUM
						<b>↓↓↑</b> RUM
DONE						
DONE						<b>↓</b> RUM
DONE			DONE			<b>↓</b> ♦↑ RUM
DONE						<b>↑↓↓</b> RUM
	DONE	DONE				<b>↓</b> ♦↑ RUM
					DONE	





Differential Updates	DONE		DONE					<b>↑</b> ↓↓ RUM
Sparse Indexing Adaptivity	DONE			DONE	DONE			<b>↓</b> ♦↑ RUM
	DONE						DONE	



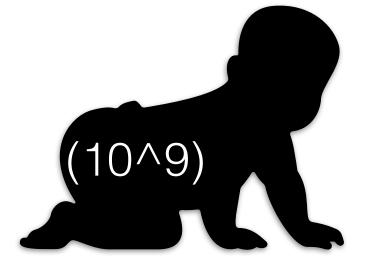


# the periodic table of data structures

al	Membership Tests	Zone maps & Variants	Bitmaps & Variants	Hashing	Base Data & Columns
				DONE	DONE

# PAPER MACHINE



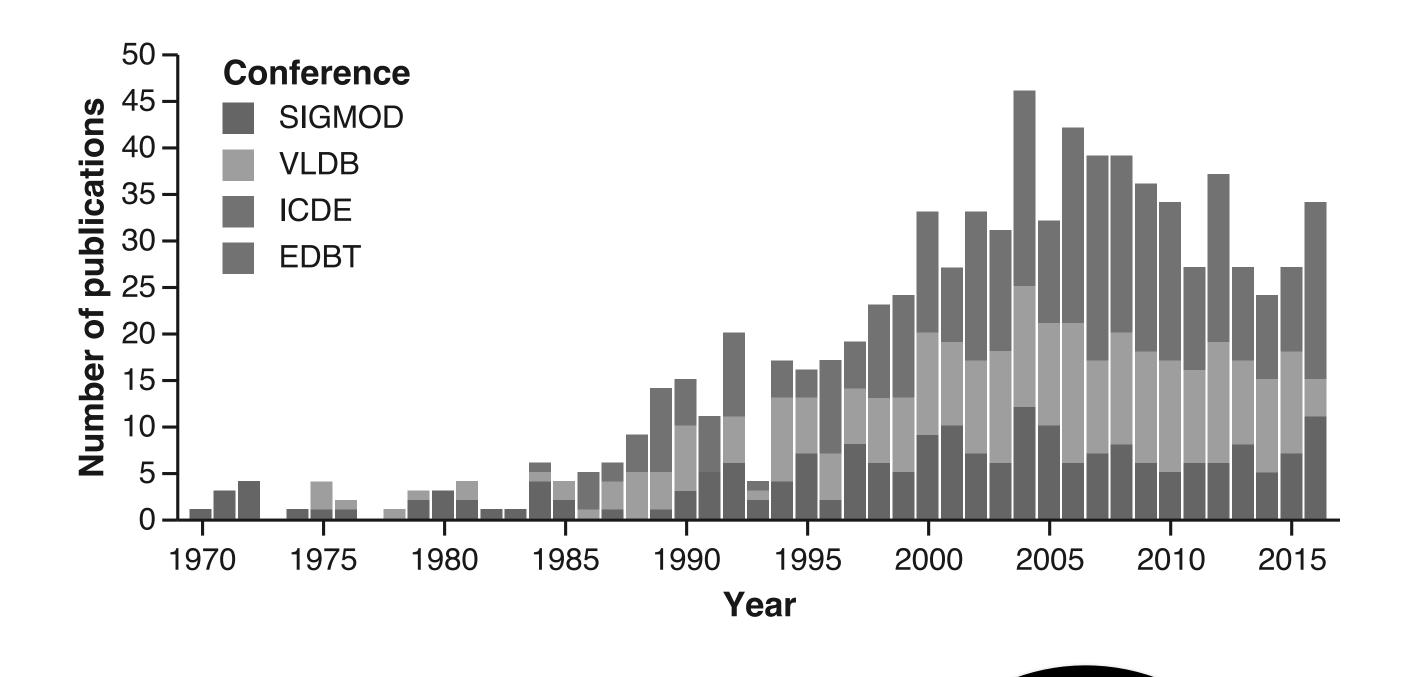


# PEOPLE ON EARTH

STARS IN THE SKY



# POSSIBLE DATA STRUCTURES





# PEOPLE ON EARTH

STARS IN THE SKY

 $(10^{24})$ 



# ~5K since the dawn of CS

### (10^32, 2-node) (10^48, 3-node)

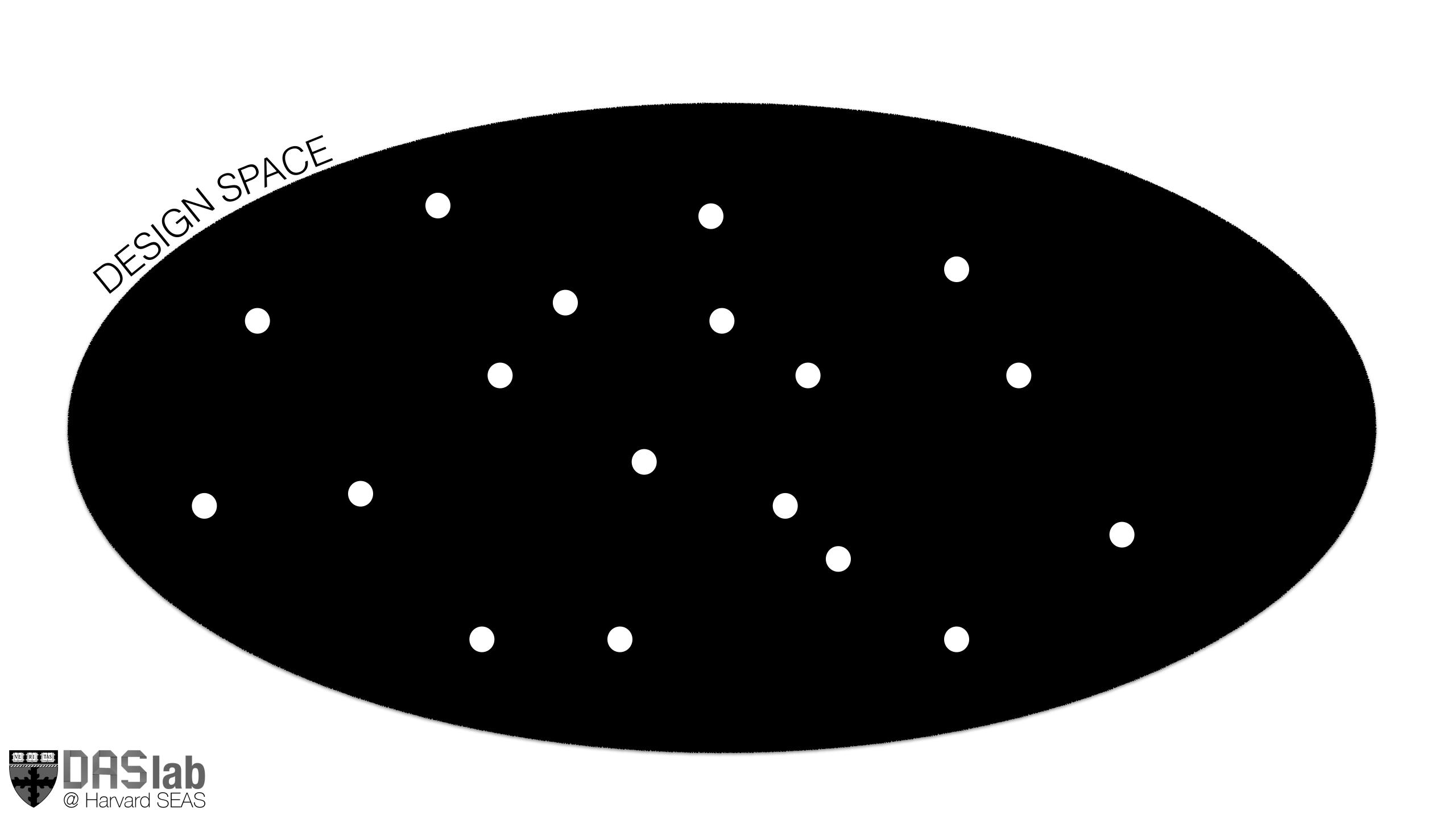
# POSSIBLE DATA STRUCTURES

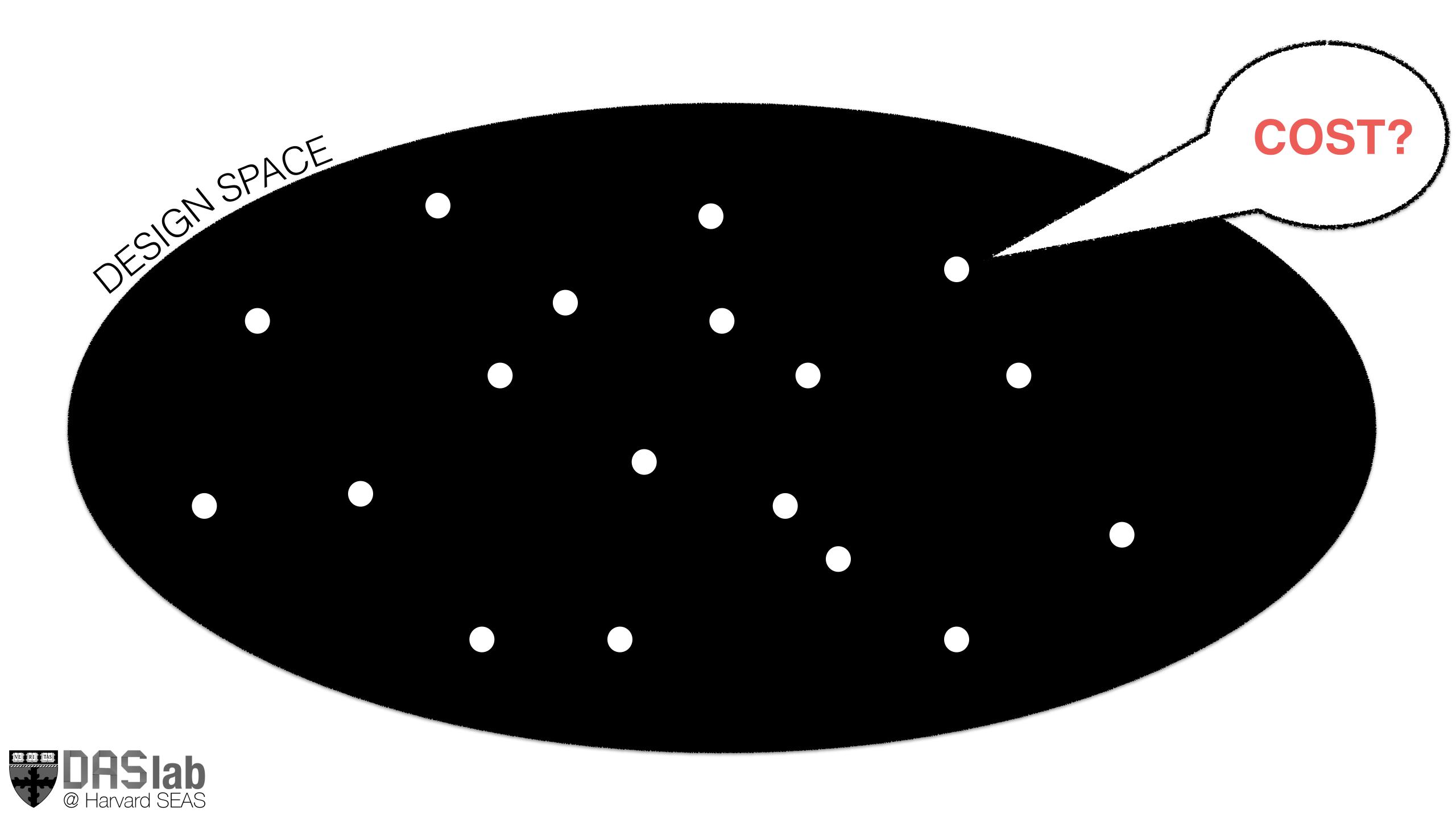
# DESIGN SPACE

if we know the fundamental building blocks, how they combine and their **properties**,

then we can automate the discovery of novel combinations and tunings







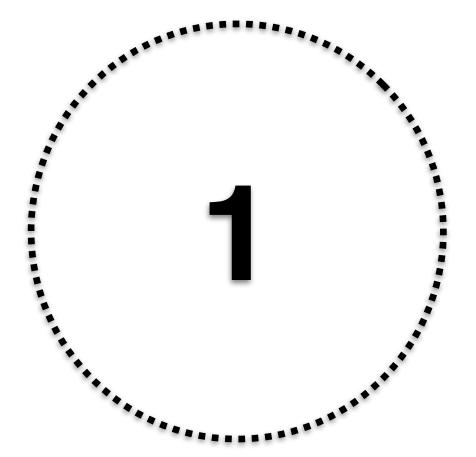
# DESIGN SPACE



# COST SYNTHESIS

# HOW TO USE

# HOW TO JUDGE A DESIGN?





# COMPLEXITY ANALYSIS

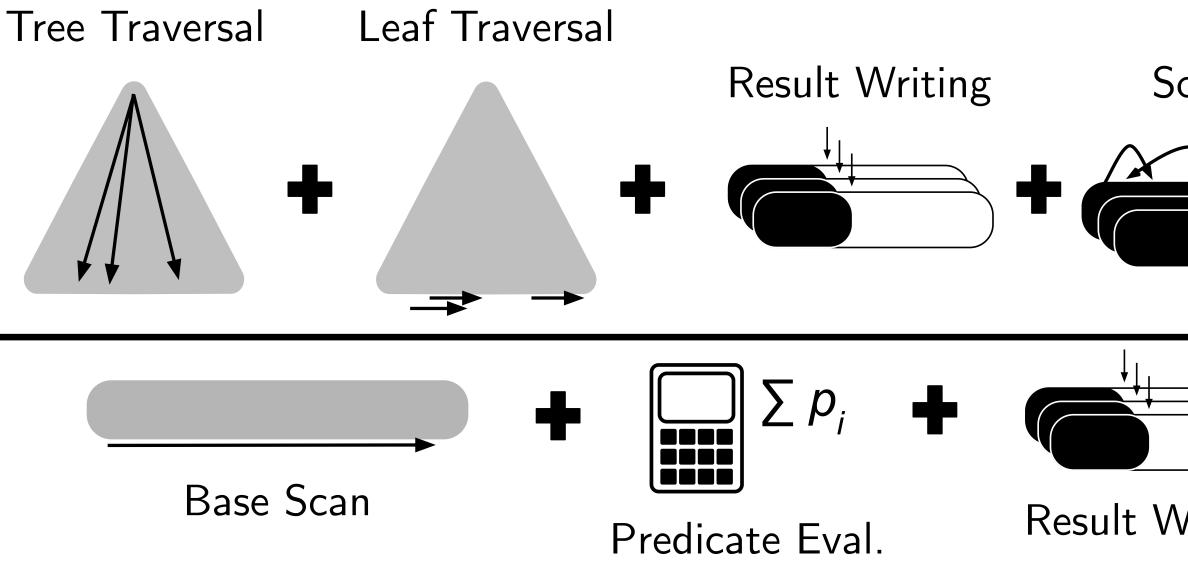
IMPLEMENTATION & TESTING



# GENERALIZED MODELS

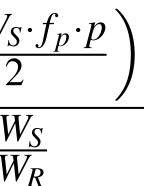
# HARD & SLOW

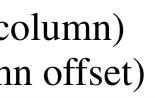
Access path selection @SIGMOD2017



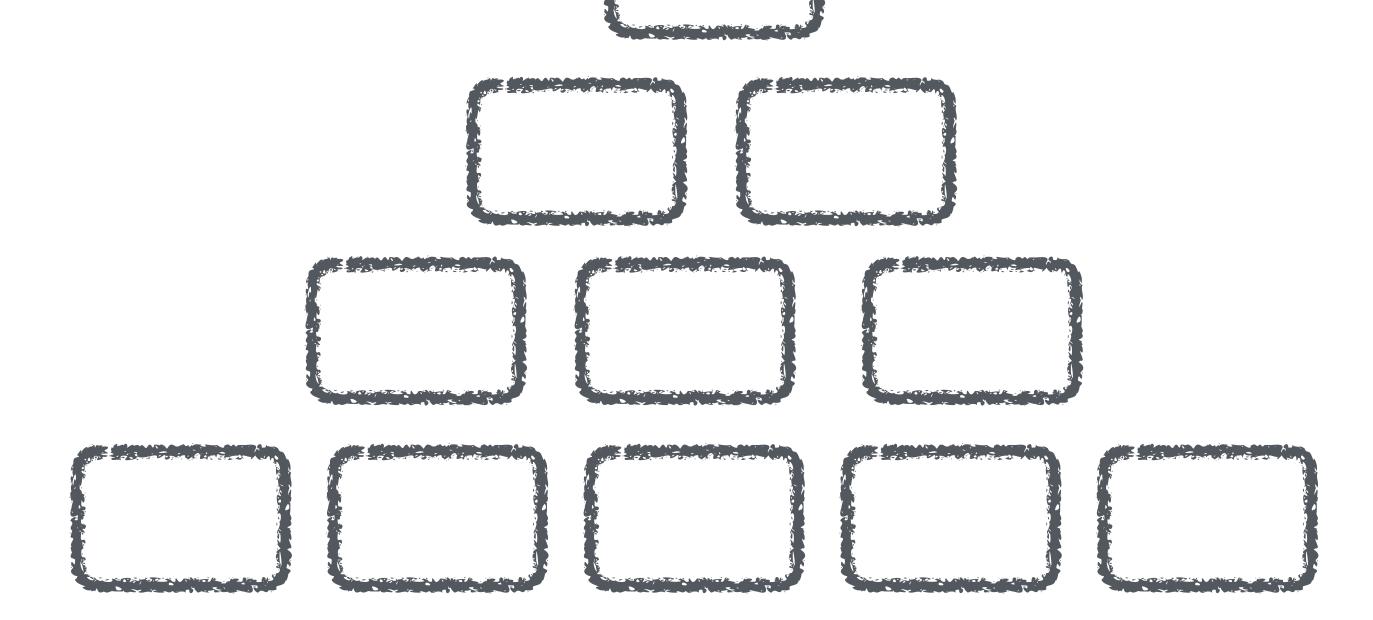
$$APS(q, S_{tot}) = \frac{q \cdot \frac{1 + \lceil log_b(N) \rceil}{N} \cdot \left(BW_S \cdot C_M + \frac{b \cdot BW_S \cdot C_A}{2} + \frac{b \cdot BW_S}{2} + \frac{b \cdot BW_S}{2} + \frac{b \cdot BW_S}{M} + \frac{max \left(ts, 2 \cdot f_p \cdot p \cdot q \cdot BW_S\right) + S_{tot} \cdot rw \cdot \frac{BW_S}{BW_R}}{max \left(ts, 2 \cdot f_p \cdot p \cdot q \cdot BW_S\right) + S_{tot} \cdot rw \cdot \frac{BW_S}{BW_R}} + \frac{S_{tot} \cdot log_2 \left(S_{tot} \cdot N\right) \cdot BW_S \cdot C_A}{max \left(ts, 2 \cdot f_p \cdot p \cdot q \cdot BW_S\right) + S_{tot} \cdot rw \cdot \frac{BW_S}{BW_R}}$$

	Workload	q	number of queries
		Si	selectivity of query <i>i</i>
		$S_{tot}$	total selectivity of the workload
Sorting	Dataset	N	data size (tuples per column)
Joi ting		ts	tuple size (bytes per tuple)
$\frown \land$	Hardware	$C_A$	L1 cache access (sec)
		$C_M$	LLC miss: memory access (sec)
		$BW_S$	scanning bandwidth (GB/s)
		$BW_R$	result writing bandwidth (GB/s)
		$BW_I$	leaf traversal bandwidth (GB/s)
		р	The inverse of CPU frequency
		$f_p$	Factor accounting for pipelining
	Scan	rW	result width (bytes per output tuple)
Vriting	&	b	tree fanout
	Index	aw	attribute width (bytes of the indexed co
		OW	offset width (bytes of the index column





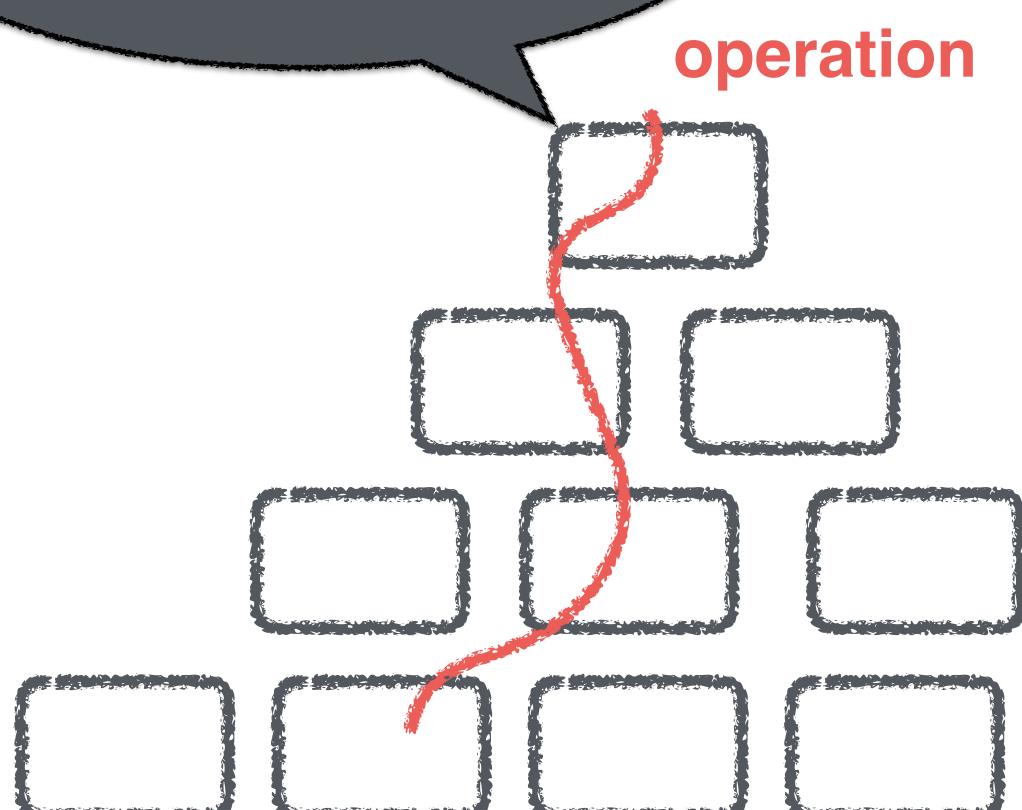
# DESIGN SPACE OF POSSIBLE STORAGE LAYOUTS



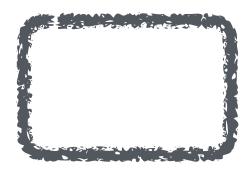
----



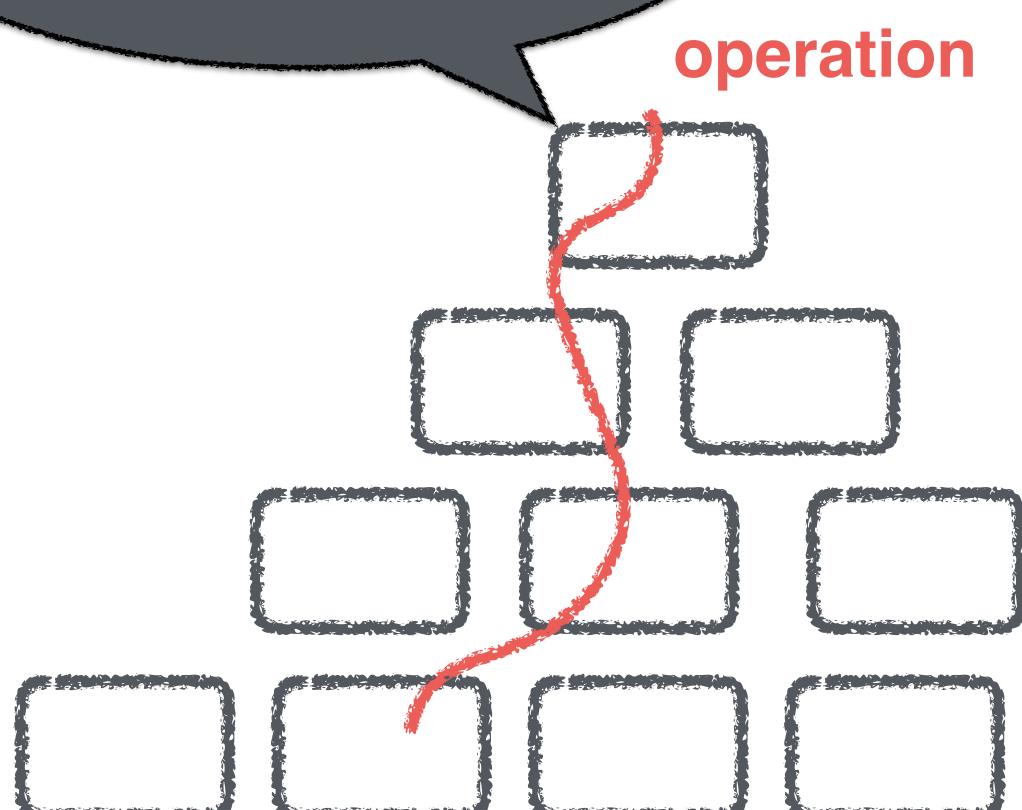
# DESIGN SPACE OF POSSIBLE STORAGE LAYOUTS







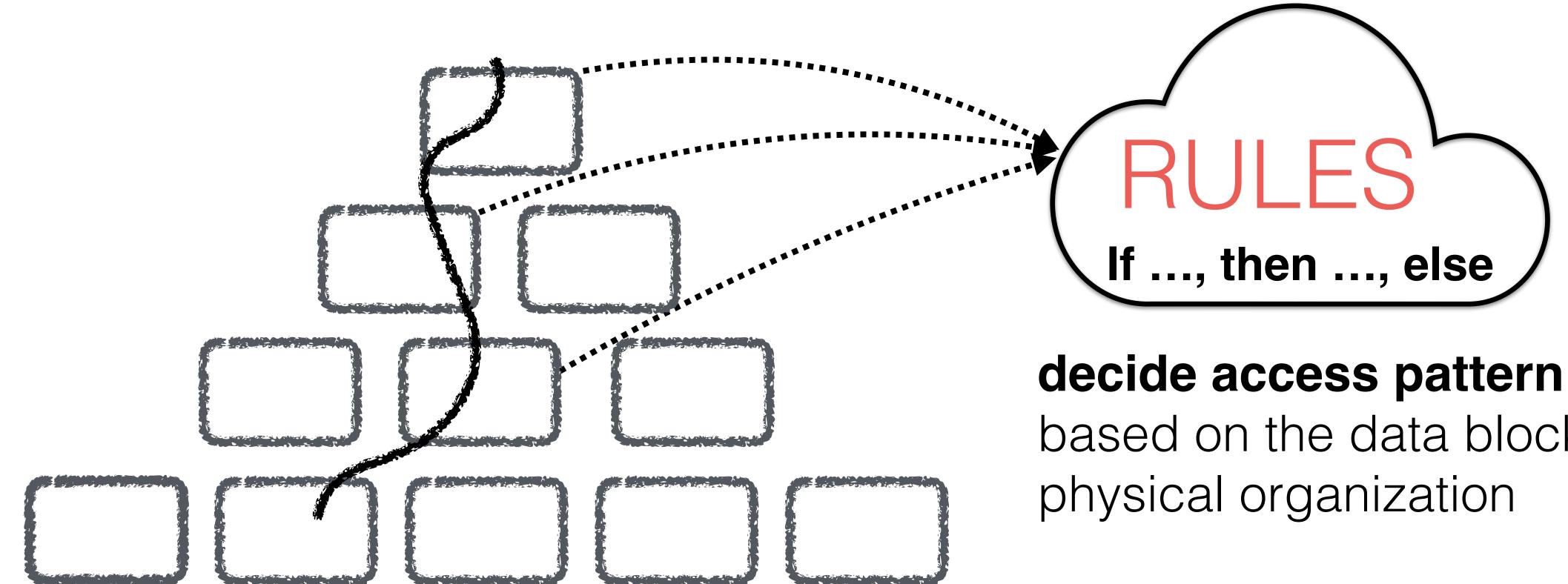
# DESIGN SPACE OF POSSIBLE STORAGE LAYOUTS





# ALGORITHM & COST SYNTHESIS







based on the data block's

### sorted keys columnar layout



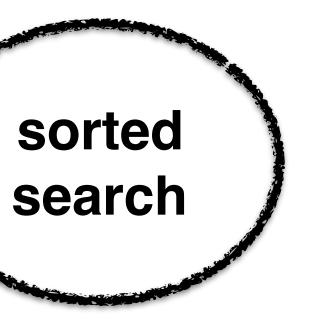
### sorted keys columnar layout

-----

- TOP ALL AND A







# DEPENDS ON HARDWARE ENGINEERING

### sorted keys columnar layout

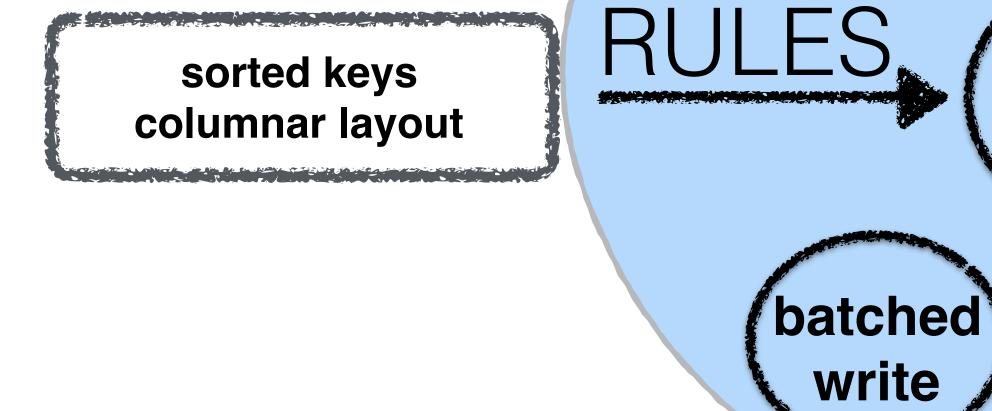




binary search1 binary search2 interpolation search1 interpolation search2 using new SIMD instruction X

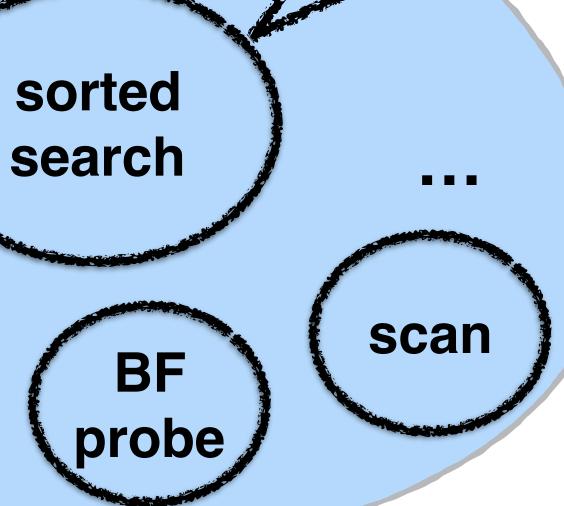
sorted search







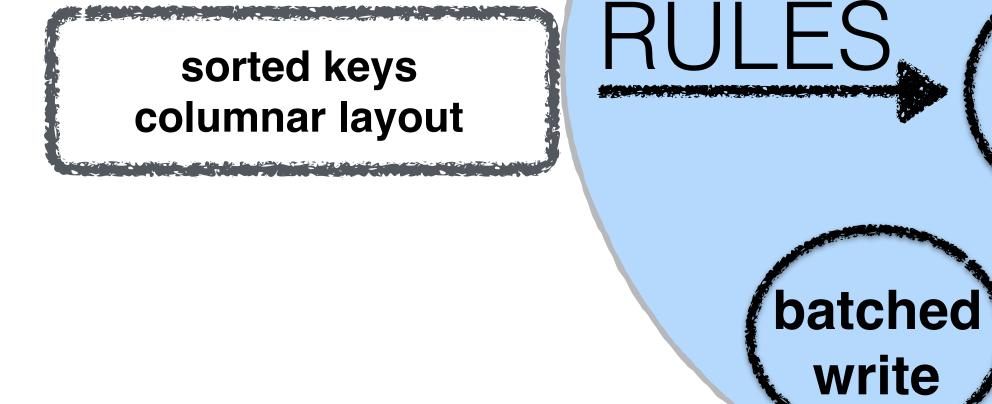
binary search1 binary search2 interpolation search1 interpolation search2 using new SIMD instruction X



# **Rules: access principles**









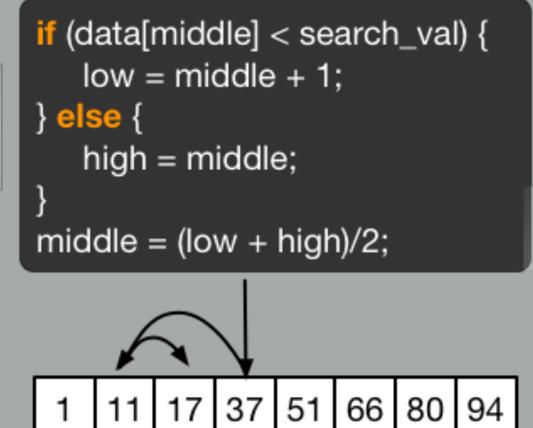
binary search1 code, binary search2 model interpolation search1 code, model interpolation search2 code, using new SIMD model instruction X Learning of fine-grained sorted search access patterns scan BF probe **Rules: access principles** 



# SYNTHESIS FROM LEARNED MODELS coding, modeling, generalized models, and a touch of ML

# **1. MINIMAL CODE**

e.g., binary search

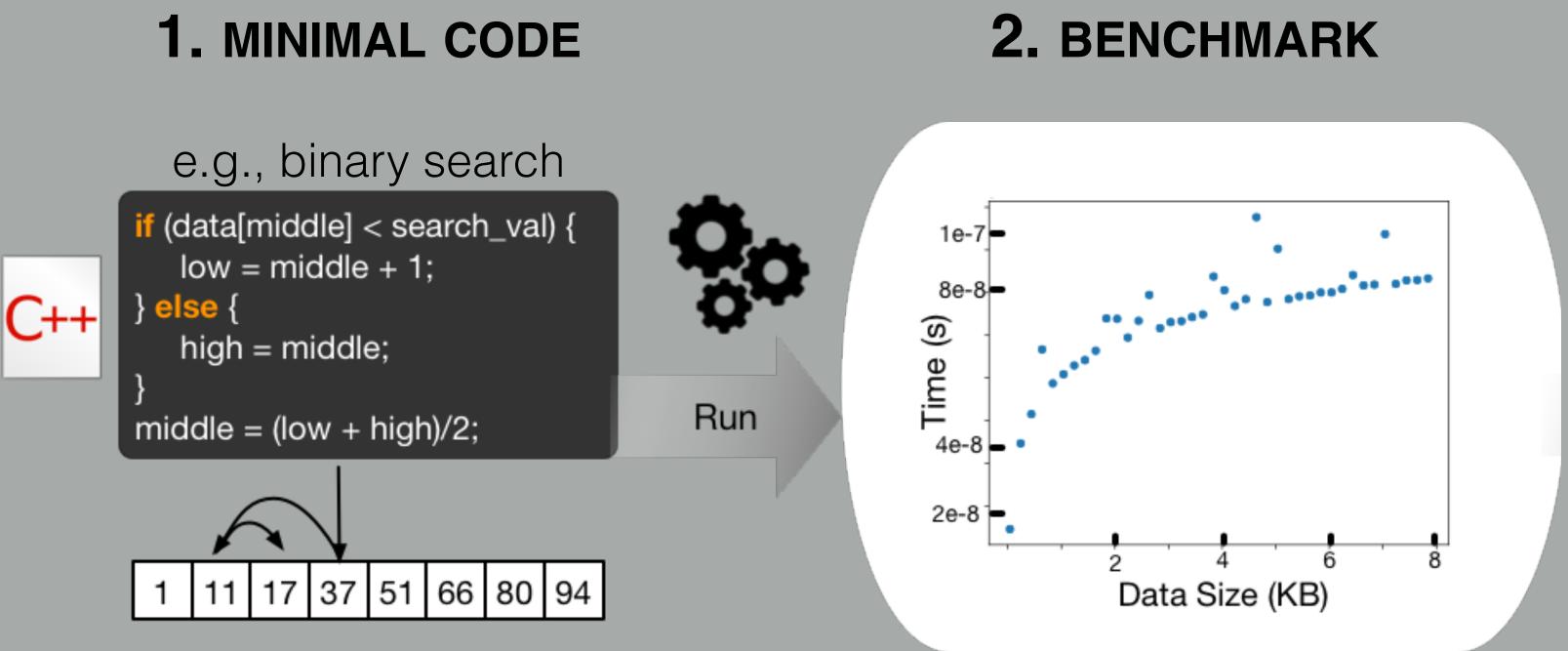




C++

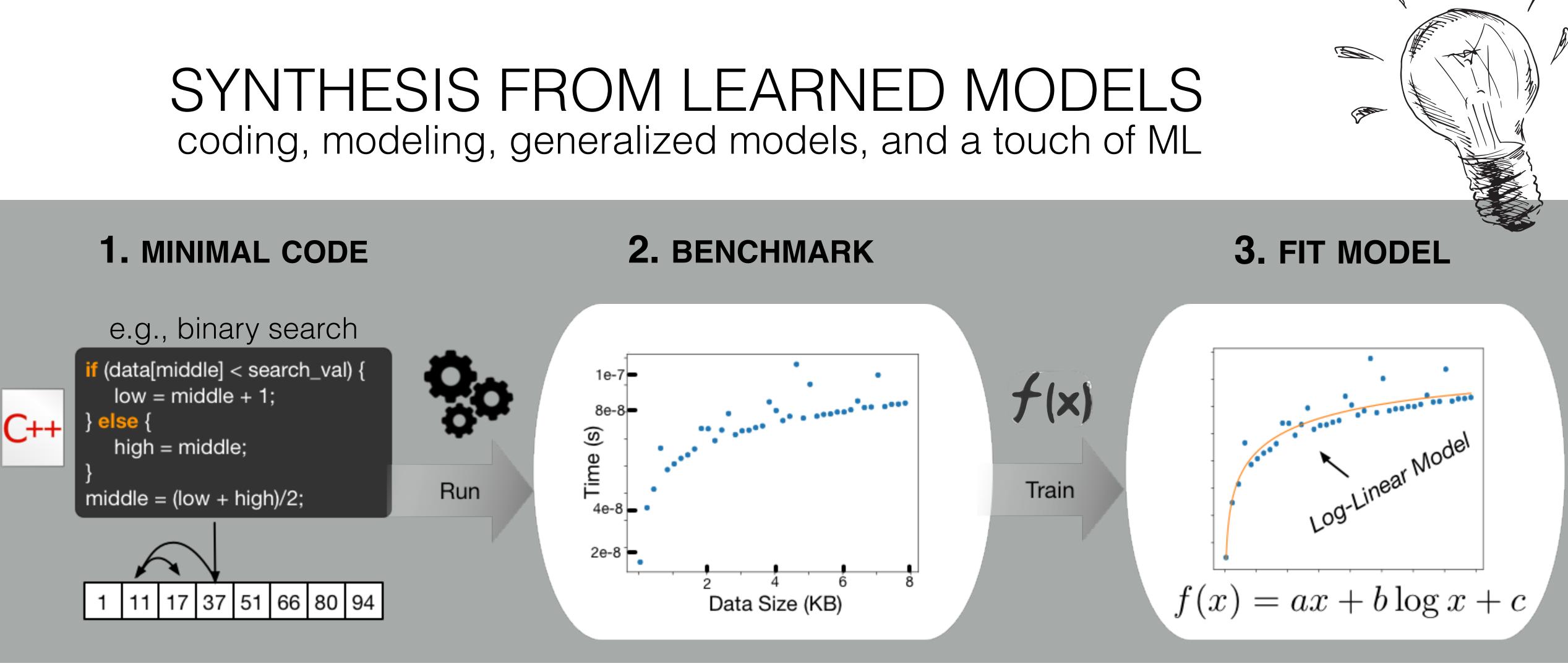


# SYNTHESIS FROM LEARNED MODELS coding, modeling, generalized models, and a touch of ML

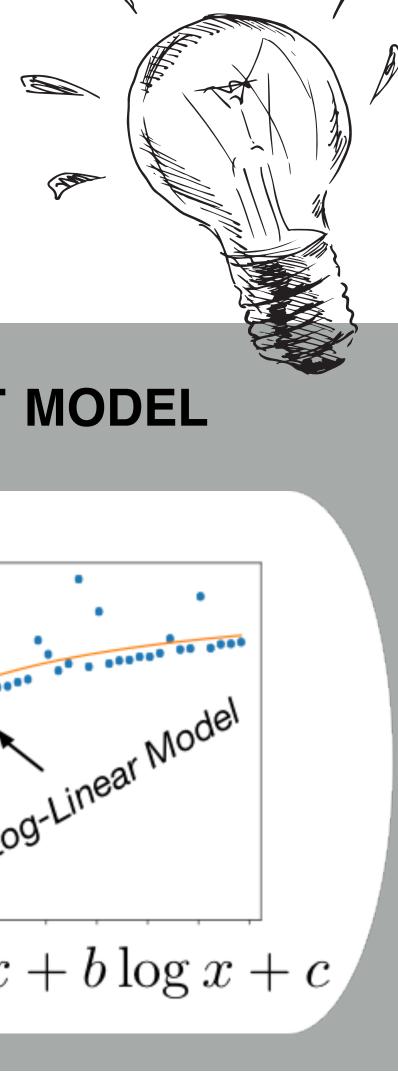


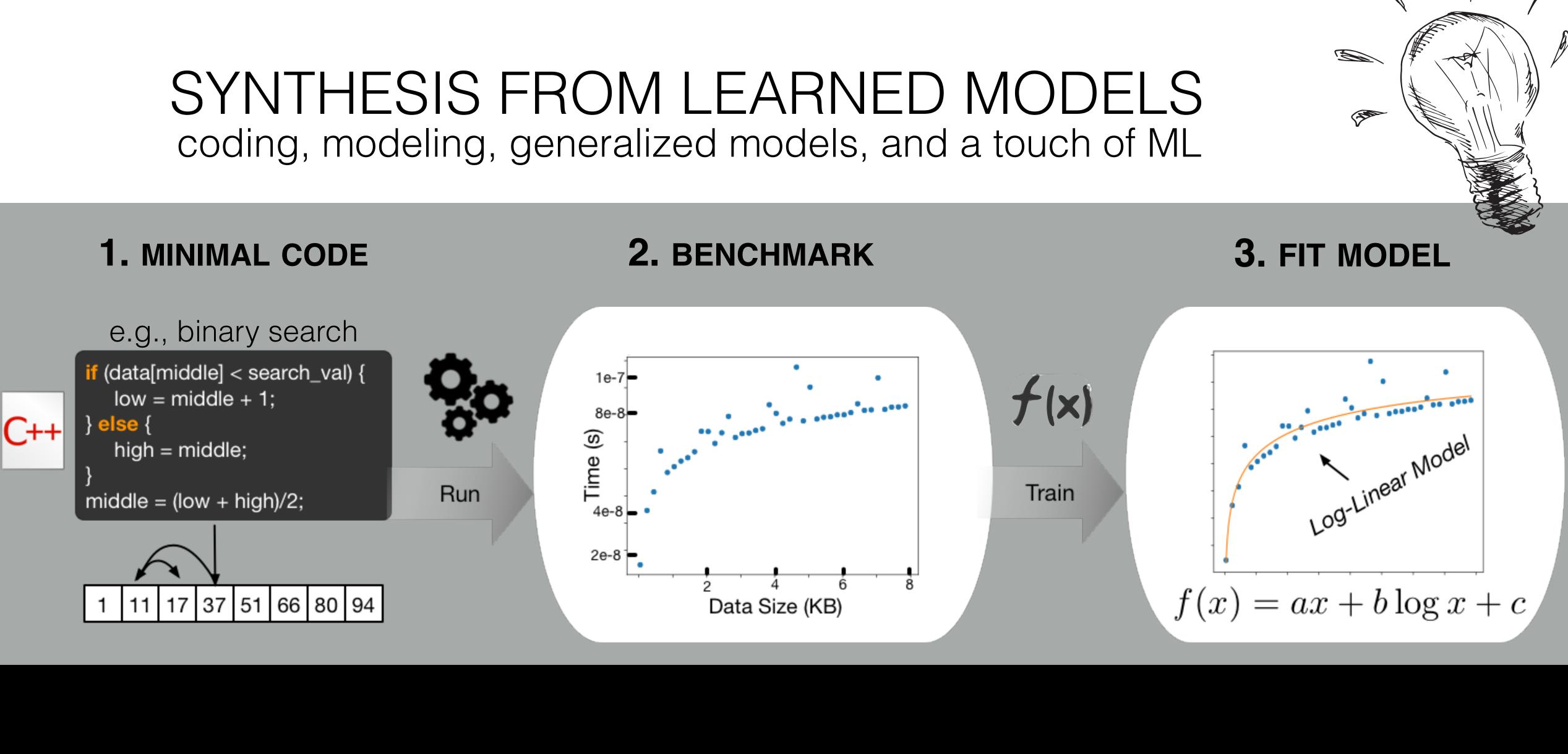








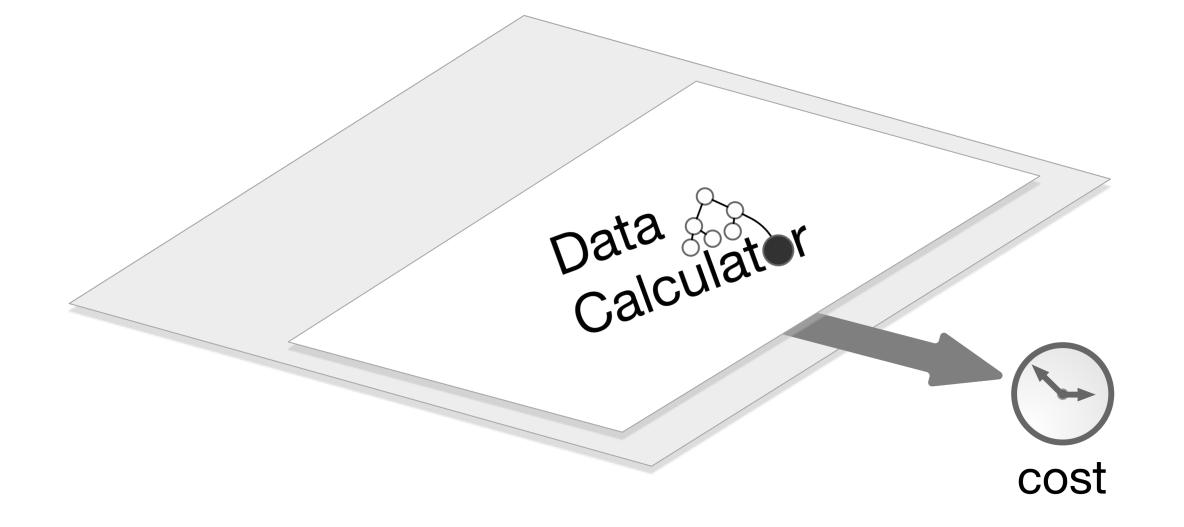




### FOLDING ALGORITHMIC, ENGINEERING, AND H/W, PROPERTIES INTO THE COEFFICIENTS



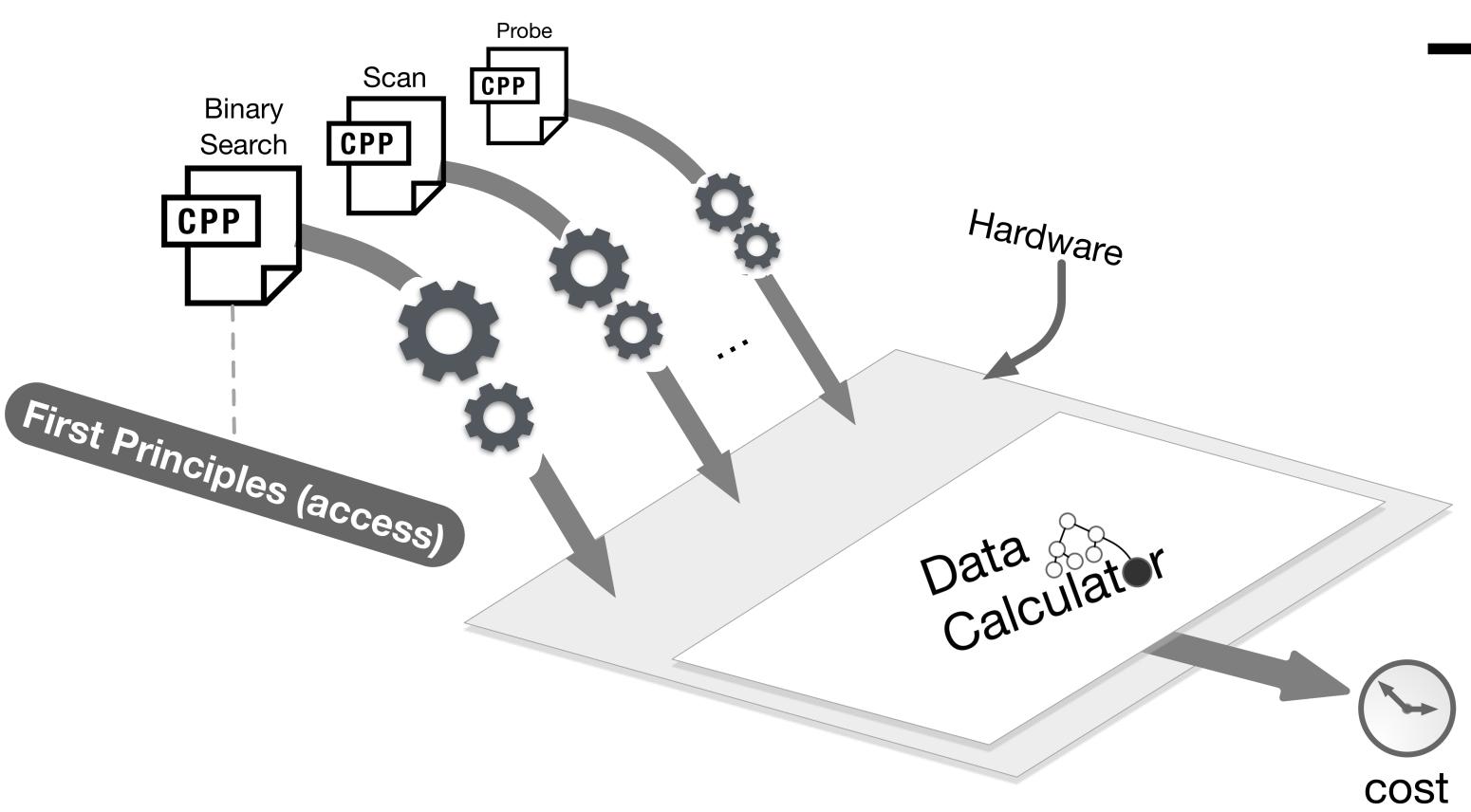






# TRAINING

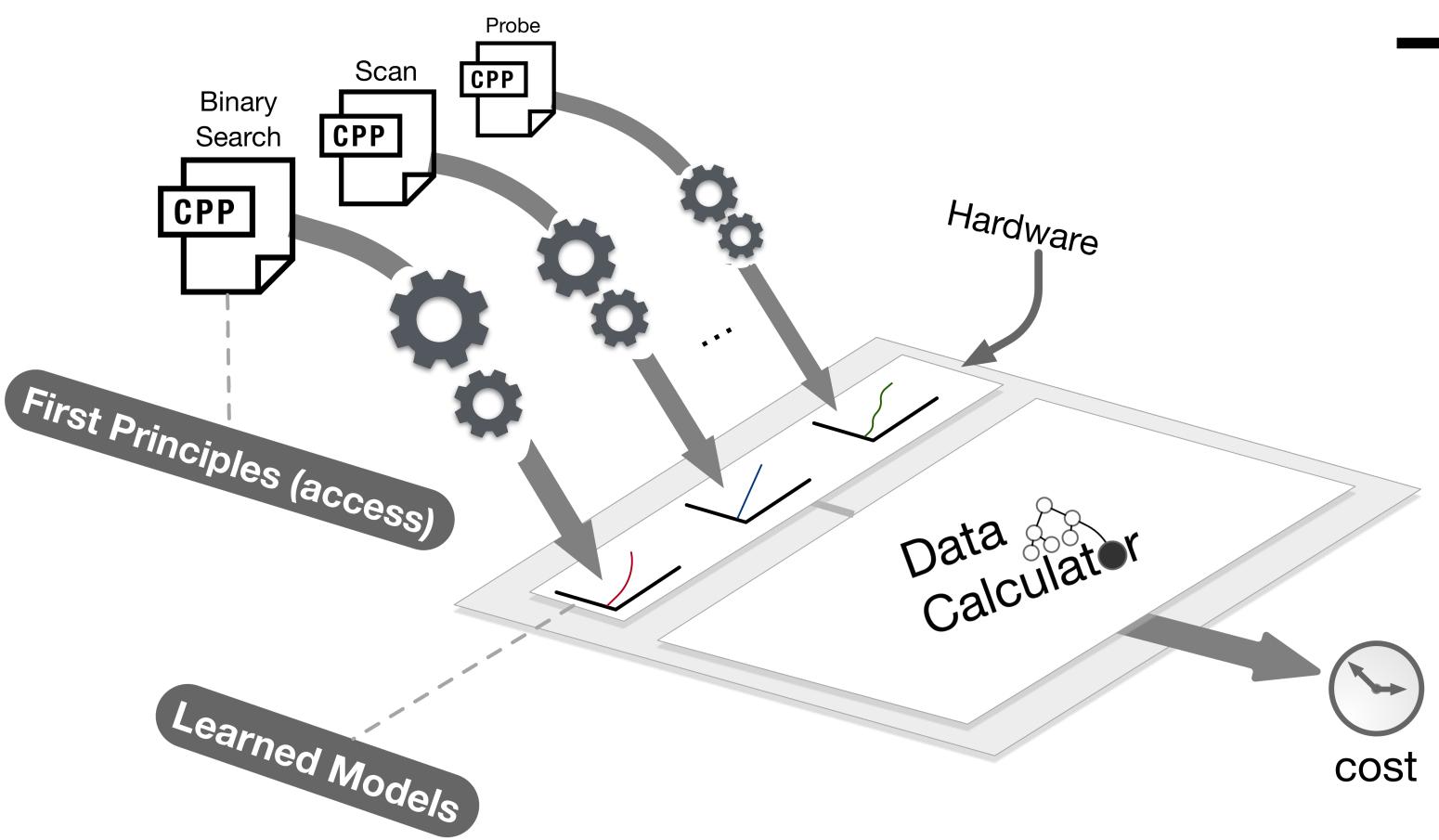






# TRAINING

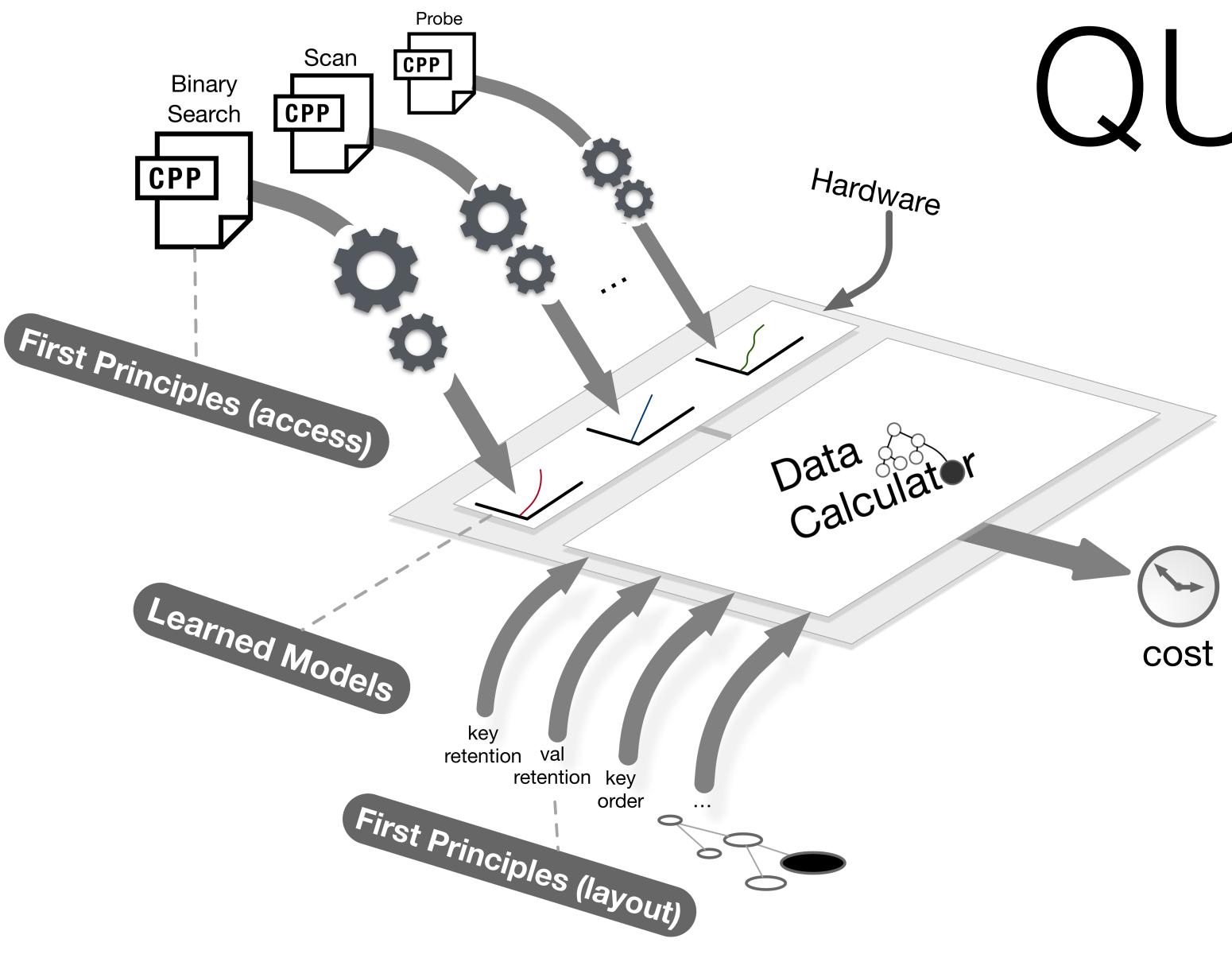






# TRAINING

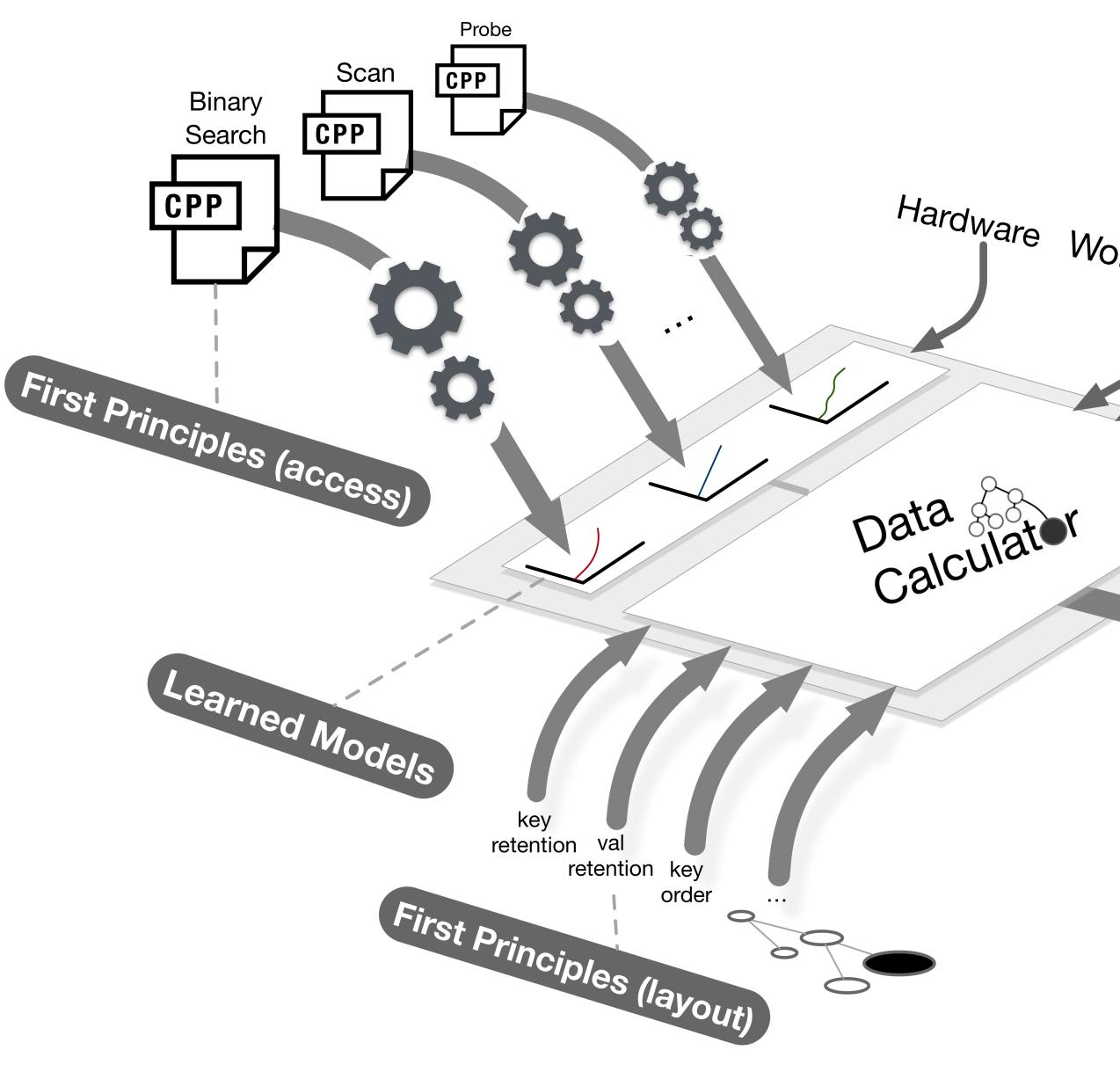






# QUEYRYING



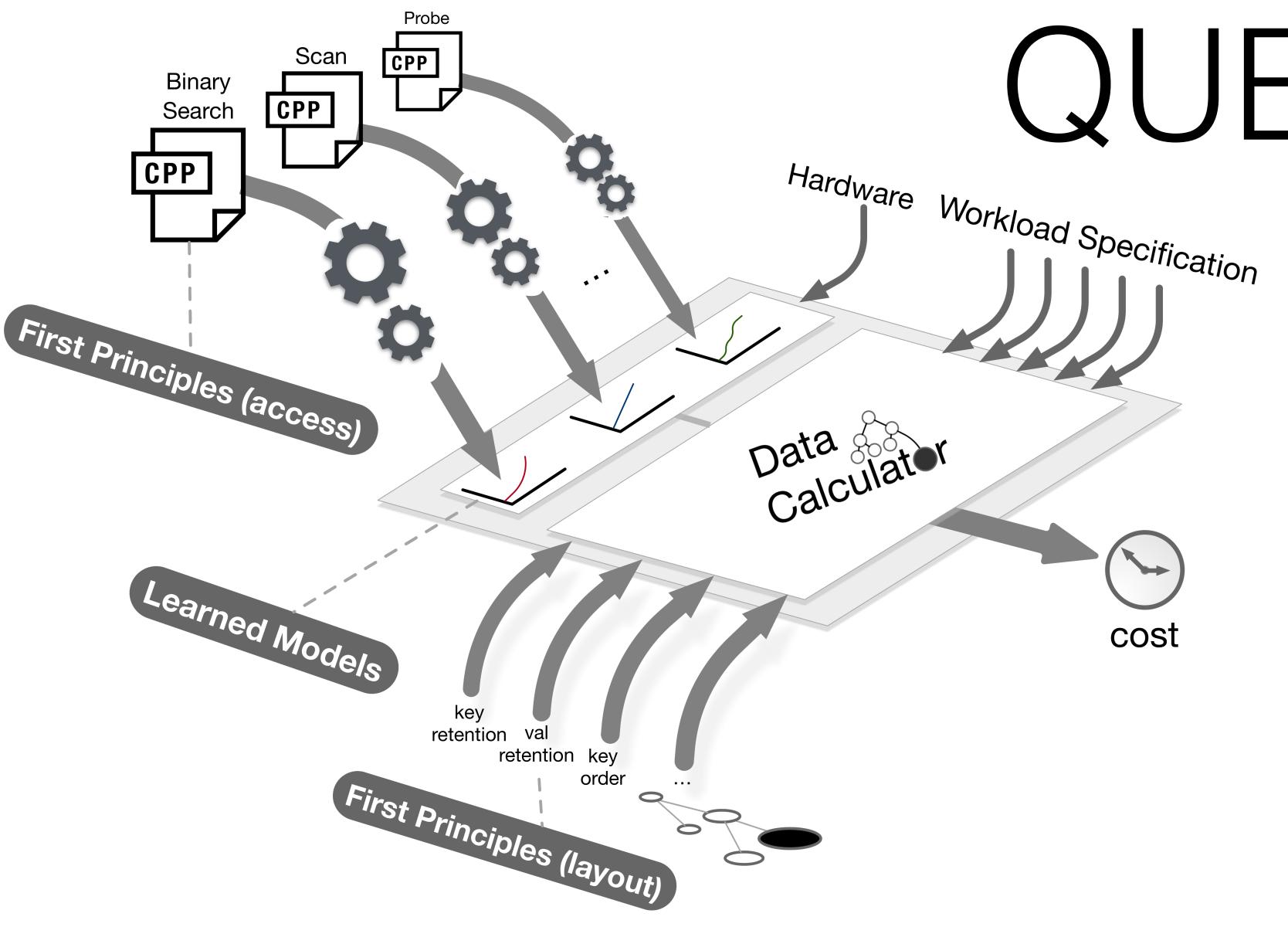




# QUEYRYING

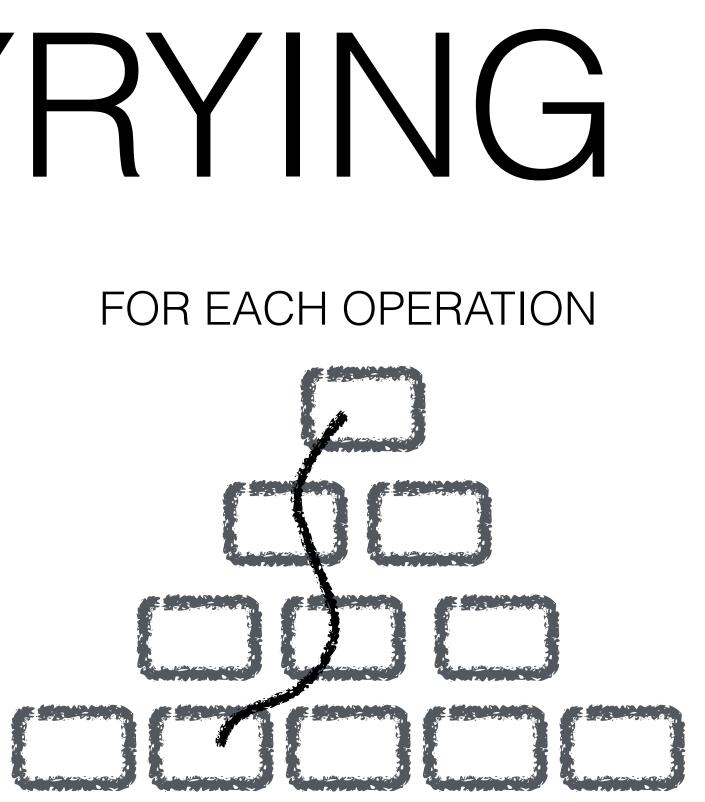
Hardware Workload Specification cost

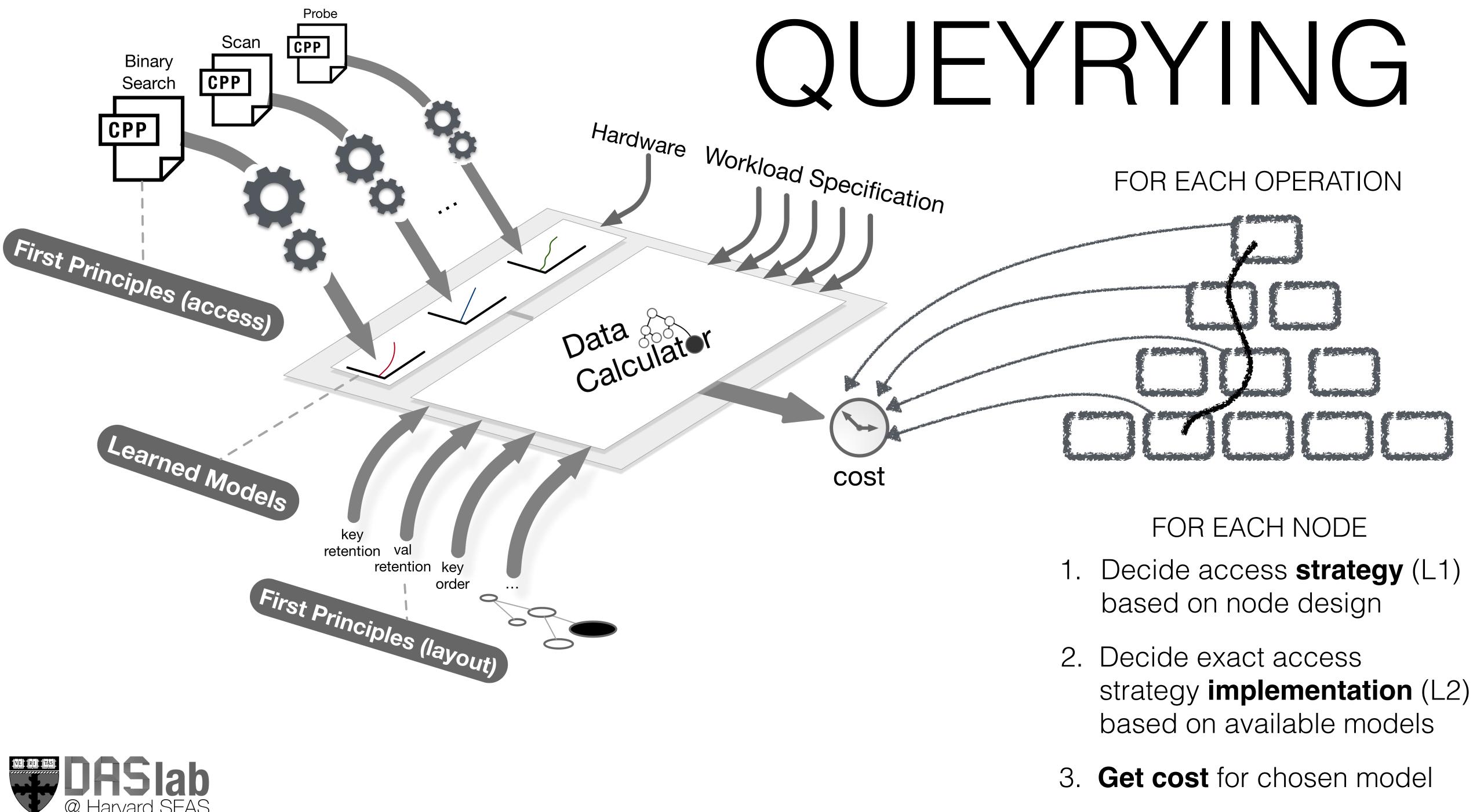






# QUEYRYING





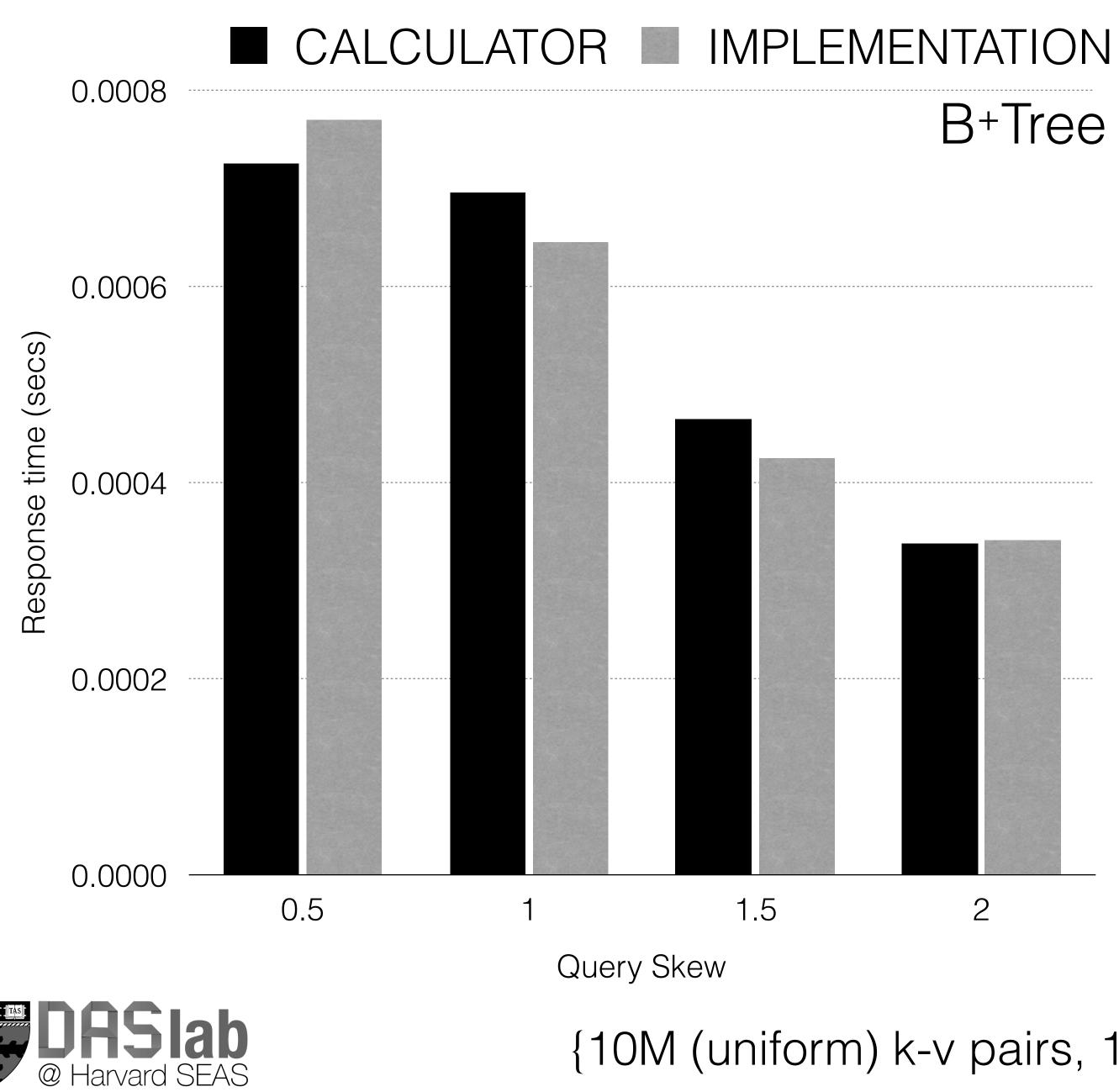


## CAN WE COMPUTE PERFORMANCE ACCURATELY?

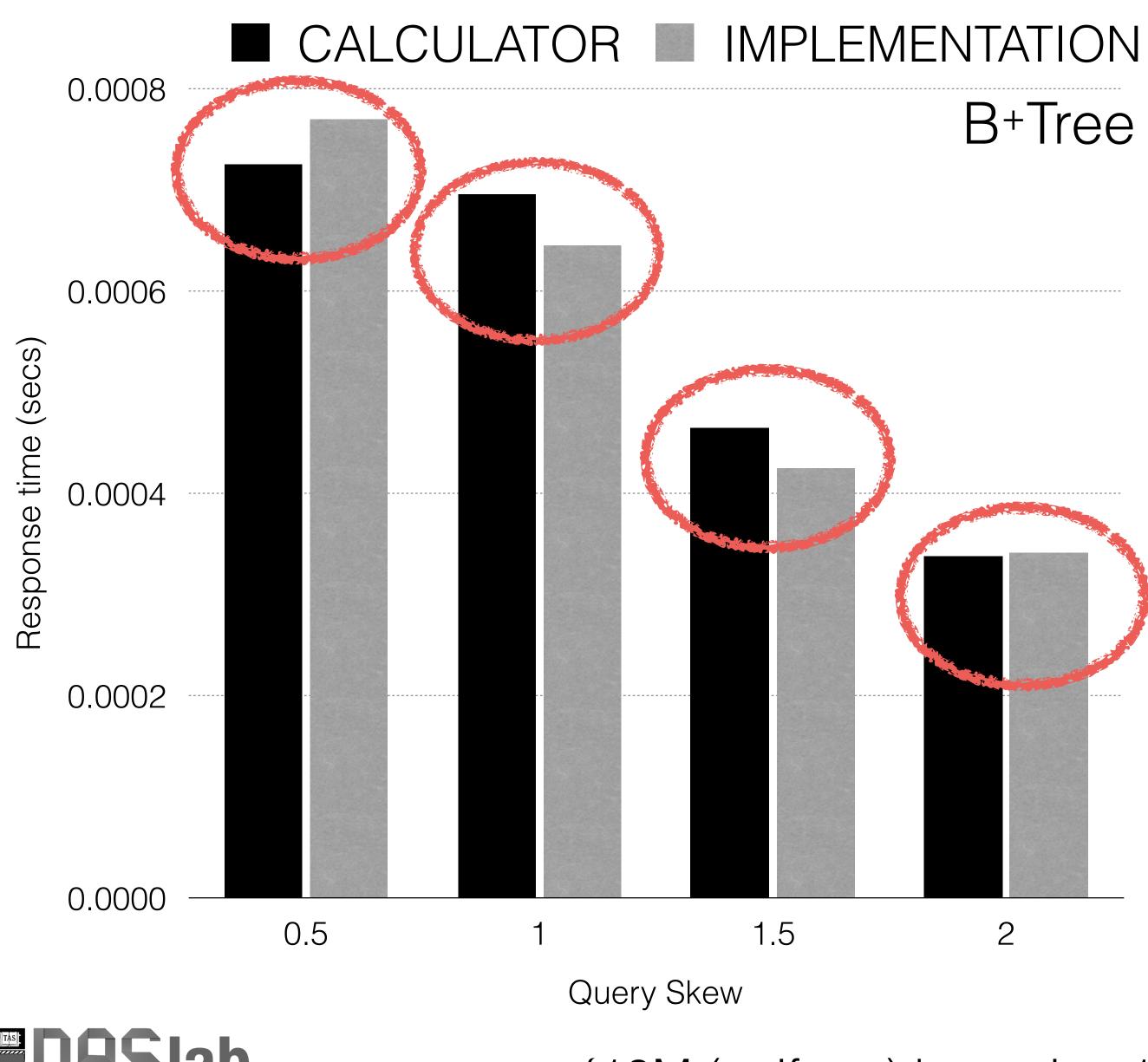


(same workload, hardware, data)





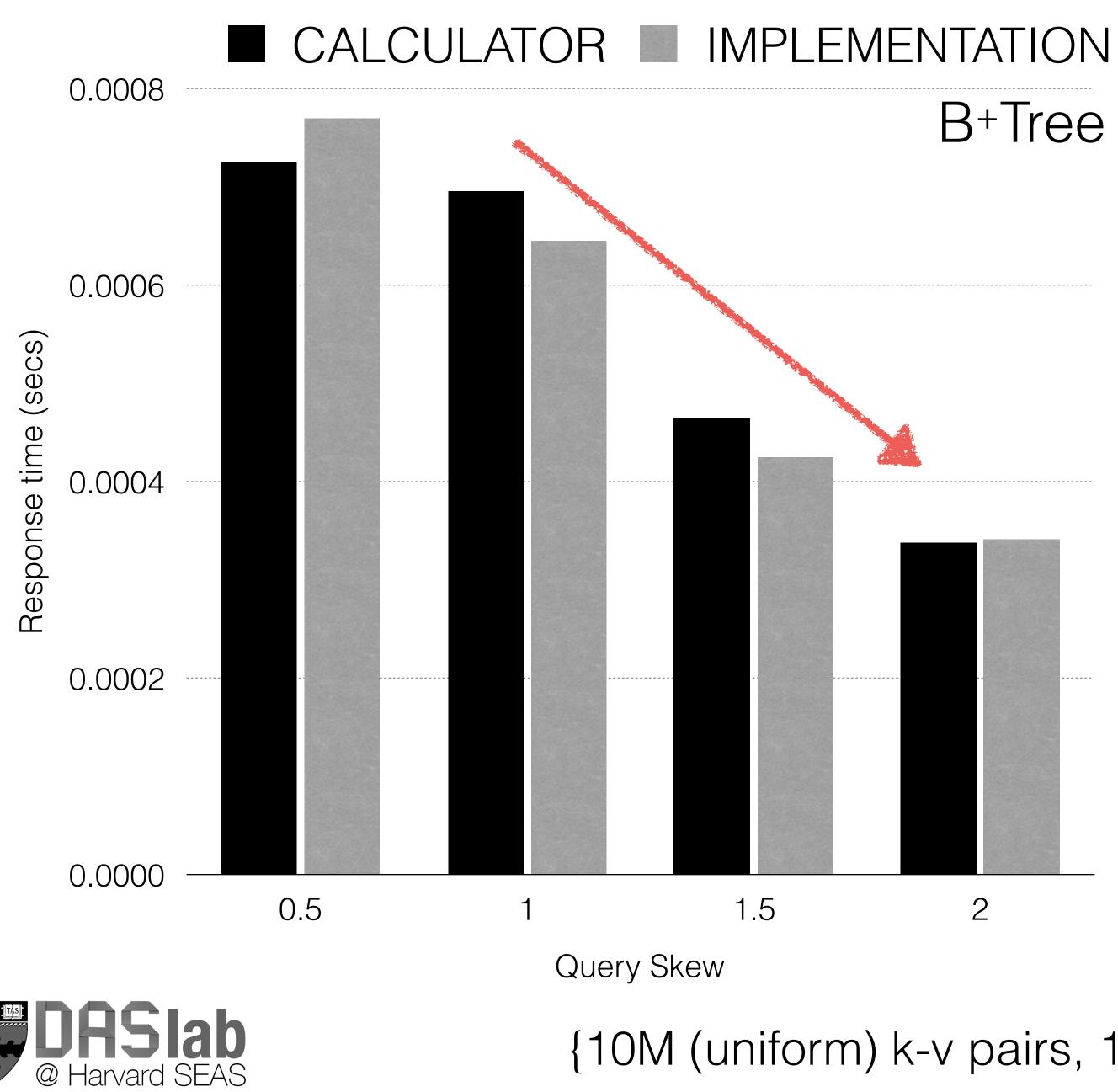
{10M (uniform) k-v pairs, 100 point queries (skewed)}



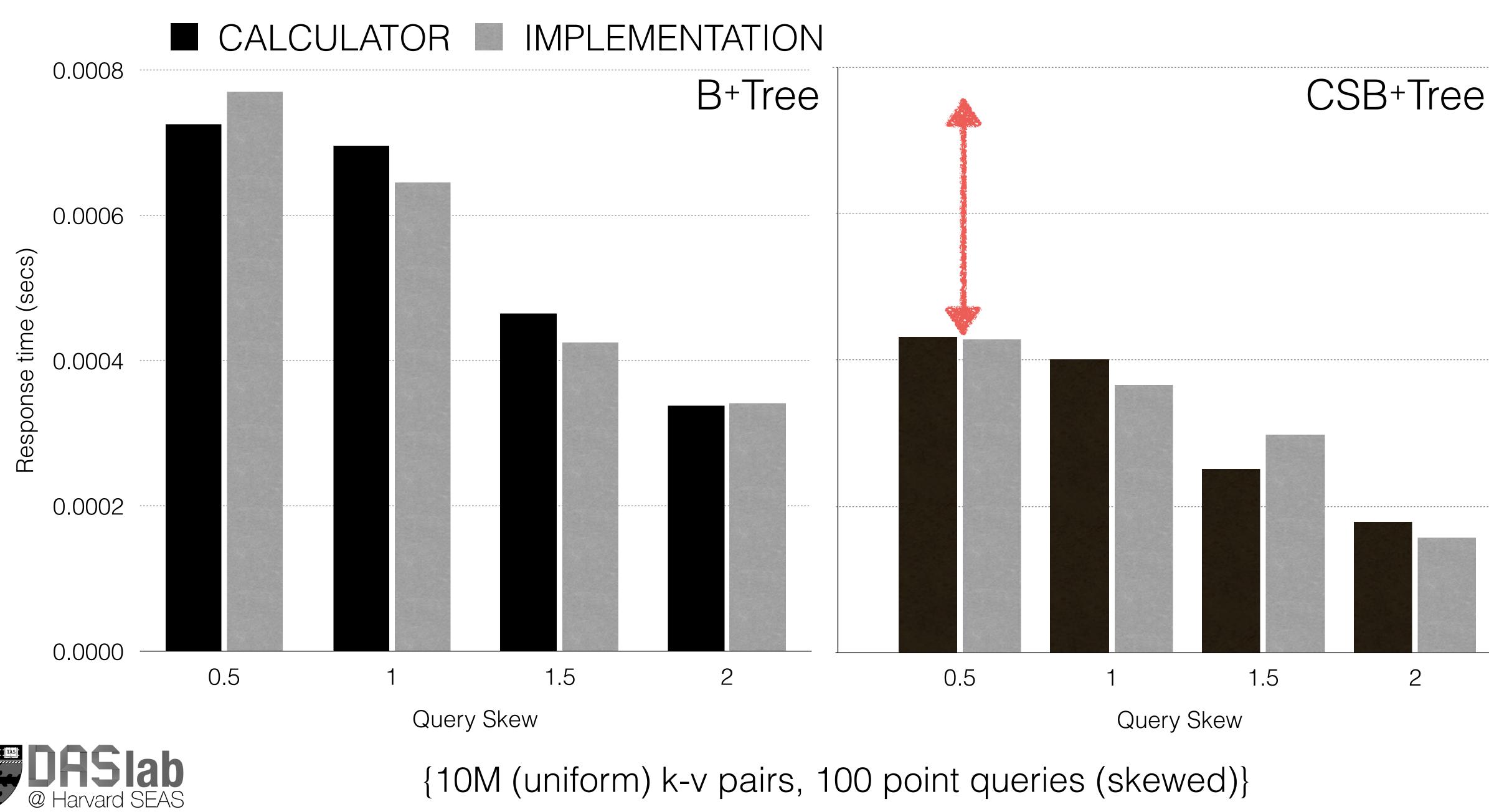


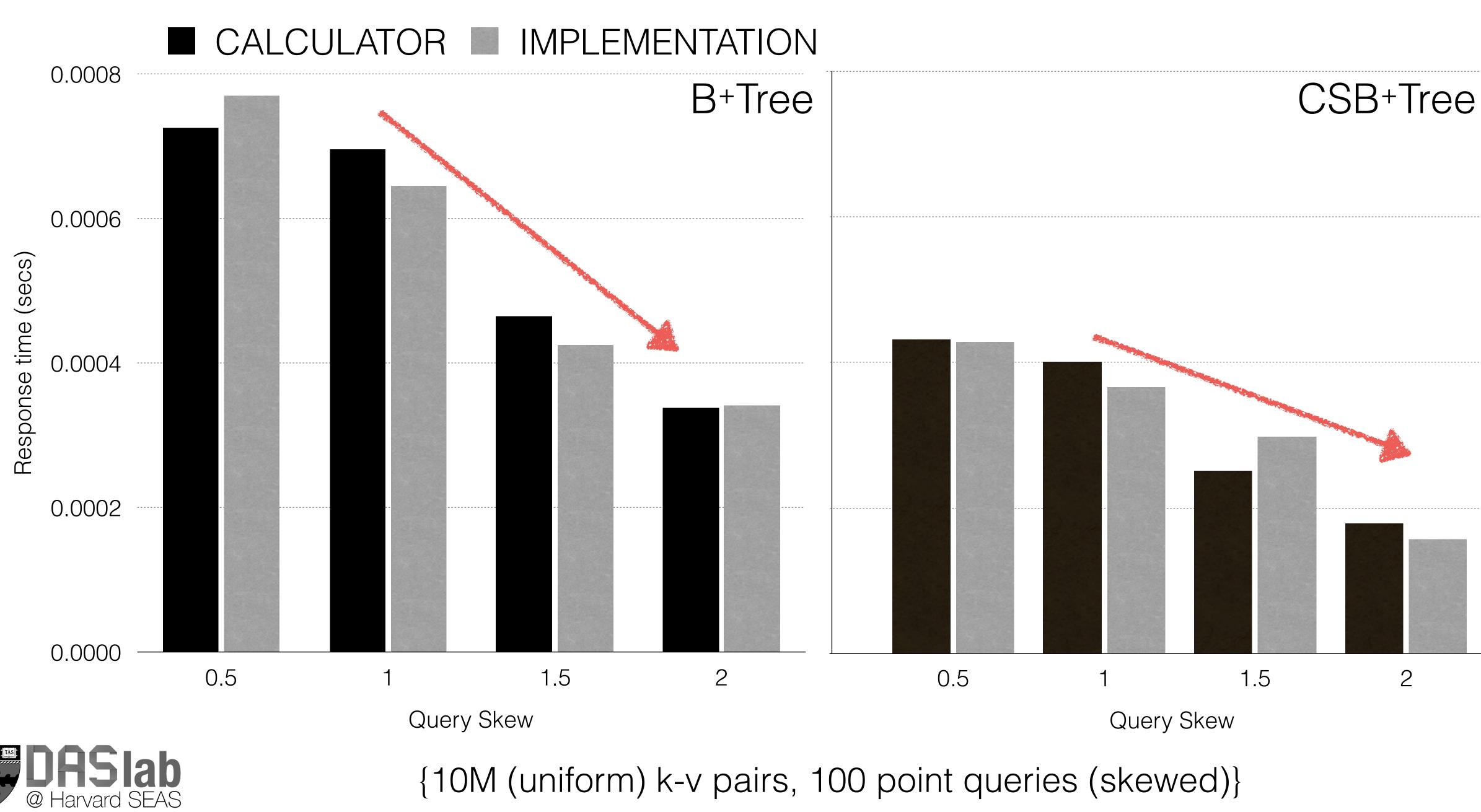
{10M (uniform) k-v pairs, 100 point queries (skewed)}

# B+Tree



{10M (uniform) k-v pairs, 100 point queries (skewed)}

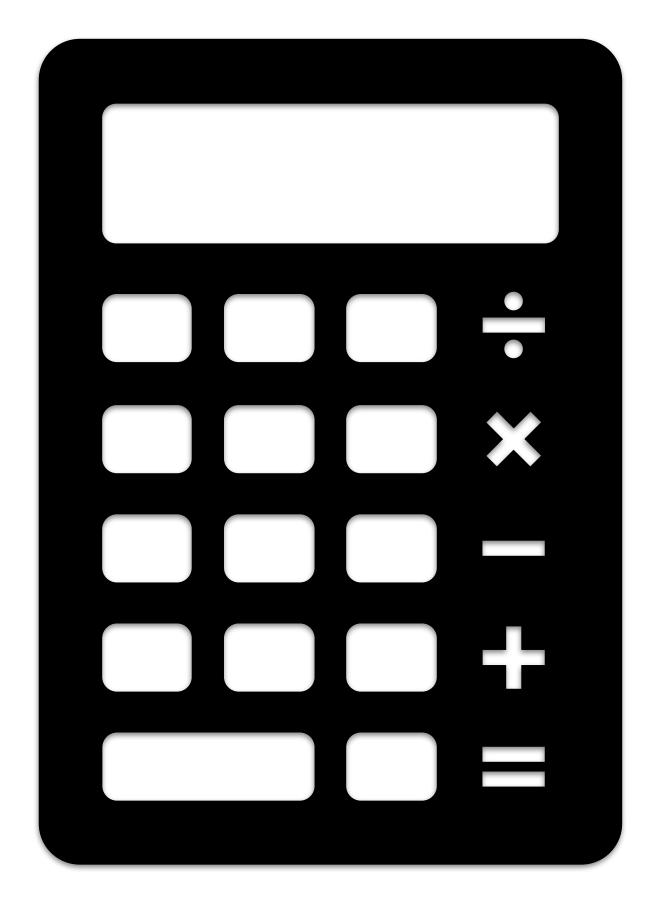


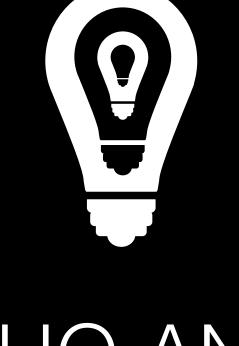


# DESIGN SPACE

## COST SYNTHESIS

# WHO AND HOW TO USE





# WHO AND HOW TO USE

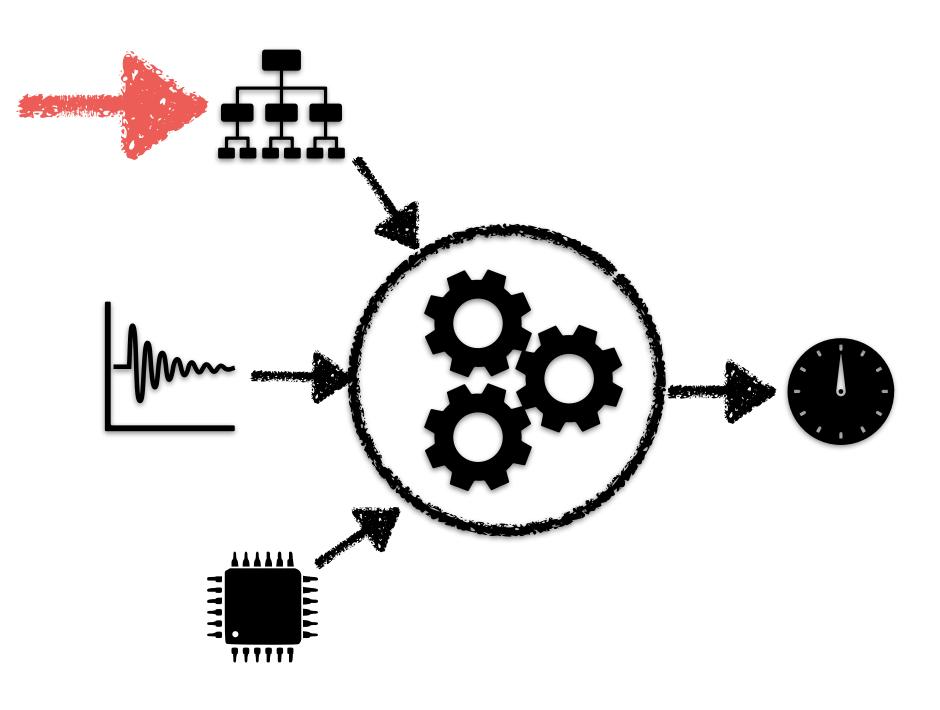


# "IMAGINE" DESIGNS



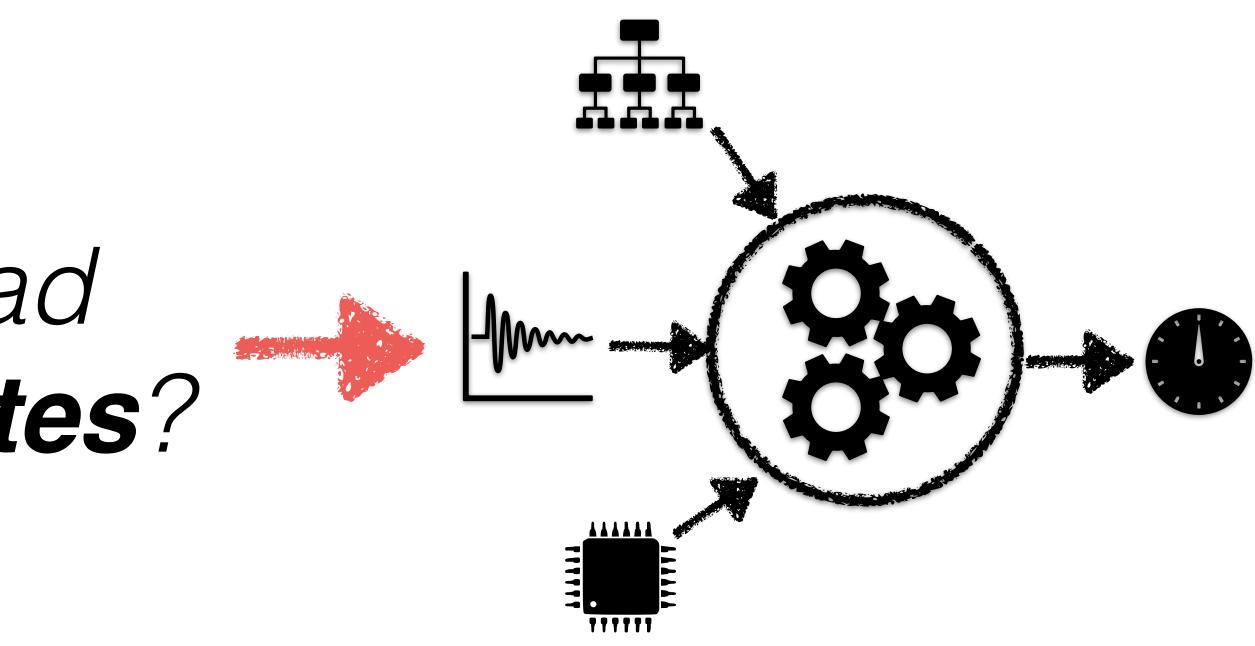
# What-if we **add bloom filters** in the hash-table buckets?

# ~20 SECONDS (workload:10 Million entries, 100 queries)



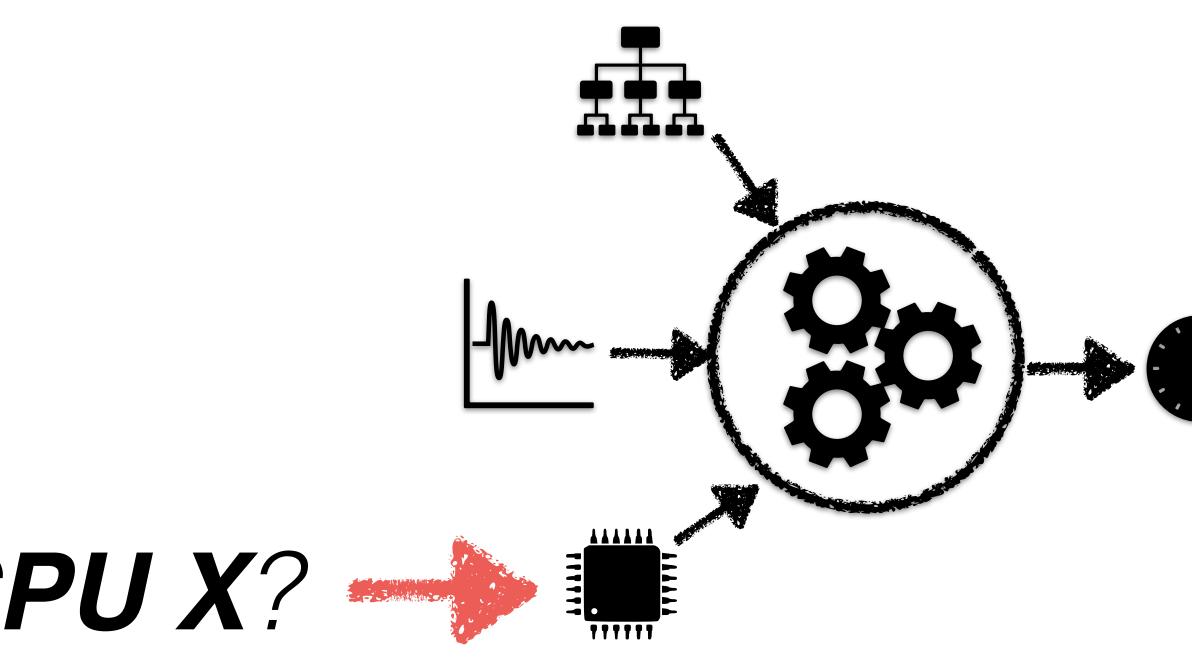
# What-if the workload changes to **90% writes**?

# ~20 SECONDS (workload:10 Million entries, 100 queries)

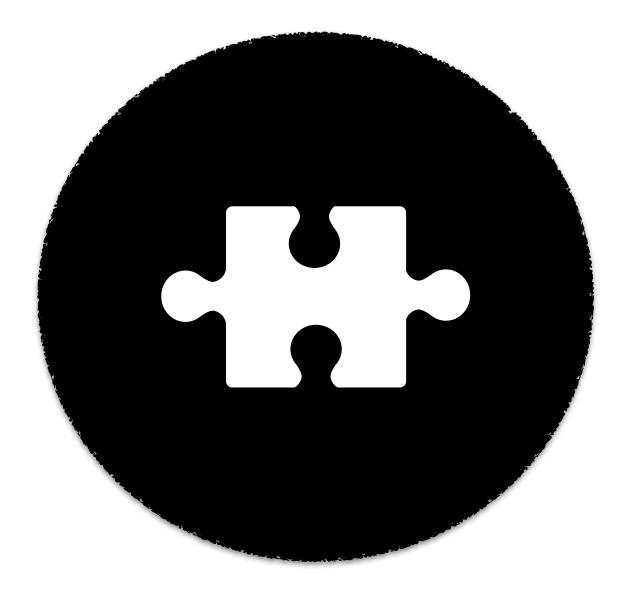


# What-if we buy faster CPUX?

# ~20 SECONDS (workload:10 Million entries, 100 queries)







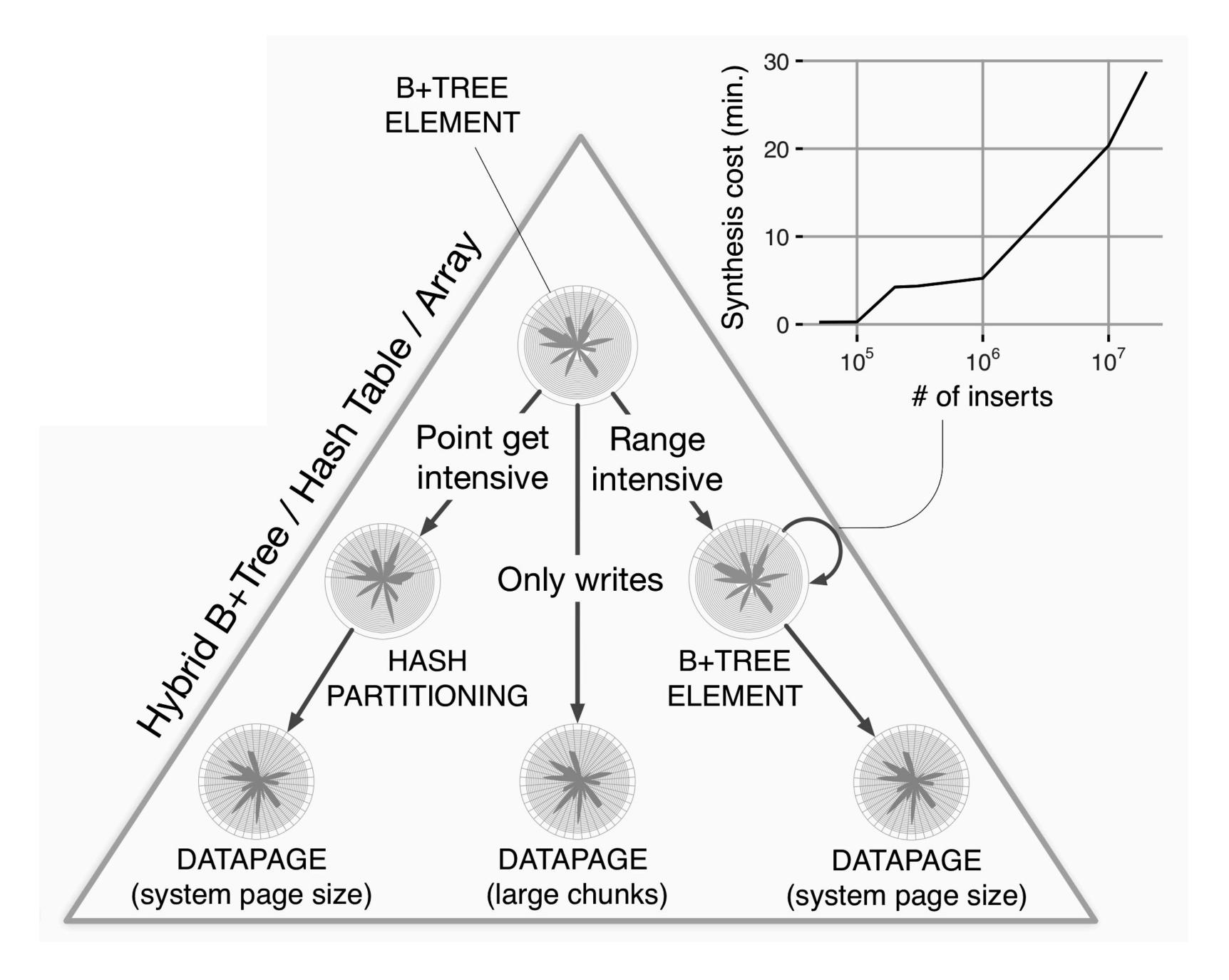
# auto design .



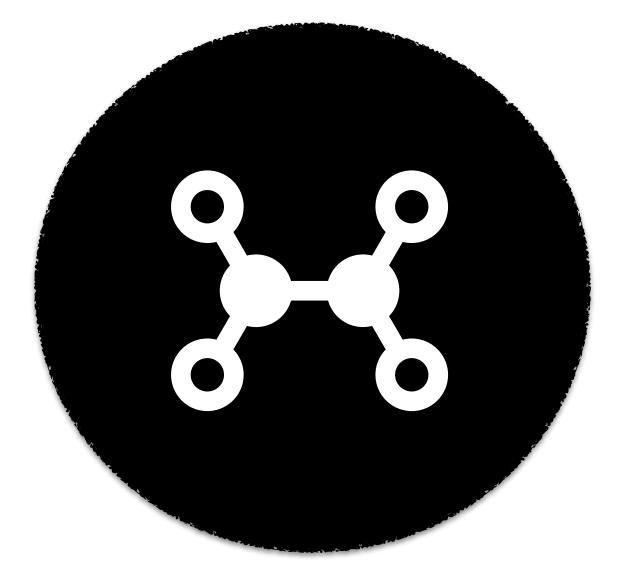
## dynamic programming genetic algorithms reinforcement learning











# **design\_continuums** UNIFY DESIGNS FOR FAST NAVIGATION





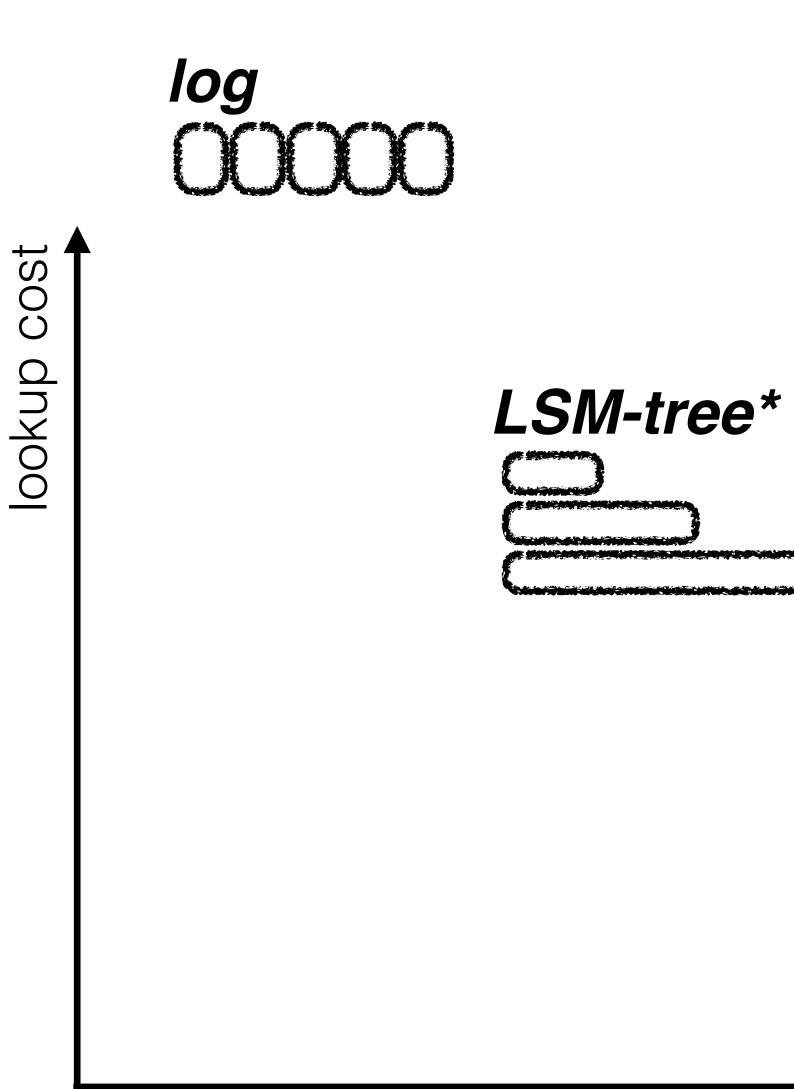




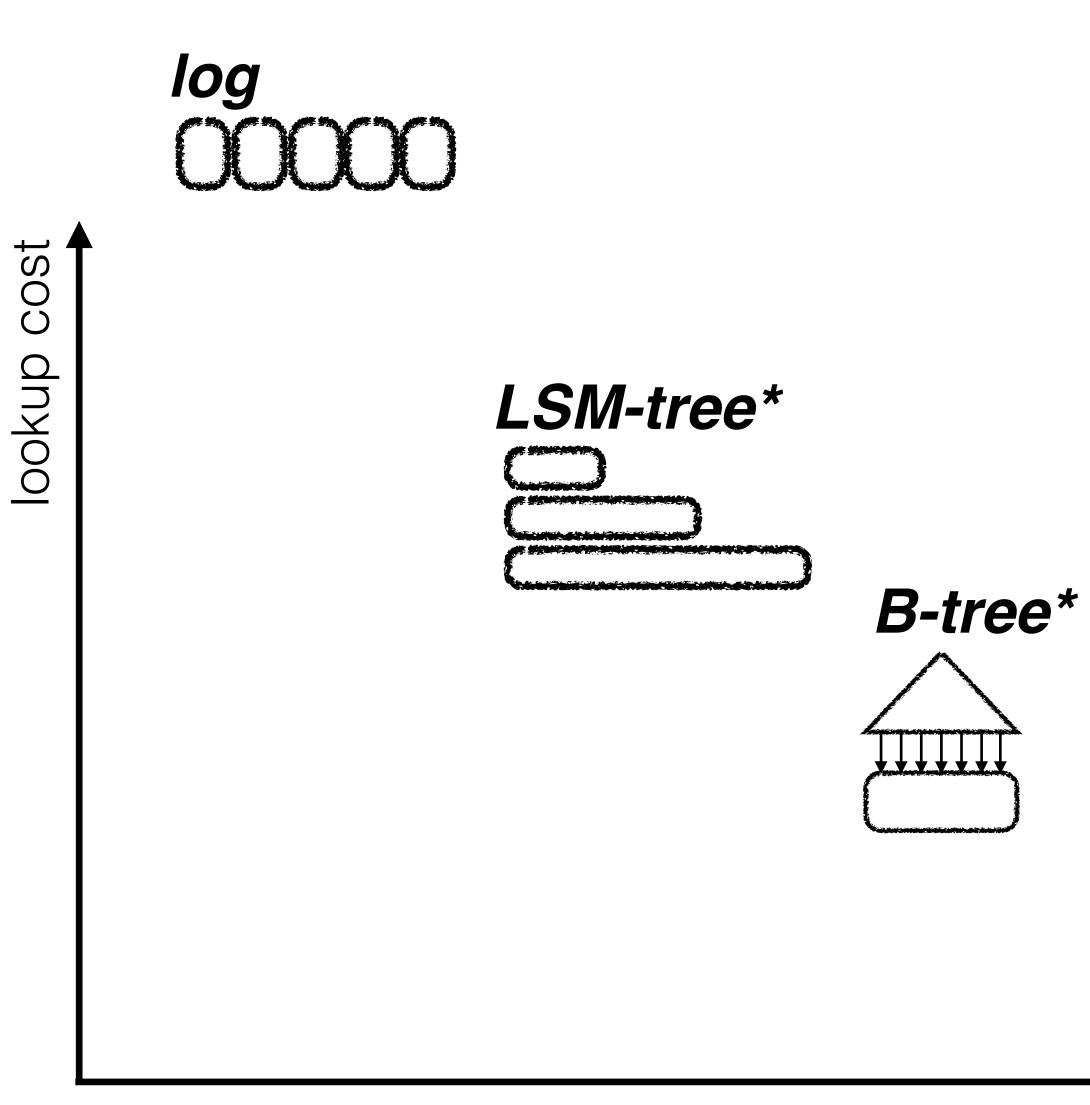
## *log* 00000

lookup cost

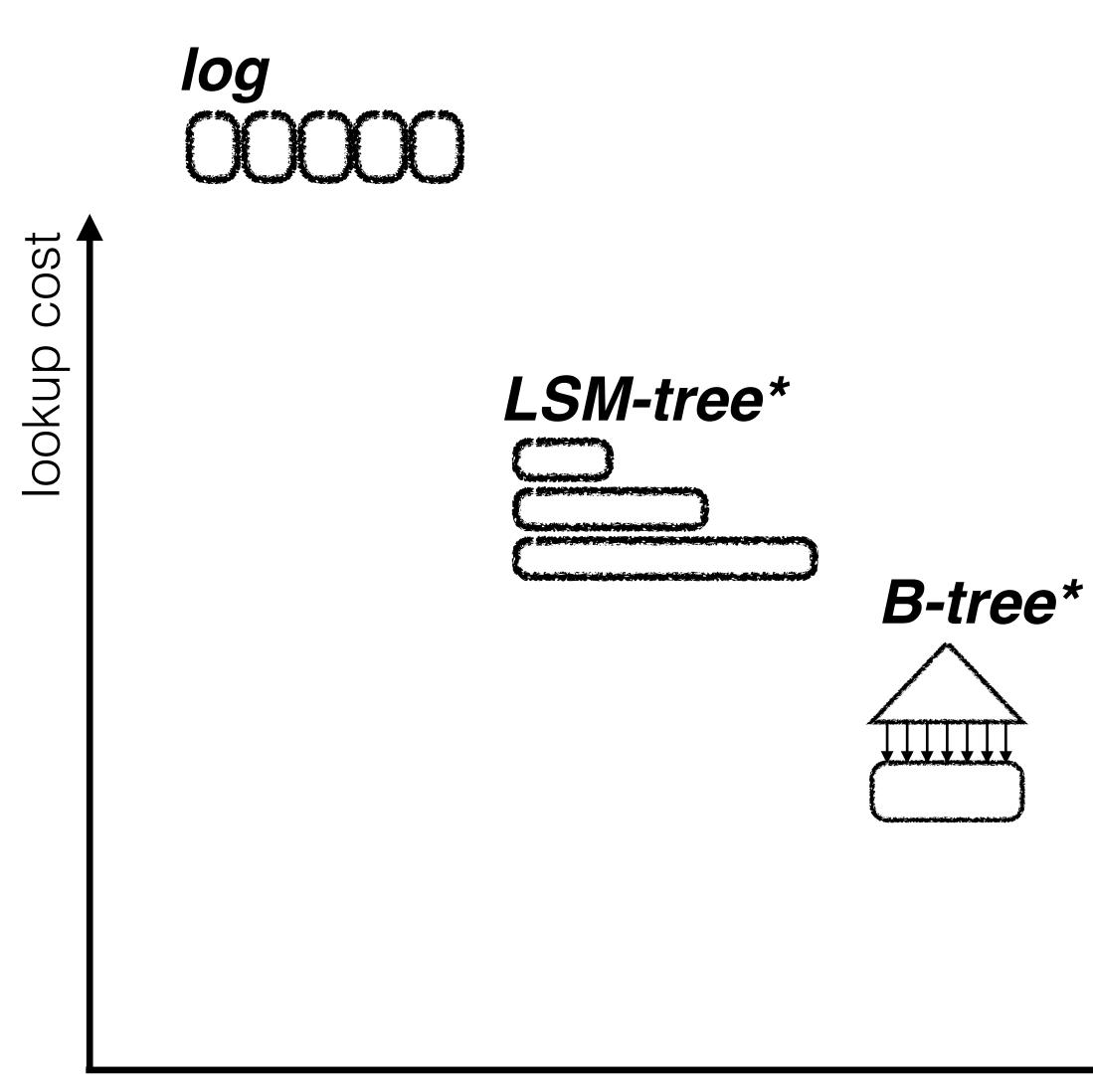






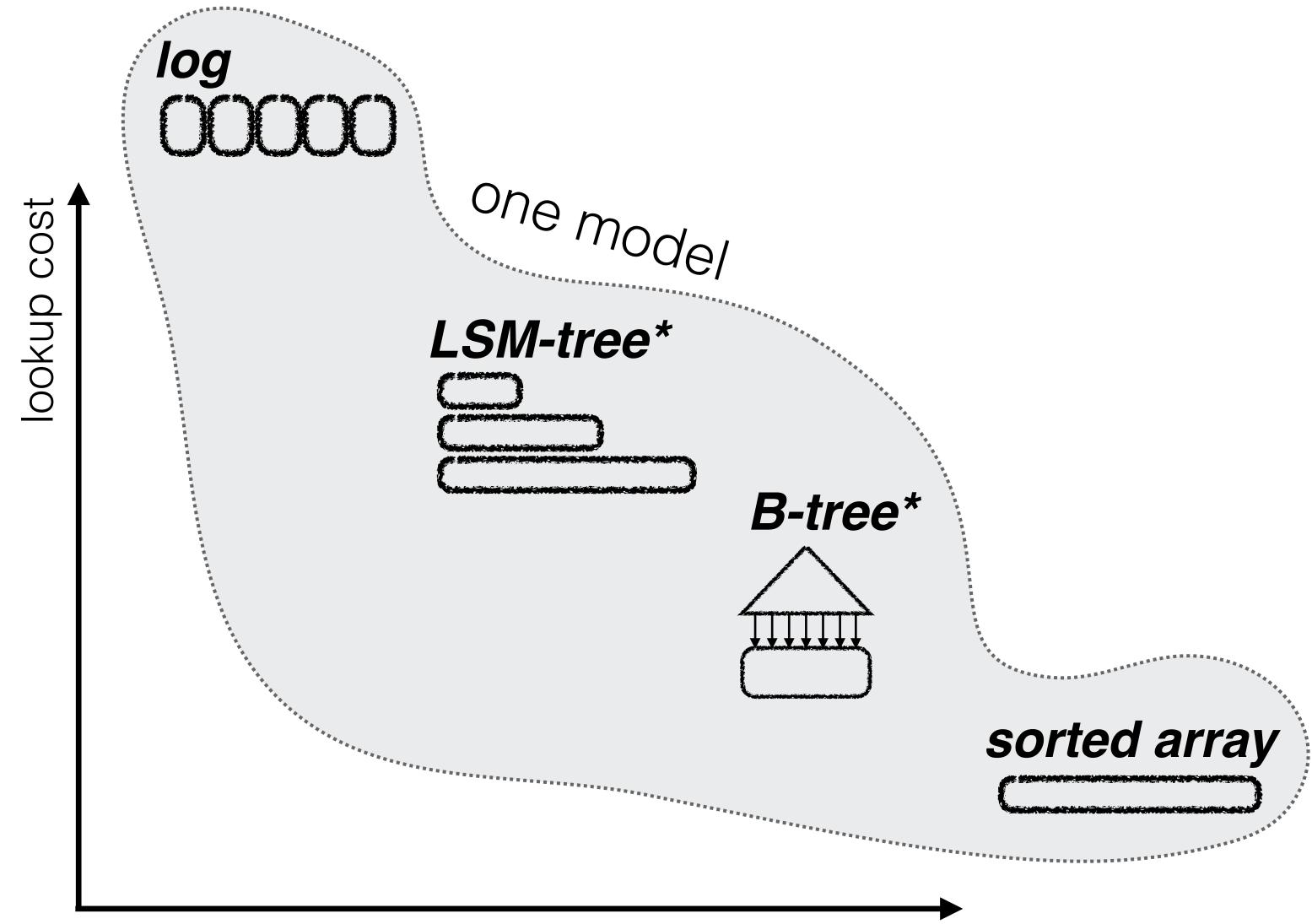




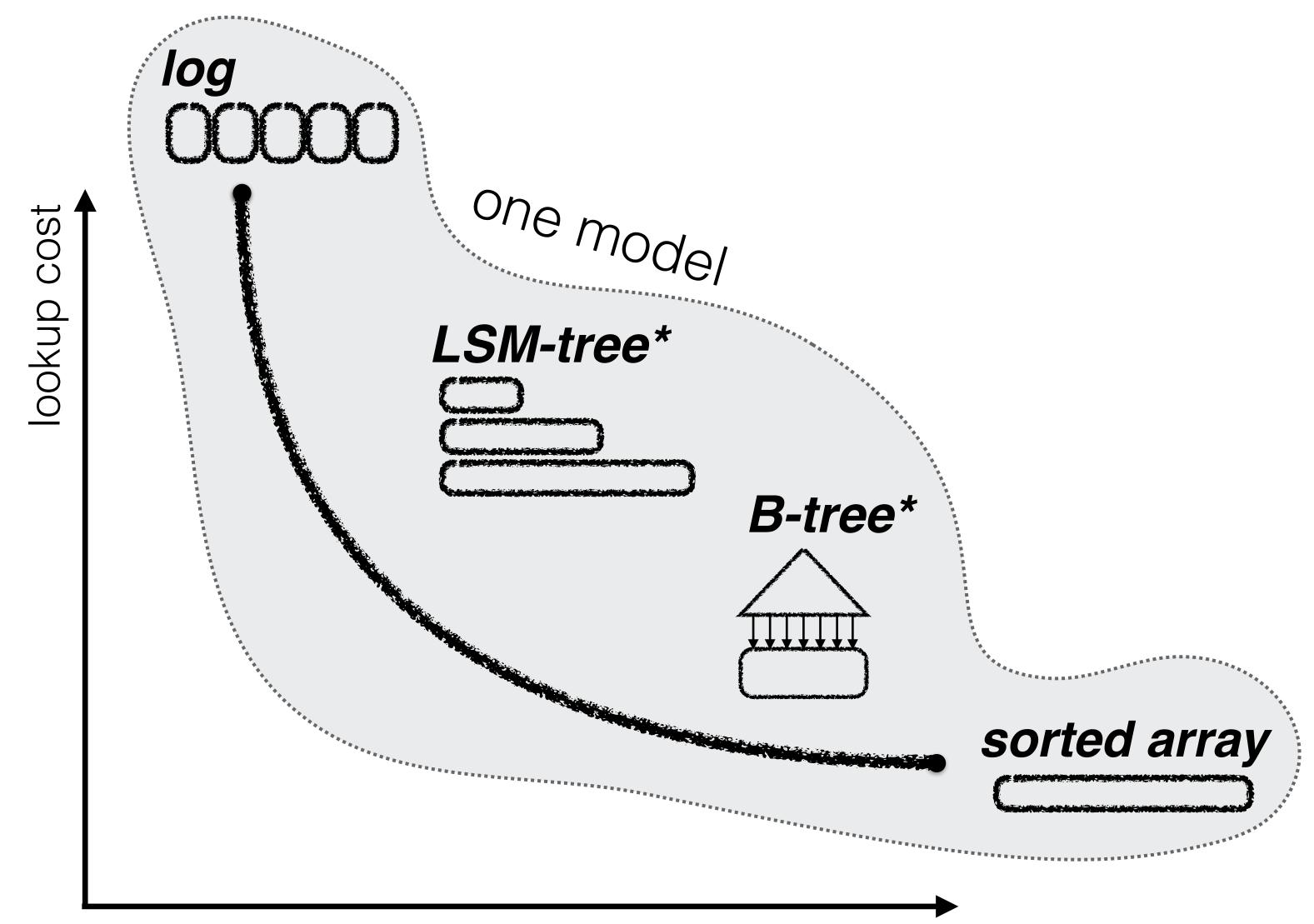




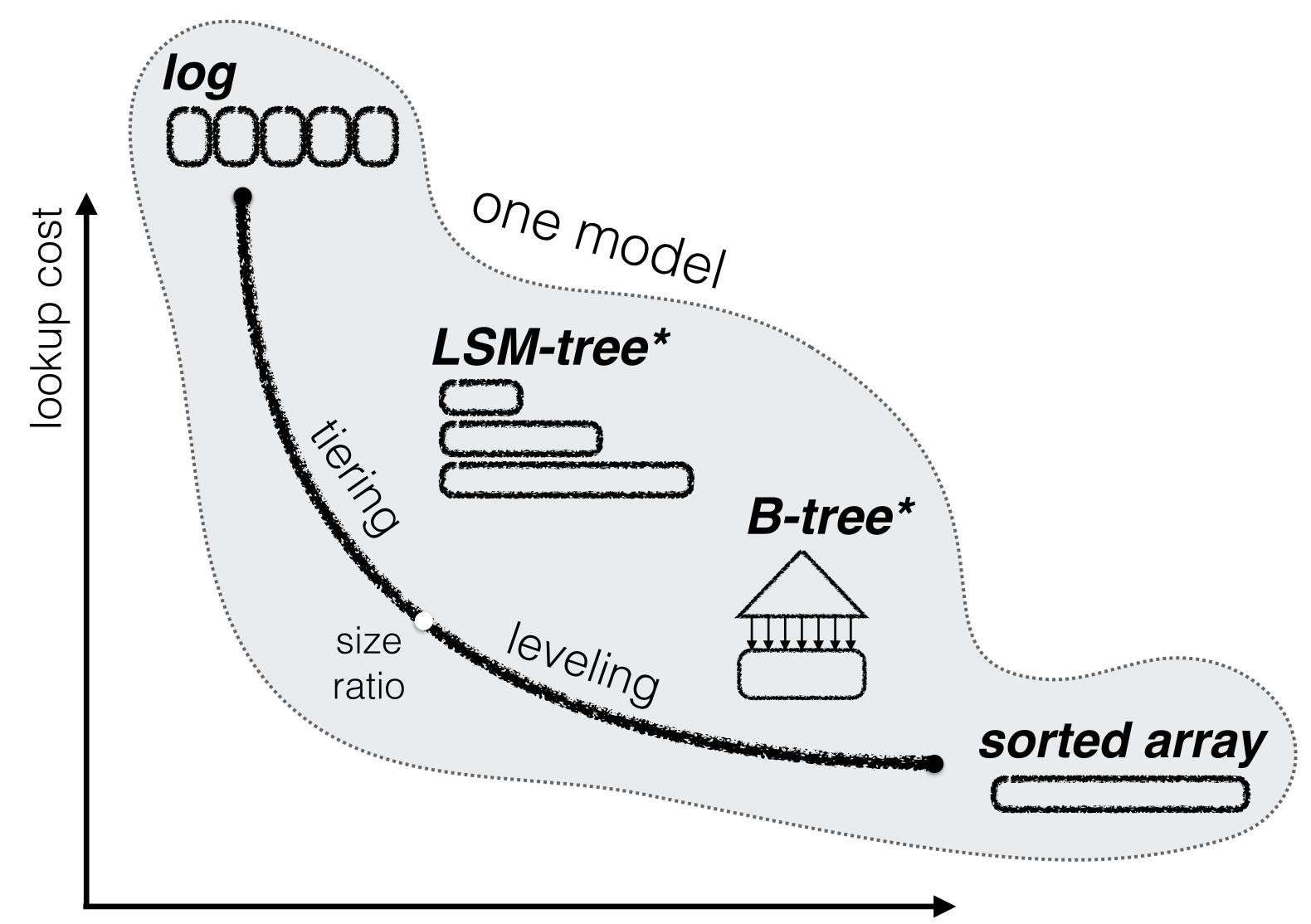




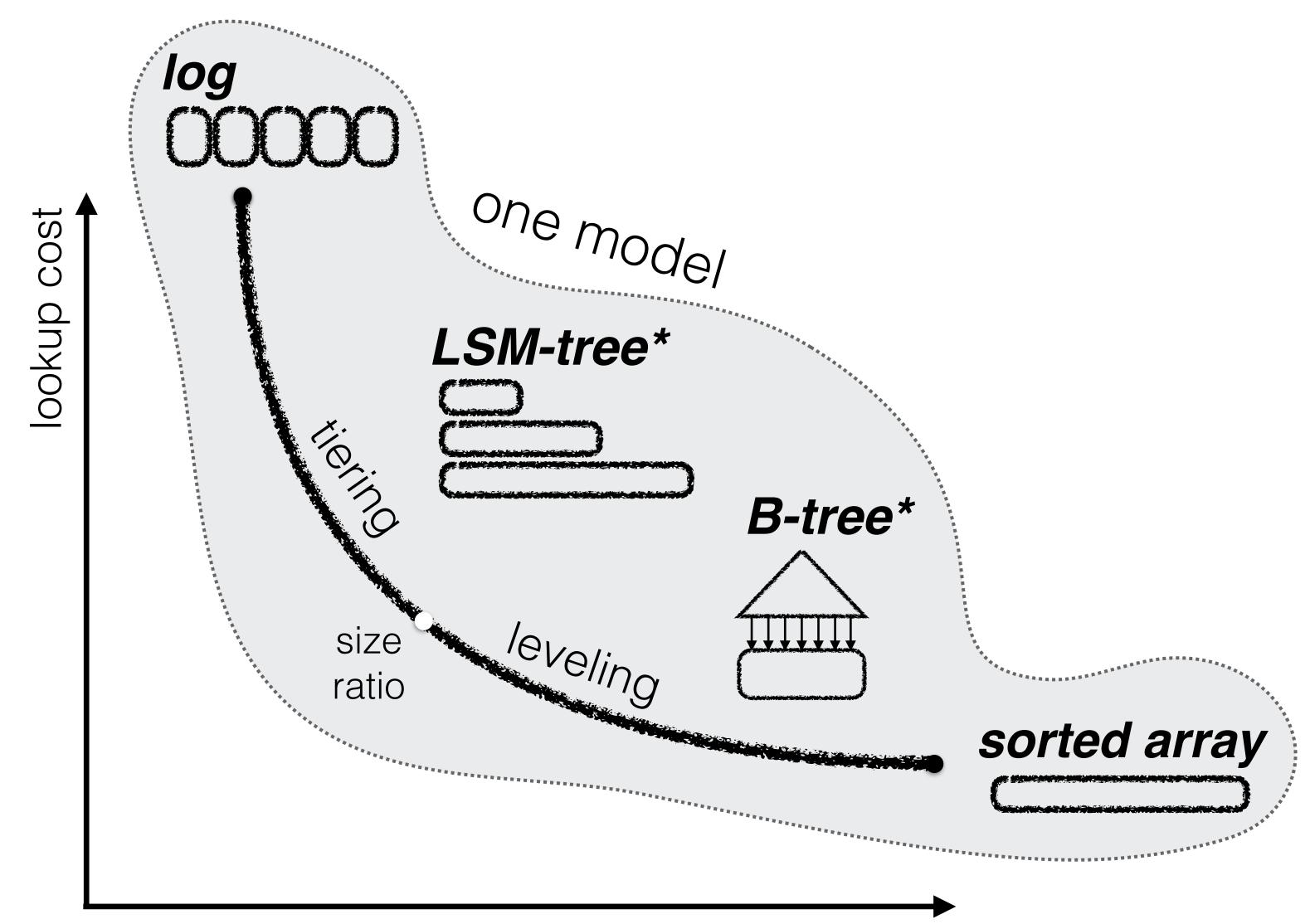








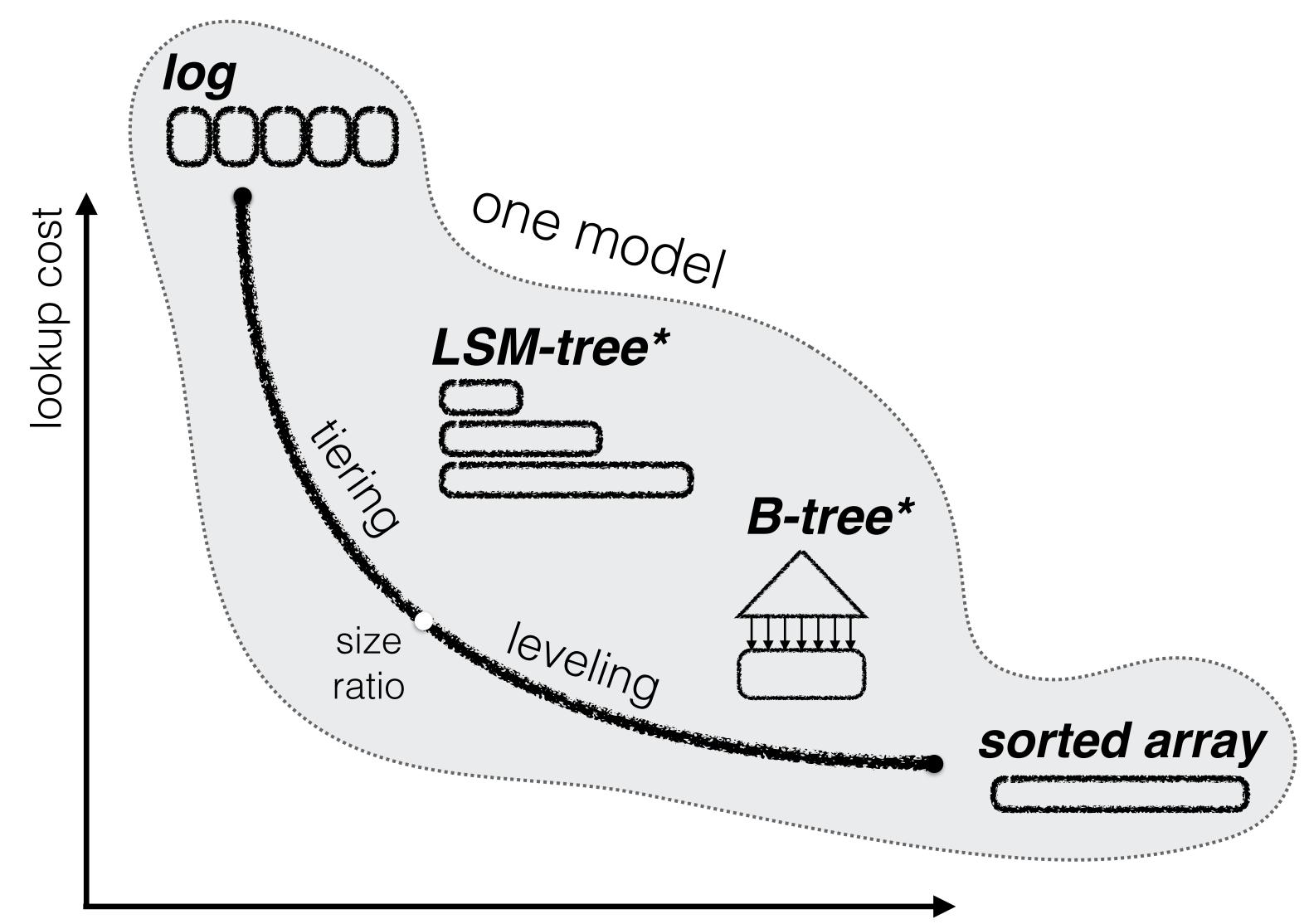






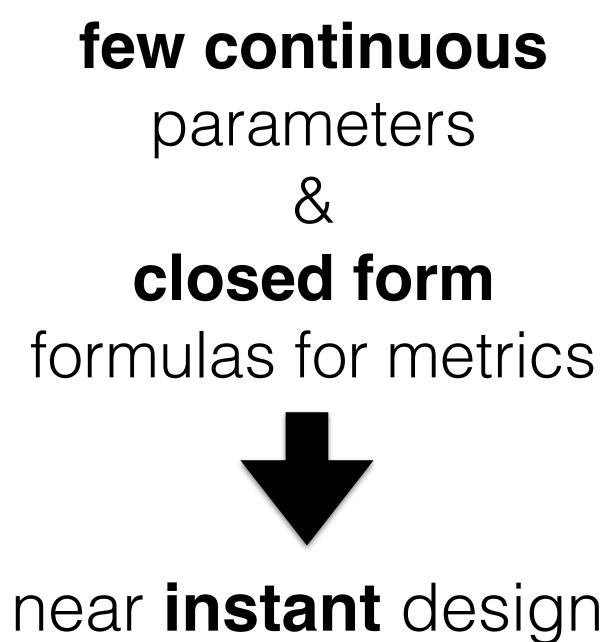
update cost

### few continuous parameters & closed form formulas for metrics

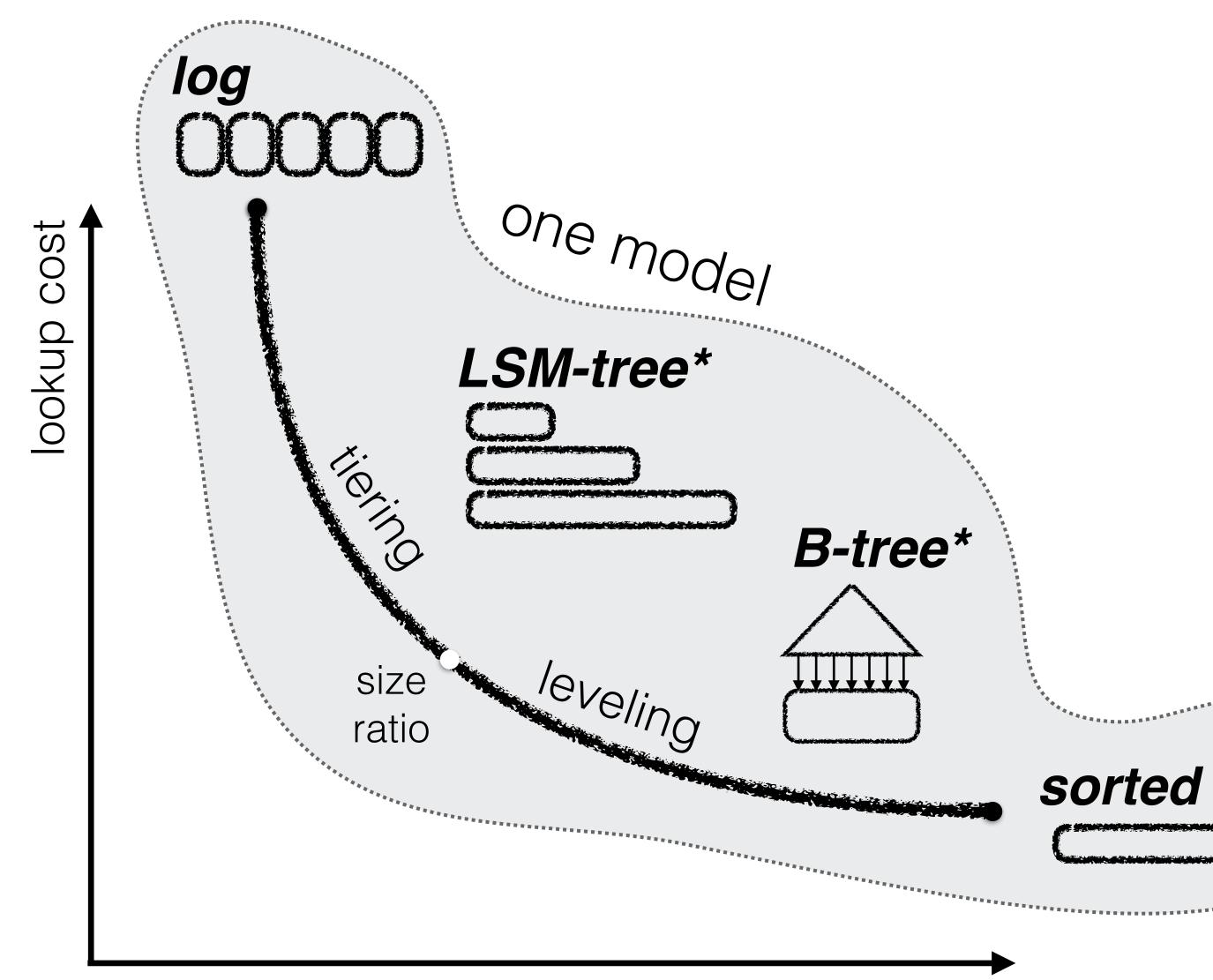




update cost

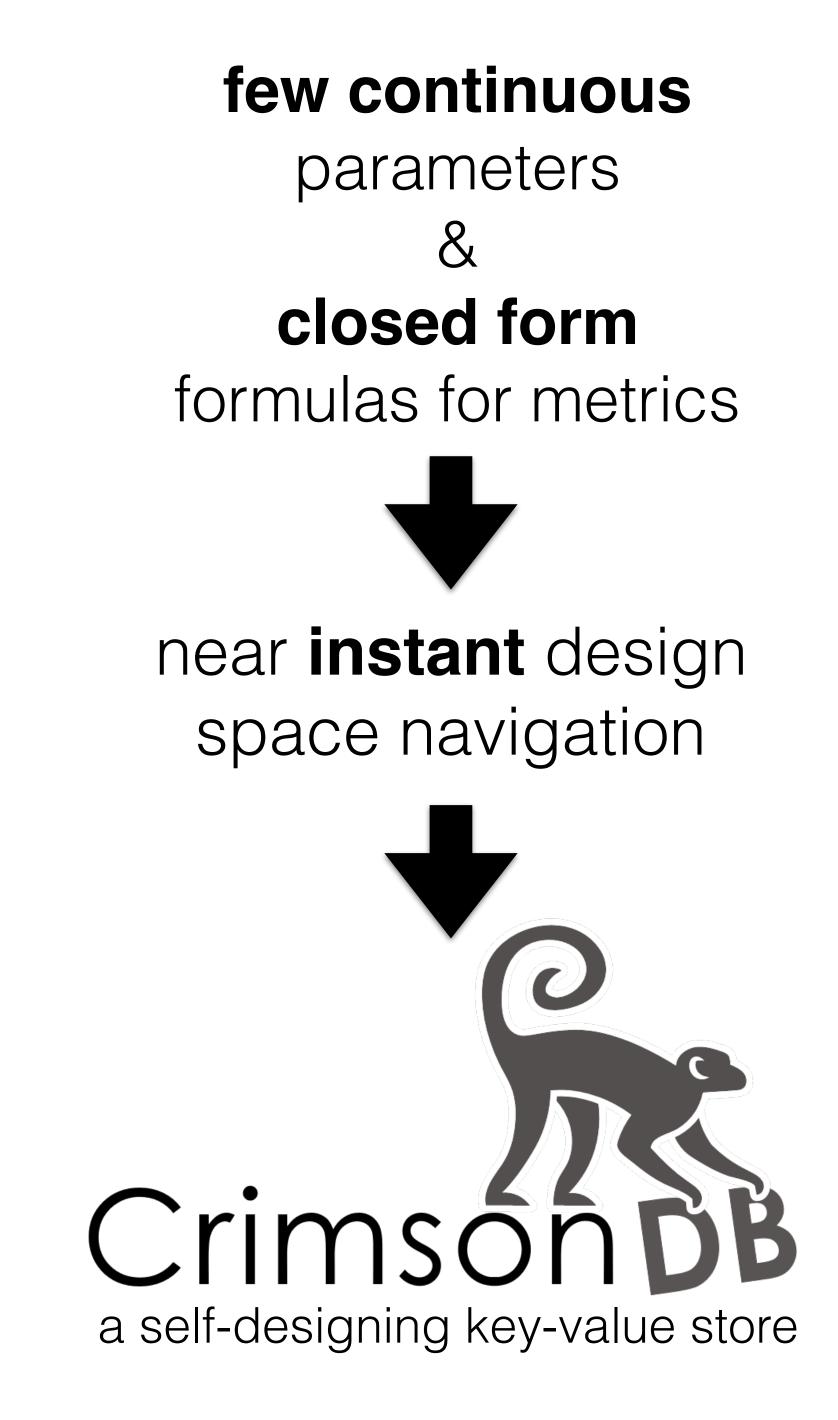


space navigation





update cost



sorted array

\*\*\*\*\*\*\*\*\*\*\*\*



### S. BING YAO models/advisors



### DON BATORY modular synthesis



# JOE HELLERSTEIN extensible indexing



### STEFAN MANEGOLD model synthesis



### daslab.seas.harvard.edu

calculator infrastructure



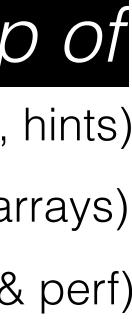
COST SYNTHESIS (accuracy, scalability) GO AFTER GAPS (new design opport.) SELF-DESIGNING (log to sorted arrays)

## study structure & gaps

## building more on top of

DESIGN SPACE (updates, concurrency) DESIGN CONTINUUMS (optimizations) AUTO-SEARCH (ML/algo hybrids, hints)

EASY EXTENSIBILITY (plug & play rules) DESIGN GUIDE (static design rule sys) DSL & COMPILERS (productivity & perf)





Manos Athanassoulis Postdoctoral Researcher



**Brian Hentschel** Ph.D. Researcher



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Niv Dayan Postdoctoral Researcher



Kostas Zoumpatianos Postdoctoral Researcher



**Michael Kester** Ph.D. Researcher



Lukas Maas Ph.D. Researcher





Wilson Qin Ph.D. Researcher



Angelo **Kastroulis** Graduate Researcher



**Franco Solleza** Graduate Researcher



Mali Akmanalp Graduate Researcher



Graduate Researcher

**Dhruv Gupta** Undergraduate Researcher



**Demi Guo** Undergraduate Researcher



Yiyou Sun Undergraduate **Research Intern** 



Mo Sun Undergraduate **Research** Intern



Yuze Liao Undergraduate **Research Intern** 





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